



# *Self-Organization and Traffic Dynamics*

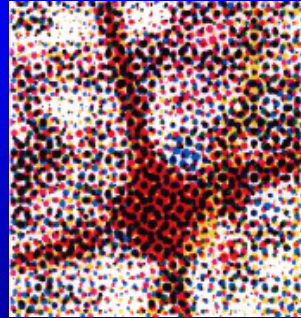
**Organic Computing, Bochum, 20 February 2009**

Prof. Dr. Michael Schreckenberg  
Physics of Transport and Traffic  
Universität Duisburg-Essen



# *Physics of Transport and Traffic*

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Since 1997 at the University of Duisburg-Essen

10 Coworkers

Study: Physics of Transport and Traffic

Topics: Analysis, Modeling, Simulation  
und Optimization of Transport Systems



# *Physics of Transport and Traffic*

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## Topics:

- Road Traffic
- Railway Traffic
- Intelligent Transport Systems
- Traffic Forecast
- Evacuation Processes
- Inland-Shipway-Traffic
- Air Traffic
- Education!



# *The „Problem“*

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**„All bad luck of the human beings stems  
from the fact, that they are not able  
to stay calmly in a room“**

**(Blaise Pascal, Pensée, 1640)**





# *Tokai TV*

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# *A3 North at the Intersection Duisburg-Kaiserberg*

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# *Traffic Data Detection*

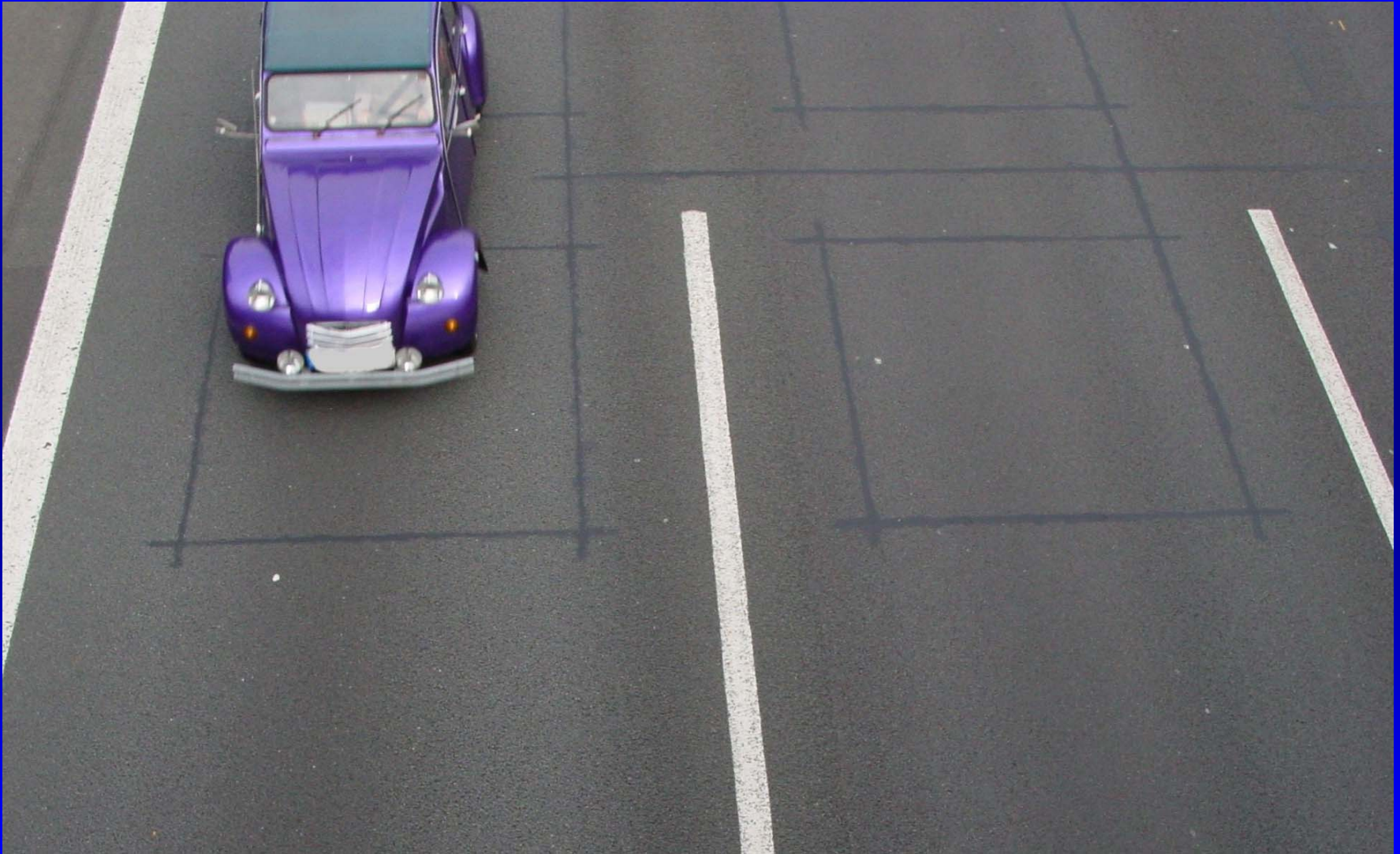
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- Inductive loops
- Radar sensors
- Traffic eyes (infrared)
- Video
- Floating cars / cellular phone (location)
- Air photography / video (plane, zeppelin, hot-air ballon, satellite)



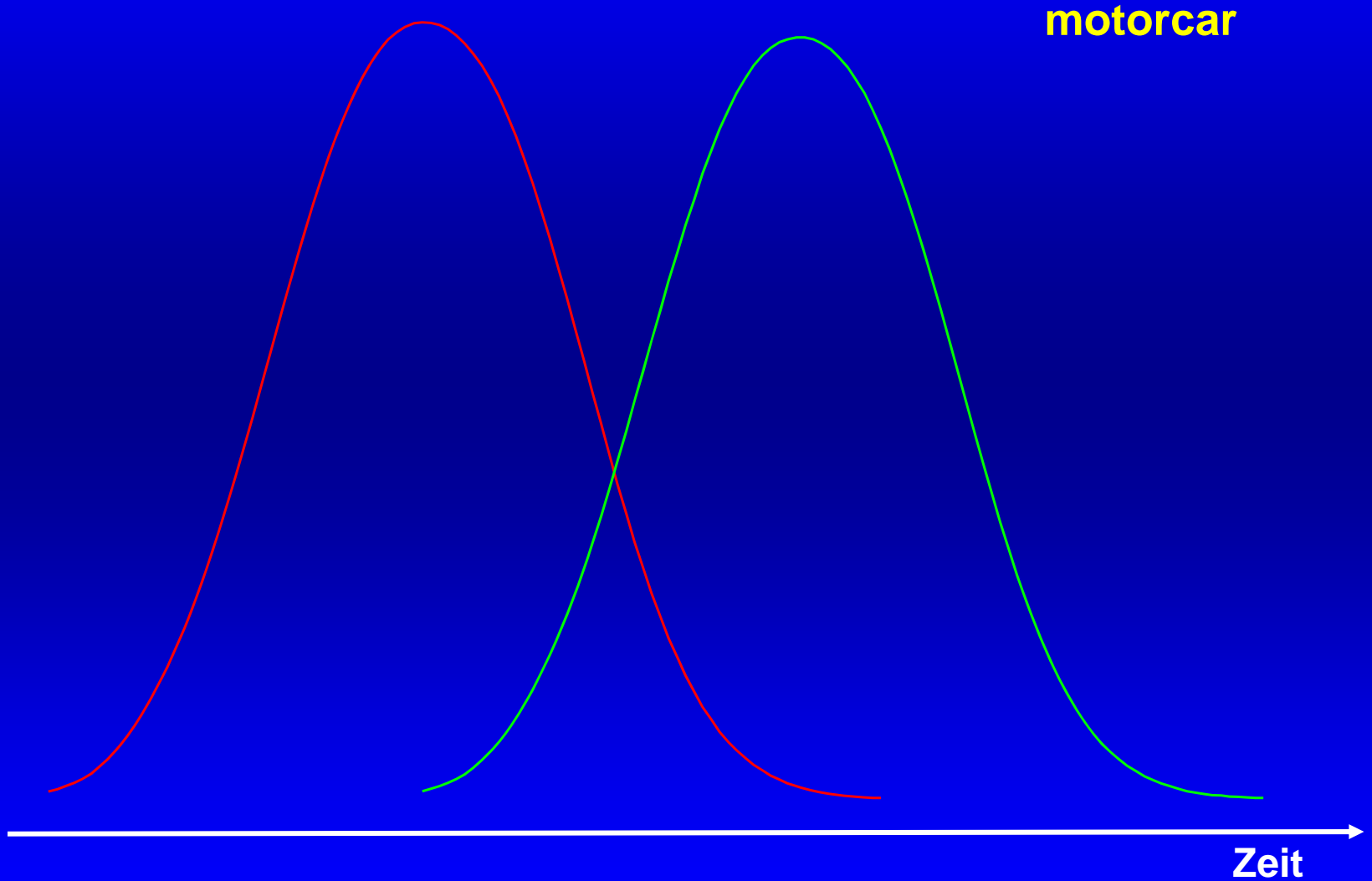
# *Inductive Loops*

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# *Signatures I*

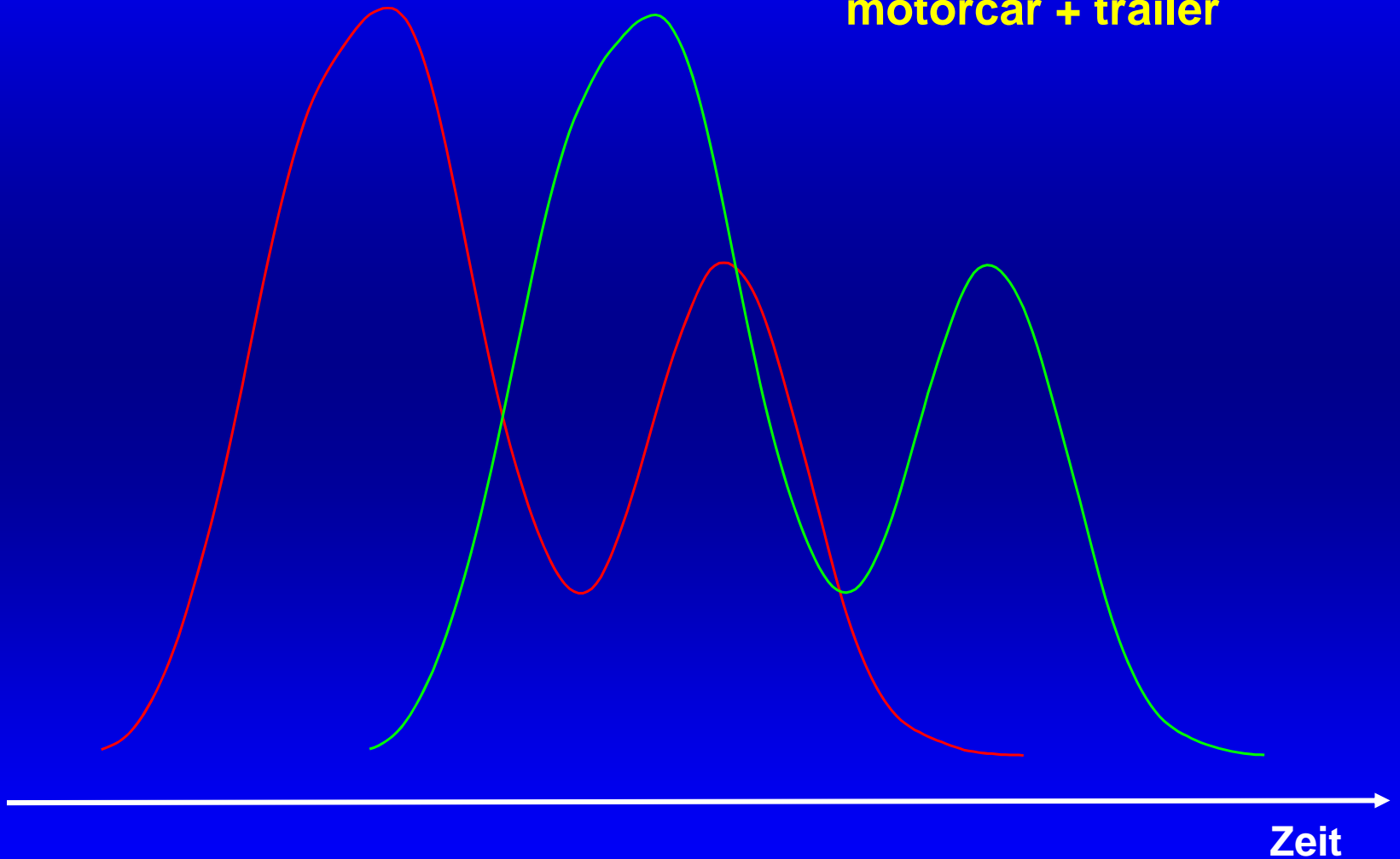
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# *Signatures II*

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**motorcar + trailer**

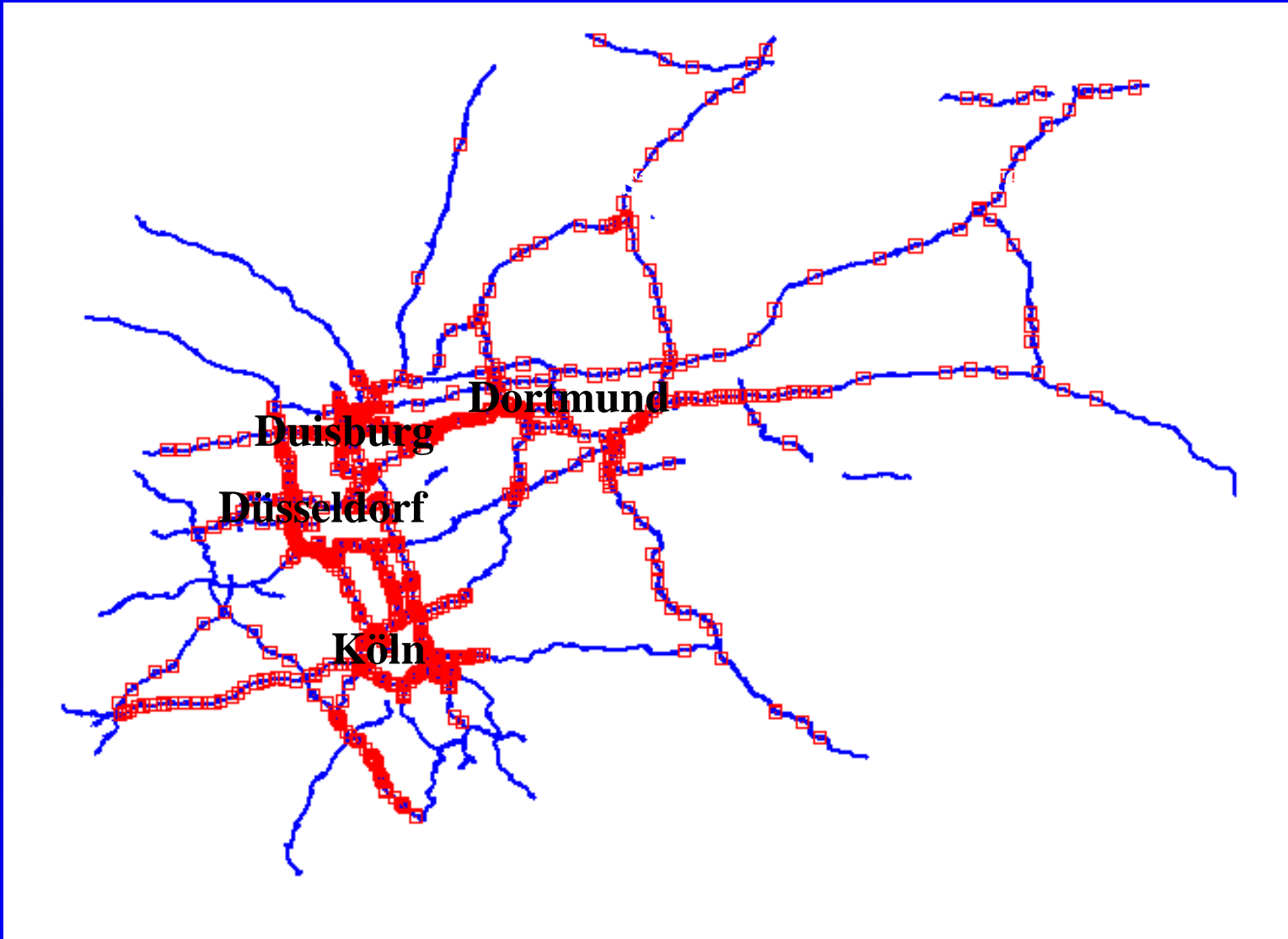


# Signatures III

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# *Inductive Loops in the Highways of NRW*



# Data Format

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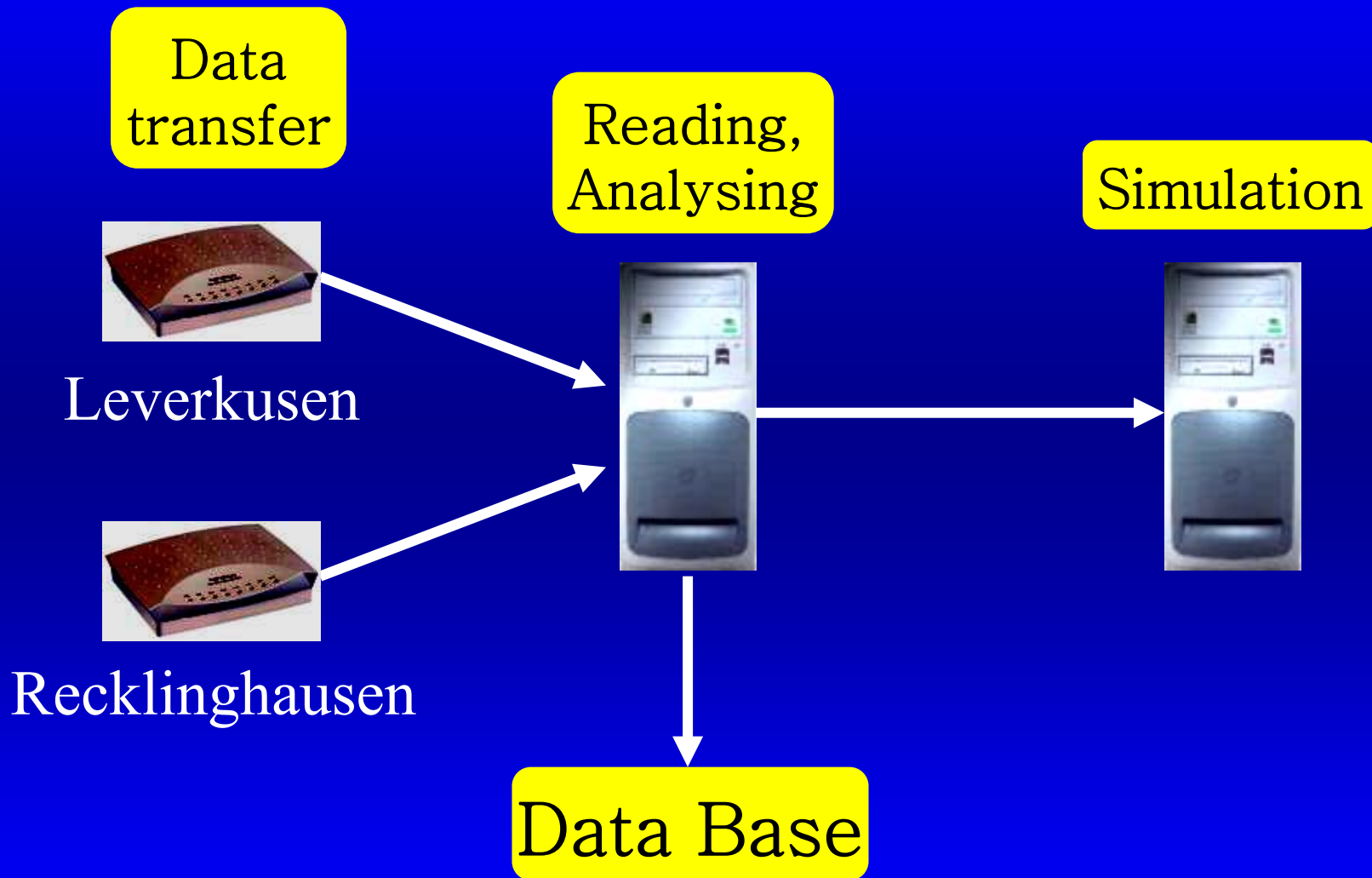
20020915 30 8 1 105 84 73 1 21 100  
20020915 31 5 0 104 0 119 0 12 102  
20020915 32 11 2 100 83 53 2 14 88  
20020915 33 8 0 103 0 74 0 11 103  
20020915 34 6 1 100 80 97 2 13 100  
20020915 35 8 2 103 85 74 1 18 110  
20020915 36 6 0 96 0 99 0 2 98  
20020915 37 6 0 96 0 99 0 2 98  
20020915 38 7 0 95 0 85 0 14 100  
20020915 39 8 4 107 89 72 3 19 109  
20020915 40 8 4 107 89 72 3 19 109  
20020915 41 12 1 104 64 48 2 15 96  
20020915 42 4 0 97 0 149 0 9 96  
20020915 43 6 1 97 87 98 1 6 95  
20020915 44 7 0 97 0 85 0 8 97  
20020915 45 8 1 103 90 73 2 8 98  
20020915 46 8 1 103 90 73 2 8 98  
20020915 47 3 0 100 0 199 0 14 95  
20020915 48 7 1 98 91 84 1 13 94

20020915 50 7 0 106 0 85 0 13 103  
20020915 51 5 0 95 0 119 0 12 93  
20020915 52 11 3 95 79 52 3 14 81  
20020915 53 13 2 104 86 45 2 13 106  
20020915 54 4 0 111 0 148 0 28 108  
20020915 55 6 2 95 87 98 1 8 93  
20020915 56 9 0 94 0 65 1 4 96  
20020915 57 6 0 99 0 99 0 14 96  
20020915 58 3 0 98 0 199 0 18 97  
20020915 59 5 0 104 0 118 0 8 103  
20020915 60 4 0 107 0 149 0 17 104  
20020915 61 4 1 91 81 148 1 13 89  
20020915 62 7 0 101 0 85 0 10 101  
20020915 63 1 1 0 89 254 0 255 98  
20020915 65 5 1 101 92 118 1 14 97  
20020915 64 5 1 101 92 118 1 14 97  
20020915 66 8 1 100 86 73 2 16 93  
20020915 67 5 1 100 92 118 1 13 97  
20020915 68 4 0 89 0 149 0 3 92

20020915 69 7 0 89 0 84 1 9 92  
20020915 70 6 1 104 97 99 0 8 101  
20020915 71 6 0 101 0 99 0 14 104  
20020915 72 1 0 91 0 254 0 255 101  
20020915 73 4 0 106 0 149 0 16 106  
20020915 74 6 1 111 82 98 1 17 106  
20020915 75 9 0 101 0 66 0 9 103  
20020915 76 7 0 108 0 85 0 16 105  
20020915 77 6 0 100 0 98 0 13 105  
20020915 78 5 1 91 70 118 1 13 92  
20020915 79 4 1 97 91 148 1 9 96  
20020915 80 8 0 105 0 74 1 10 107  
20020915 81 9 0 95 0 65 1 16 99  
20020915 82 5 0 104 0 119 0 11 104  
20020915 83 9 1 102 98 65 1 14 108  
20020915 84 6 1 97 78 98 2 9 96  
20020915 85 8 1 91 86 73 1 13 91  
20020915 86 7 4 102 93 83 2 9 96  
20020915 87 10 0 96 0 59 1 11 100



# Data Transfer





# *The Energy Problem*

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- Oil (ltd)
- Natural gas (ltd)
- Solar car (slow)
- Electric car (losses?)
- Water-diesel mixture (not stable)
- Fuel cell (hydrogen is only energy carrier! (80% loss))
- Rape (monoculture)
- Methanol (natural gas)
- Ethanol (rape, sugar cane / beet))
- Human power



# Traffic Data: Example of Inductive Loops

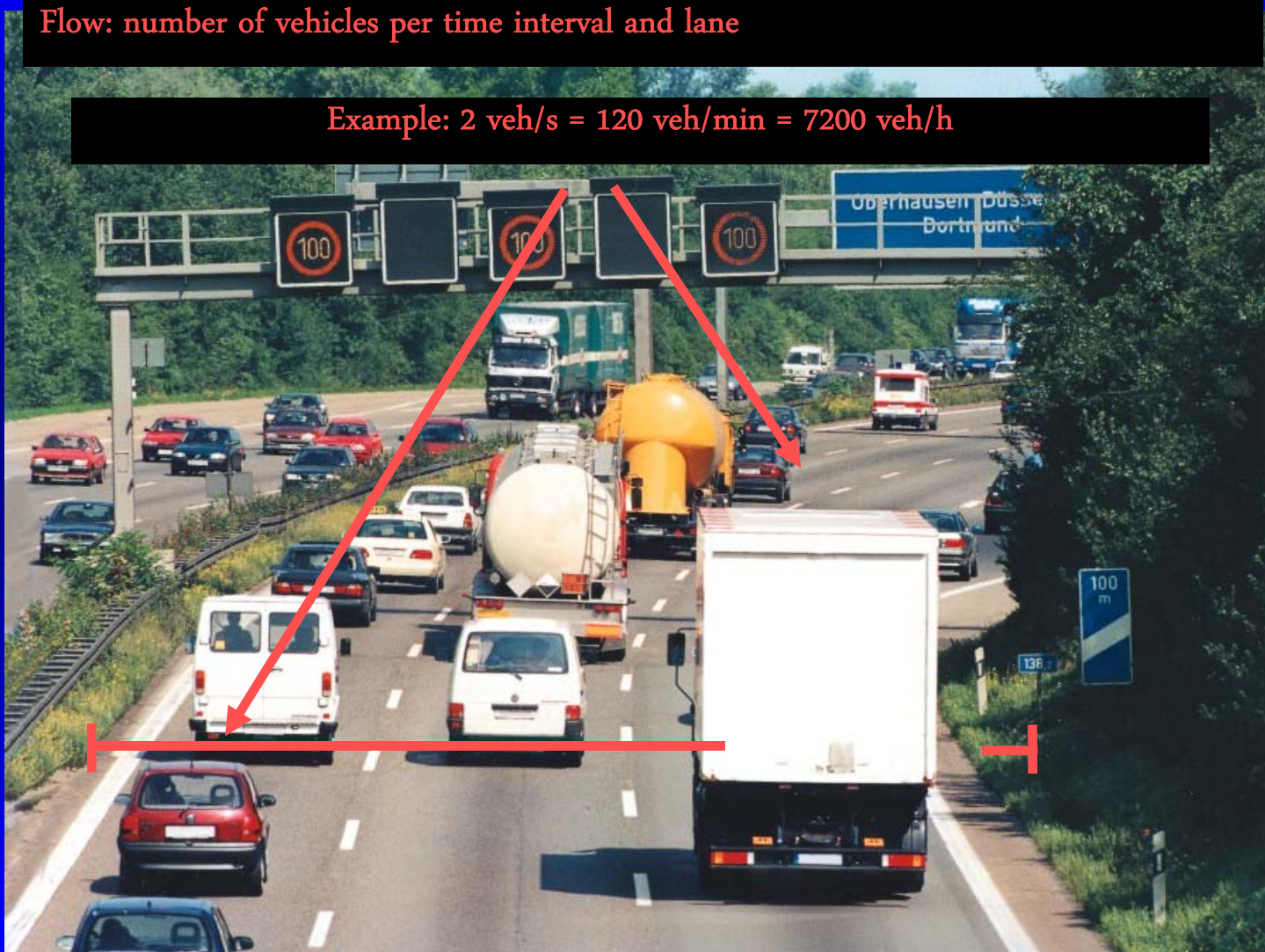




# Traffic Data: Example of Inductive Loops

Flow: number of vehicles per time interval and lane

Example:  $2 \text{ veh/s} = 120 \text{ veh/min} = 7200 \text{ veh/h}$



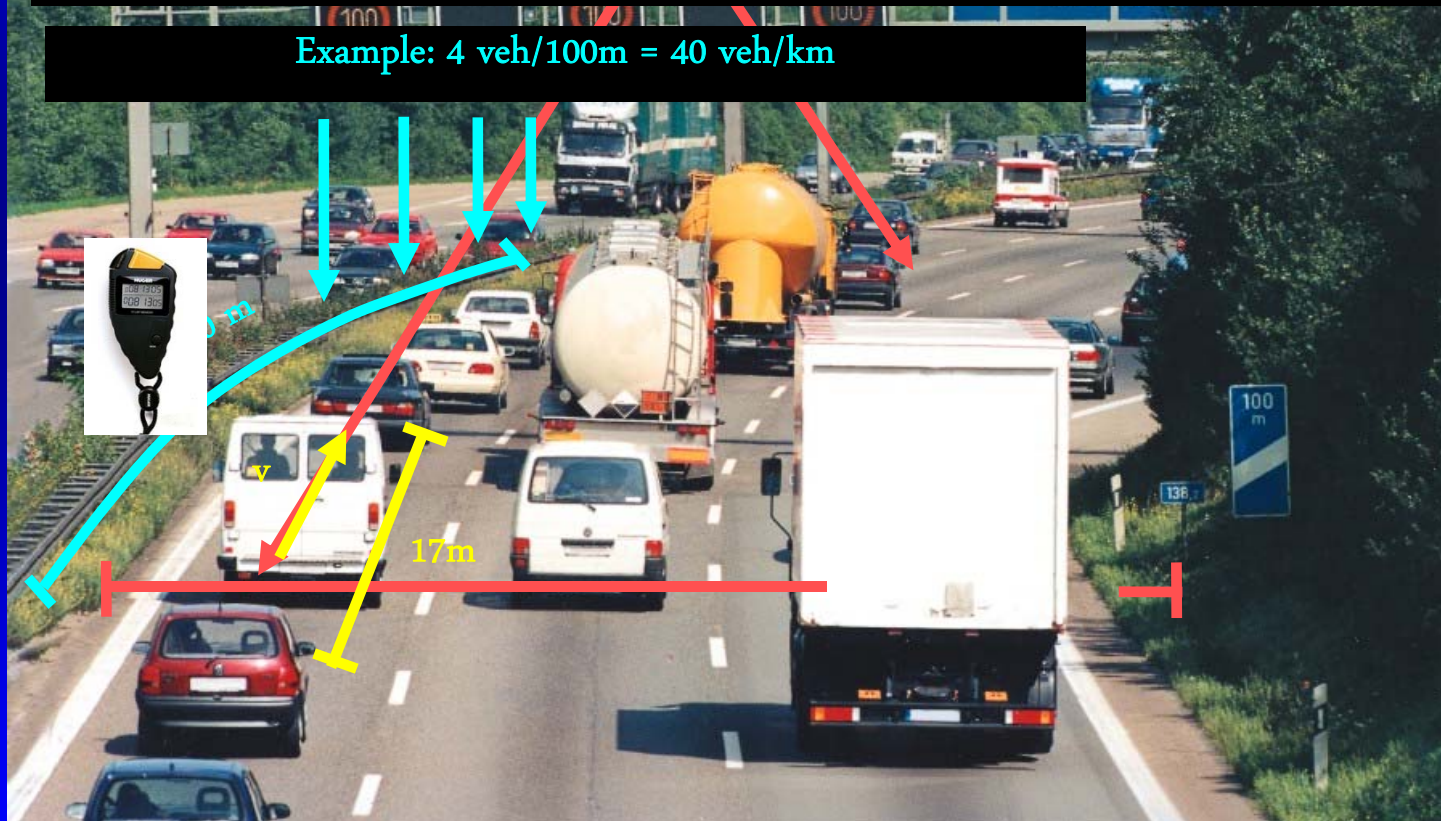
# Traffic Data: Example of Inductive Loops

Flow: number of vehicles per time interval and lane

Speed: distance per time interval

Example: 17 m/s = 61 km/h

Example: 4 veh/100m = 40 veh/km



# Data Format

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20020915 30 8 1 105 84 73 1 21 100  
20020915 31 5 0 104 0 119 0 12 102  
20020915 32 11 2 100 83 53 2 14 88  
20020915 33 8 0 103 0 74 0 11 103  
20020915 34 6 1 100 80 97 2 13 100  
20020915 35 8 2 103 85 74 1 18 110  
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20020915 37 6 0 96 0 99 0 2 98  
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20020915 43 6 1 97 87 98 1 6 95  
20020915 44 7 0 97 0 85 0 8 97  
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20020915 48 7 1 98 91 84 1 13 94

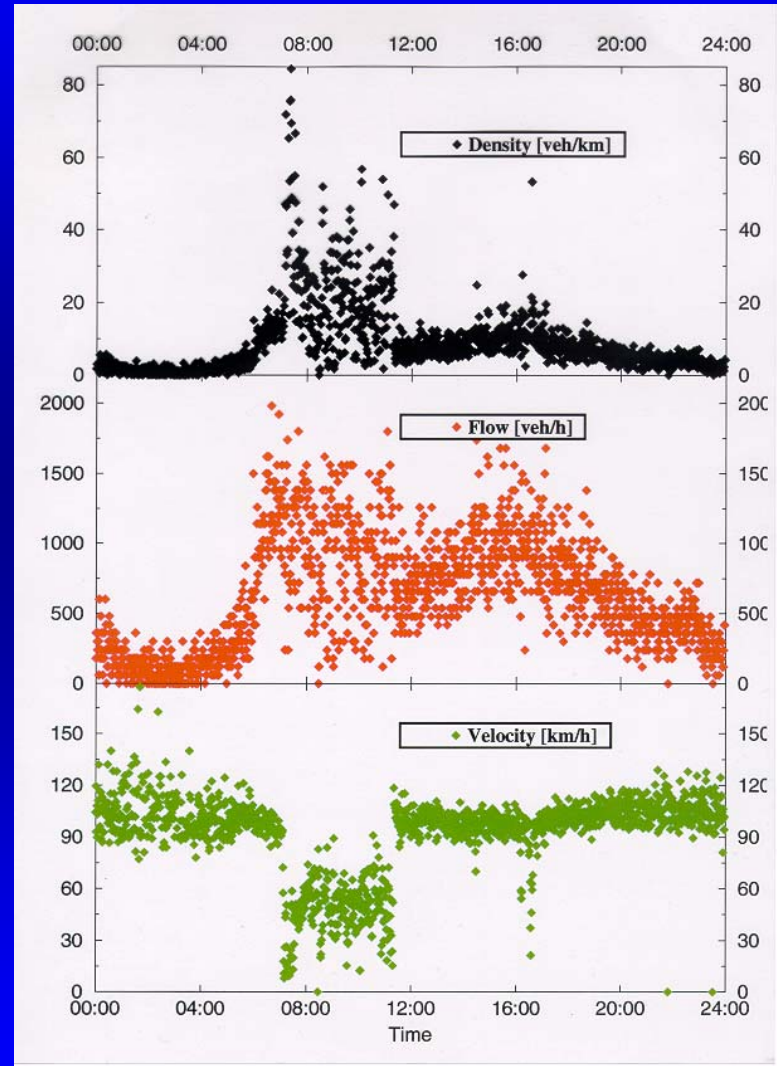
20020915 50 7 0 106 0 85 0 13 103  
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20020915 52 11 3 95 79 52 3 14 81  
20020915 53 13 2 104 86 45 2 13 106  
20020915 54 4 0 111 0 148 0 28 108  
20020915 55 6 2 95 87 98 1 8 93  
20020915 56 9 0 94 0 65 1 4 96  
20020915 57 6 0 99 0 99 0 14 96  
20020915 58 3 0 98 0 199 0 18 97  
20020915 59 5 0 104 0 118 0 8 103  
20020915 60 4 0 107 0 149 0 17 104  
20020915 61 4 1 91 81 148 1 13 89  
20020915 62 7 0 101 0 85 0 10 101  
20020915 63 1 1 0 89 254 0 255 98  
20020915 65 5 1 101 92 118 1 14 97  
20020915 64 5 1 101 92 118 1 14 97  
20020915 66 8 1 100 86 73 2 16 93  
20020915 67 5 1 100 92 118 1 13 97  
20020915 68 4 0 89 0 149 0 3 92

20020915 69 7 0 89 0 84 1 9 92  
20020915 70 6 1 104 97 99 0 8 101  
20020915 71 6 0 101 0 99 0 14 104  
20020915 72 1 0 91 0 254 0 255 101  
20020915 73 4 0 106 0 149 0 16 106  
20020915 74 6 1 111 82 98 1 17 106  
20020915 75 9 0 101 0 66 0 9 103  
20020915 76 7 0 108 0 85 0 16 105  
20020915 77 6 0 100 0 98 0 13 105  
20020915 78 5 1 91 70 118 1 13 92  
20020915 79 4 1 97 91 148 1 9 96  
20020915 80 8 0 105 0 74 1 10 107  
20020915 81 9 0 95 0 65 1 16 99  
20020915 82 5 0 104 0 119 0 11 104  
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20020915 87 10 0 96 0 59 1 11 100

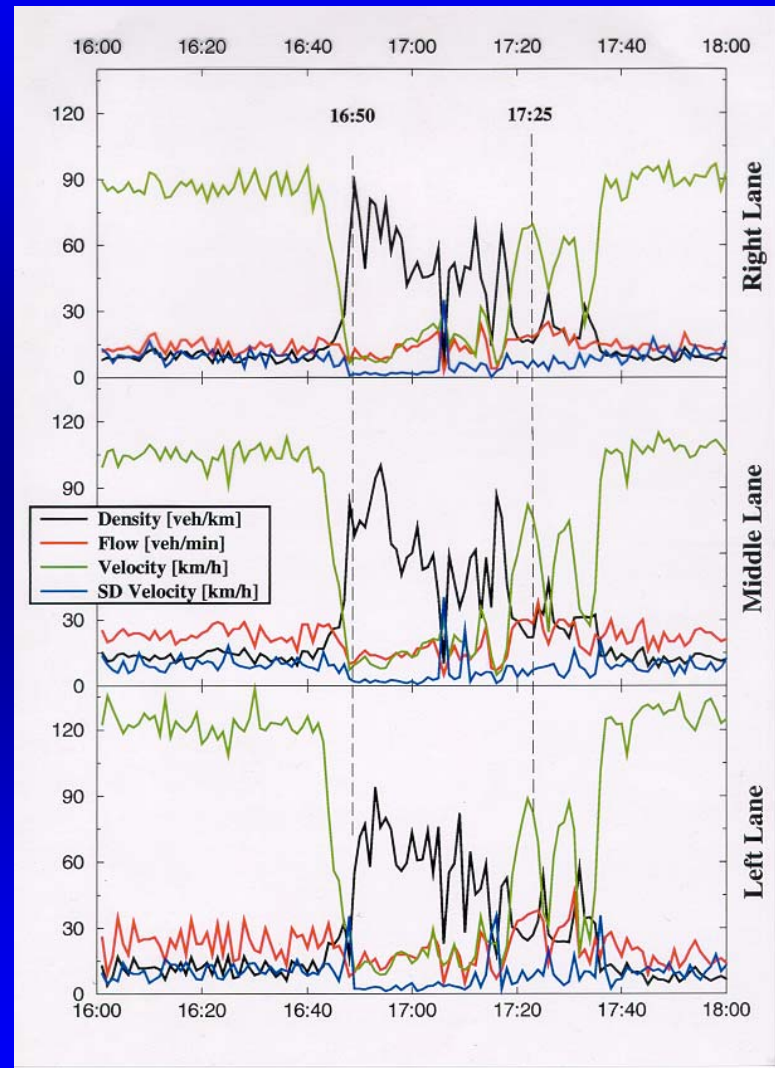




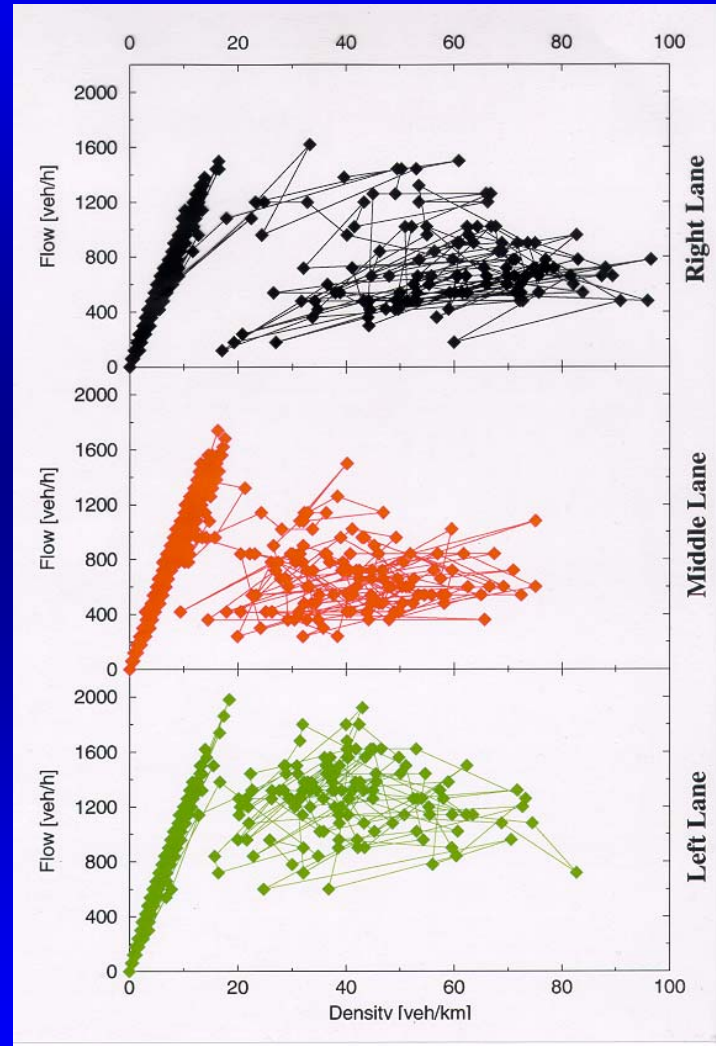
# Density/Flow/Velocity



# Lane Resolution and Traffic States

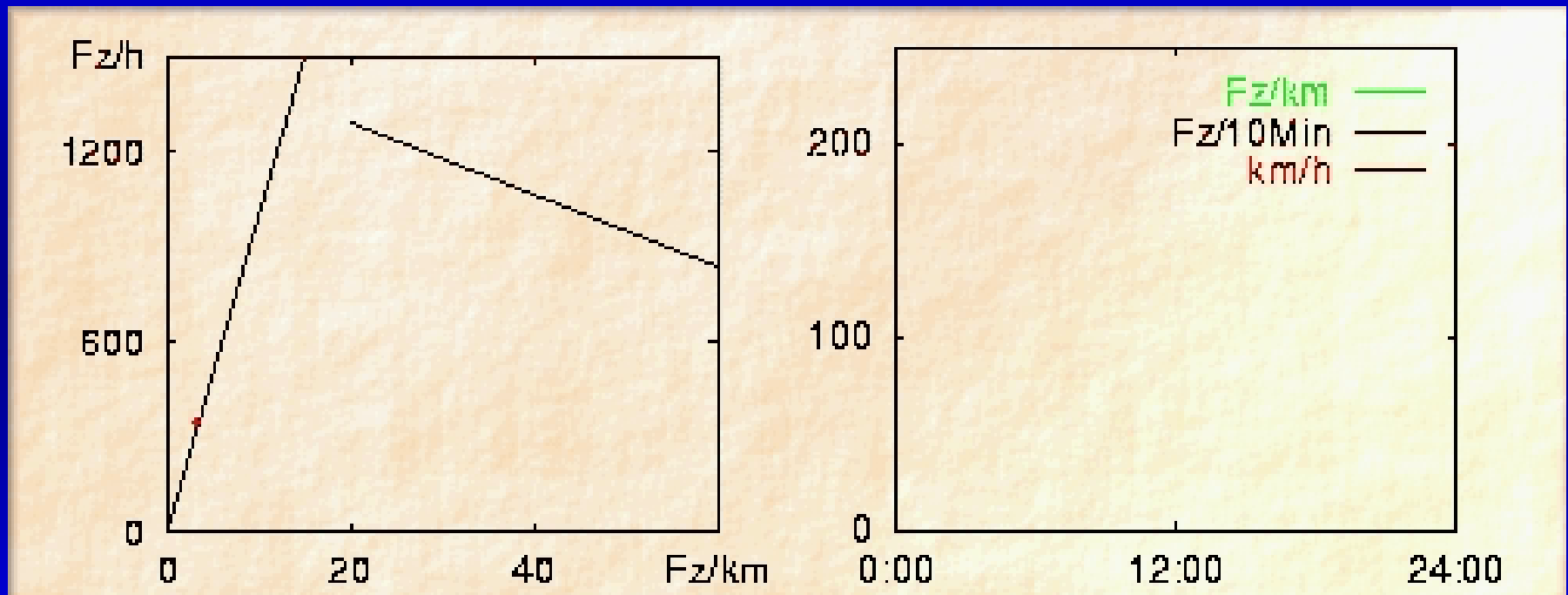


# Fundamental Diagram

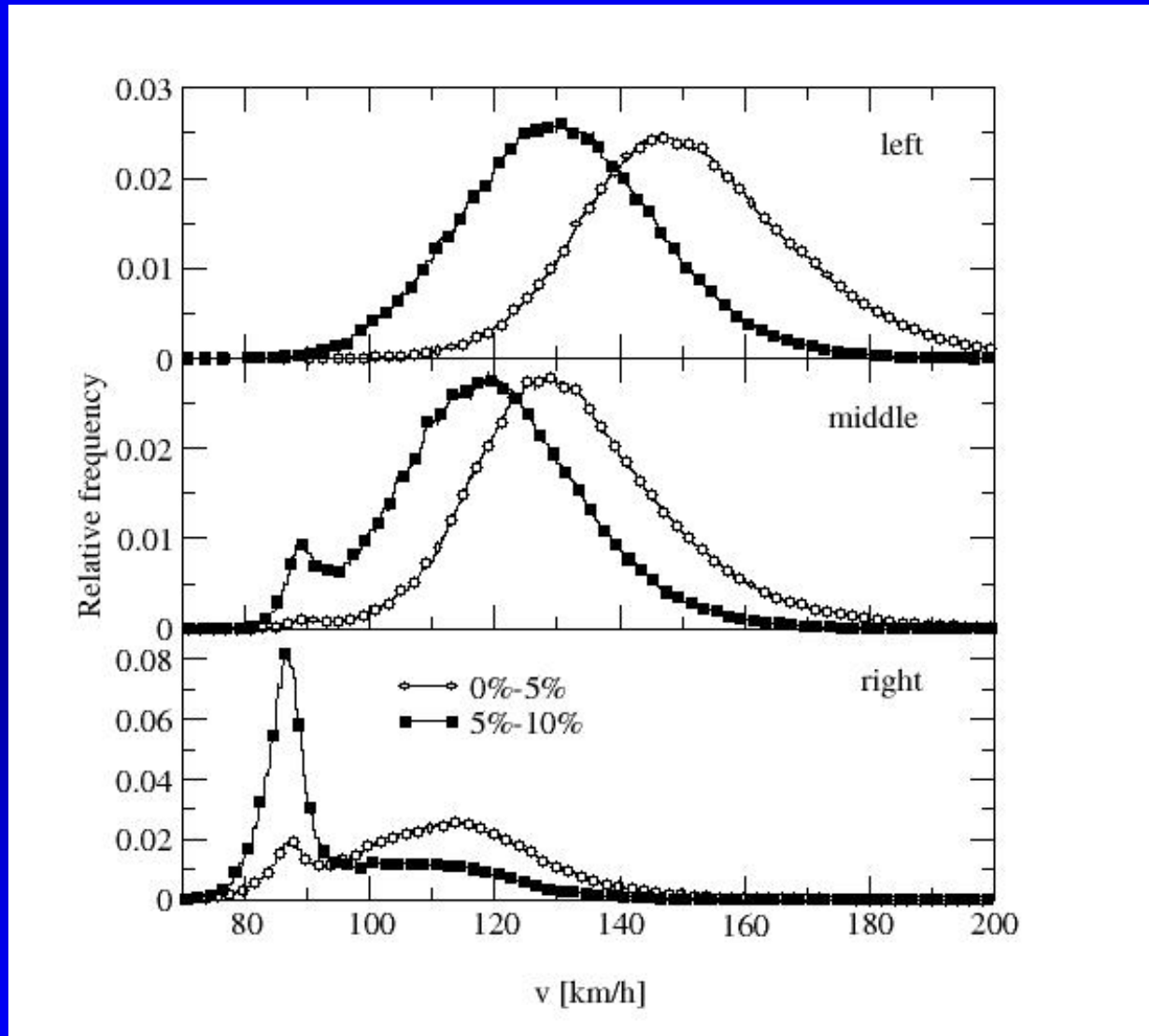




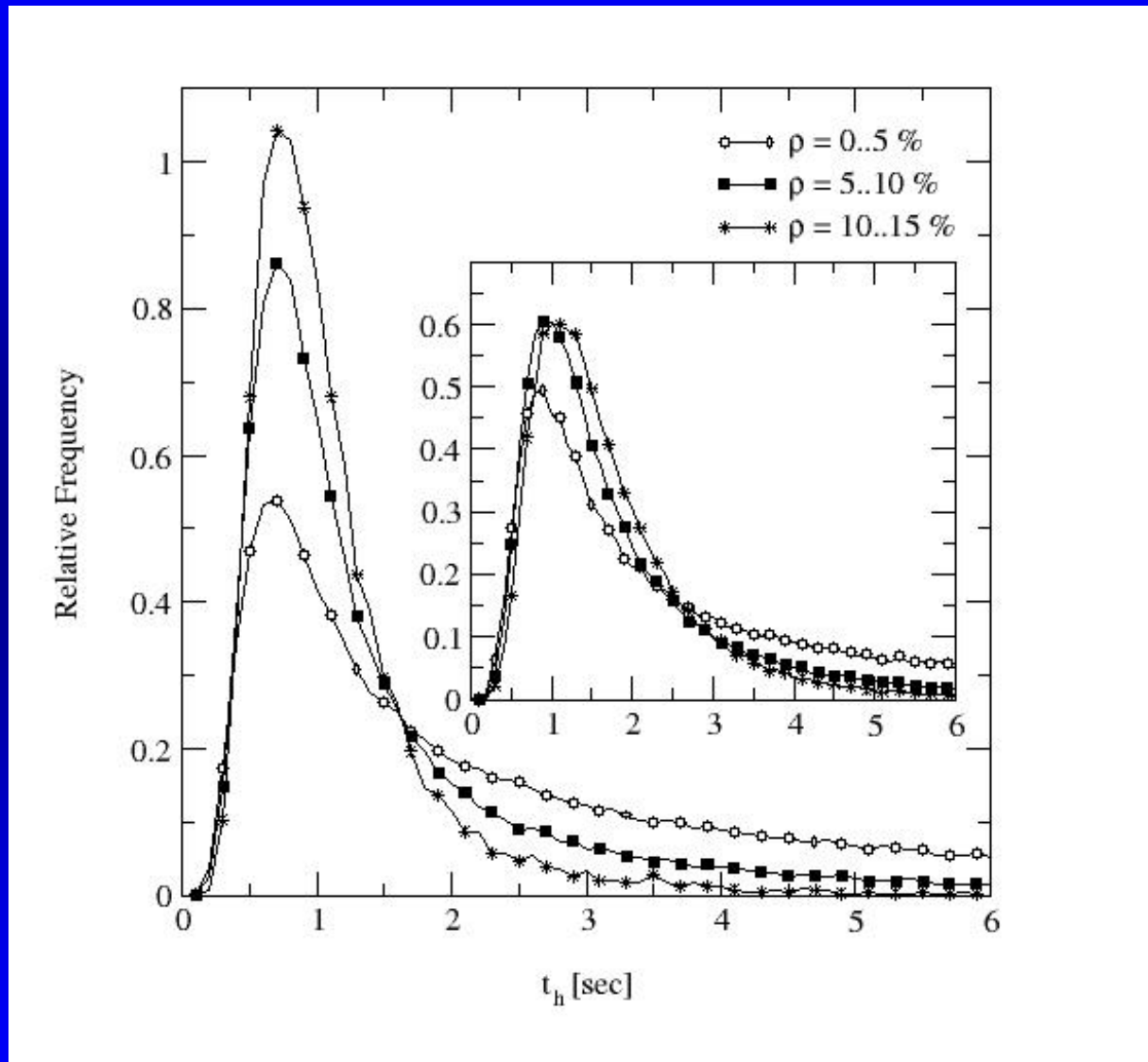
# Dynamic Flow-Density Relation



# Speed Distribution

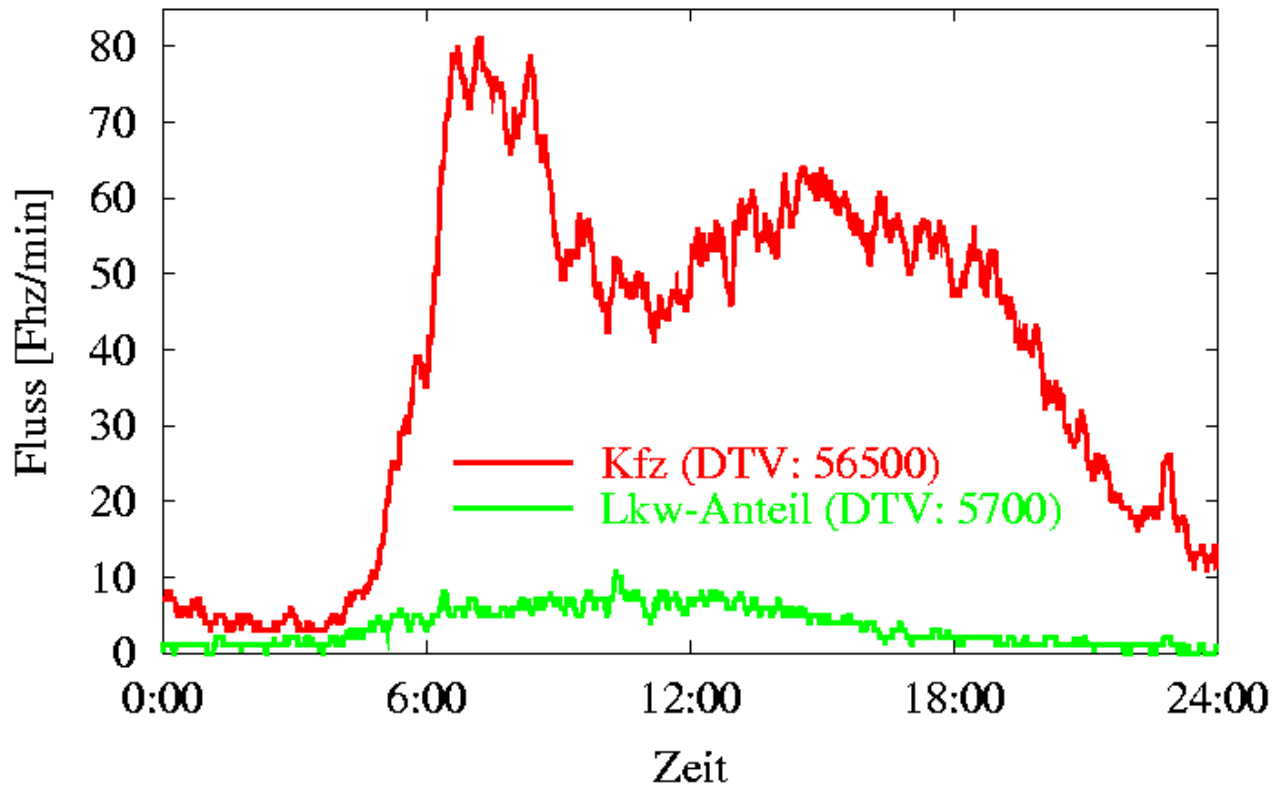


# Time Headways



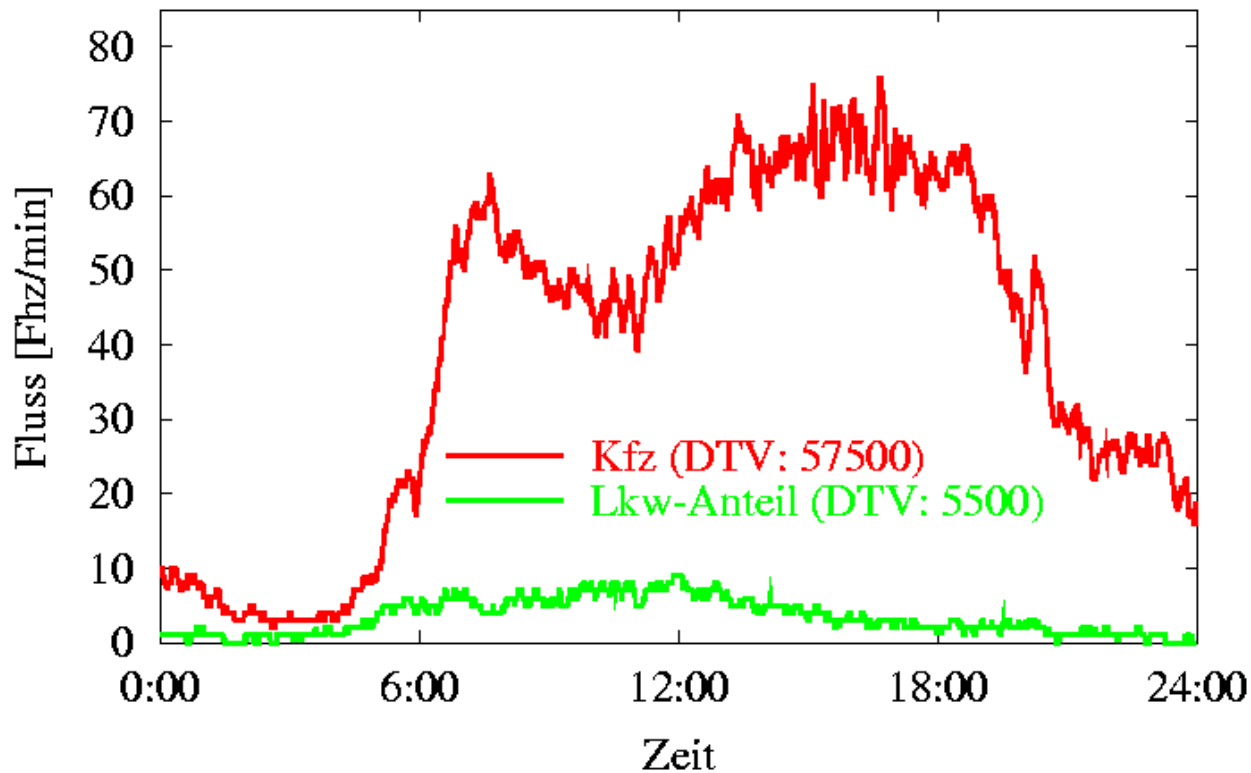
# Daily Traffic Load BAB: West

11.01.2002: A40 Gelsenkirchen-E.Kray Richtung Duisburg



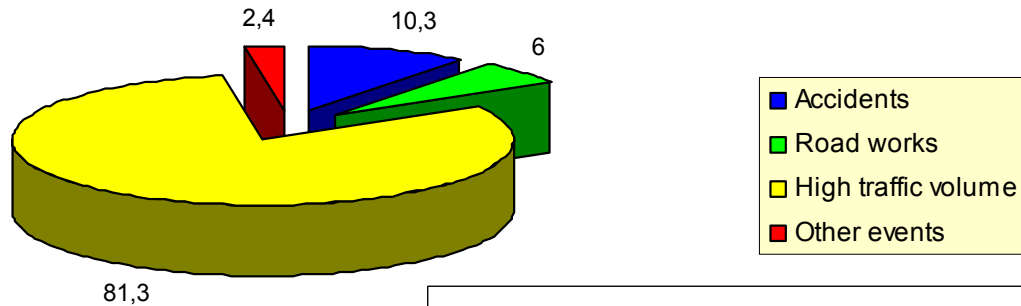
# Daily Traffic Load BAB: East

11.01.2002: A40 E.Kray-Gelsenkirchen Richtung Dortmund

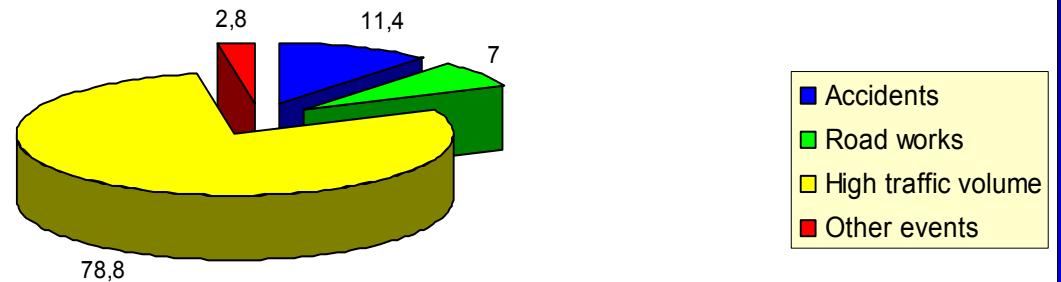


# Jam Statistics

Breakdown Statistics 2001



Breakdown Statistics 2002



# *General Strategy of Online-Simulations*

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- One-to-one (car by car) mapping of real traffic into the computer (via connection to detection devices, e.g. loops)
- Install a historical data base for evaluation and "background"
- Use a highly realistic but efficient microscopic simulation model ("Cellular Automaton", CA)
- Run the simulation and analyze the results: (e.g. actual flow pattern)
- Derive indirect quantities: travel times are measured by "virtual" floating cars
- Accelerate the simulation for a traffic forecast (again comparison with the historical data base)
- Formulate traffic informations
- ~~Include driver reactions on the information and iterate~~

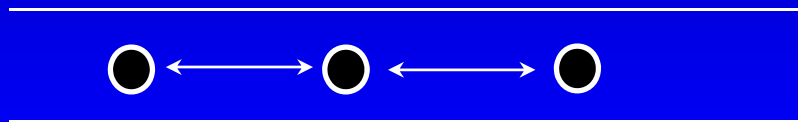


# Modelling Traffic Flow

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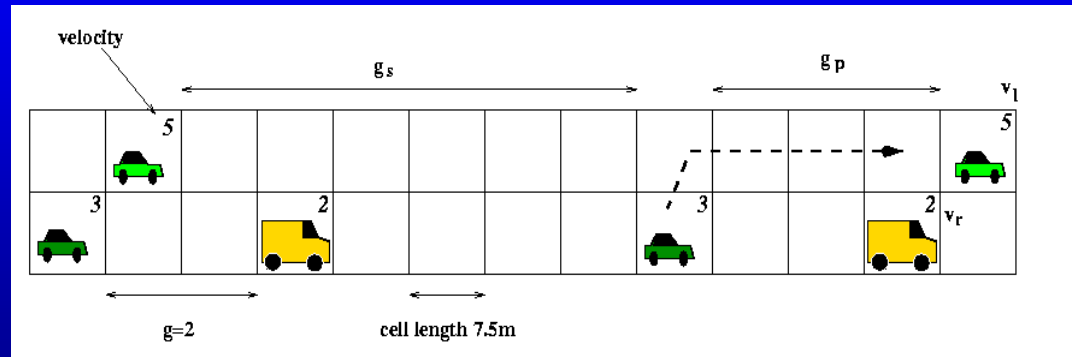
- Macroscopic models:
  - Traffic is similar to fluids
  - Continuity equation
  - Describe density waves
  - But: Assumption for function  $j(\rho)$
- Microscopic models:
  - Traffic is similar to granular media
  - Describe car-following (interaction)

$$\frac{\partial \rho}{\partial t} + \nabla \cdot \vec{j} = 0$$





# General Strategy

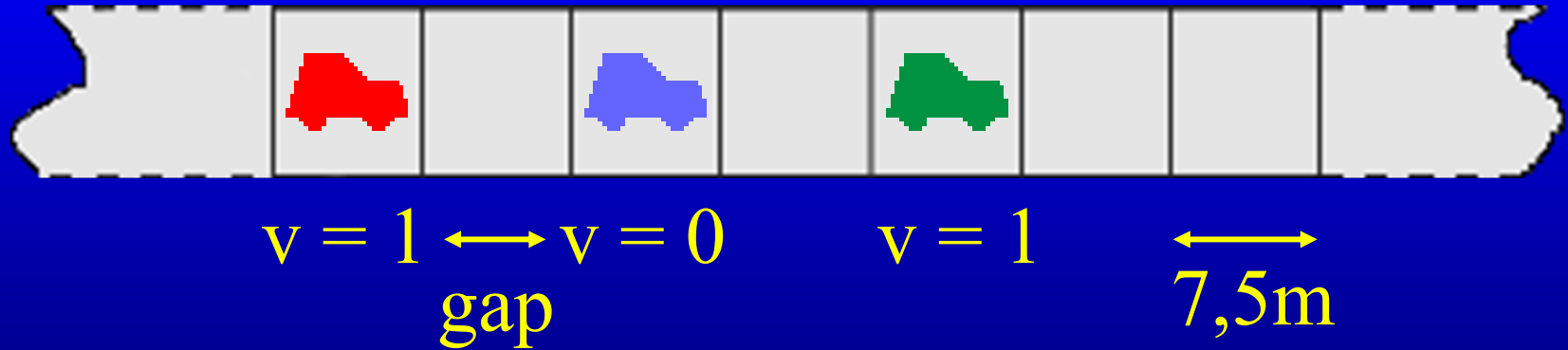


## Cellular Automaton (CA) Model:

- > Discrete in time and space
- > Dynamics through update rules (in parallel)
- > Fast and efficient algorithms
- > Analysis of dynamical phases:  
free, synchronized and wide moving jams



# Discrete Simulation Model

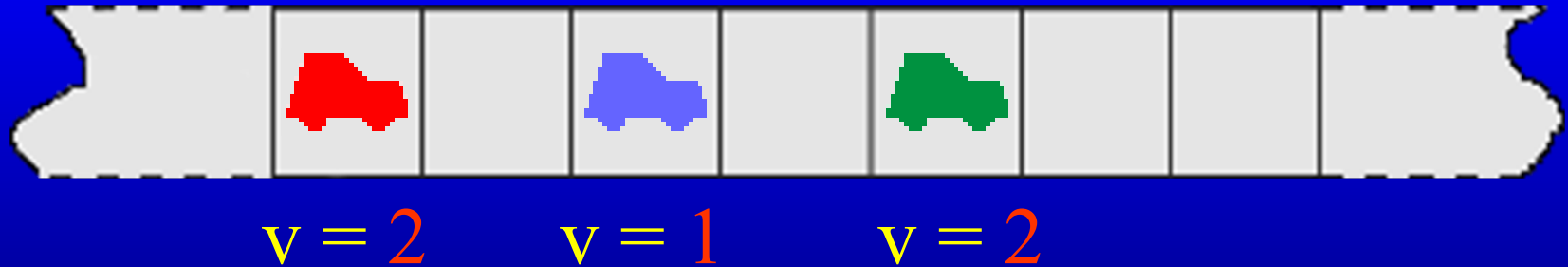


- Cell length = 7,5 m
- $v =$  speed
- gap = # of empty cells between the cars



# Cellular Automaton (I)

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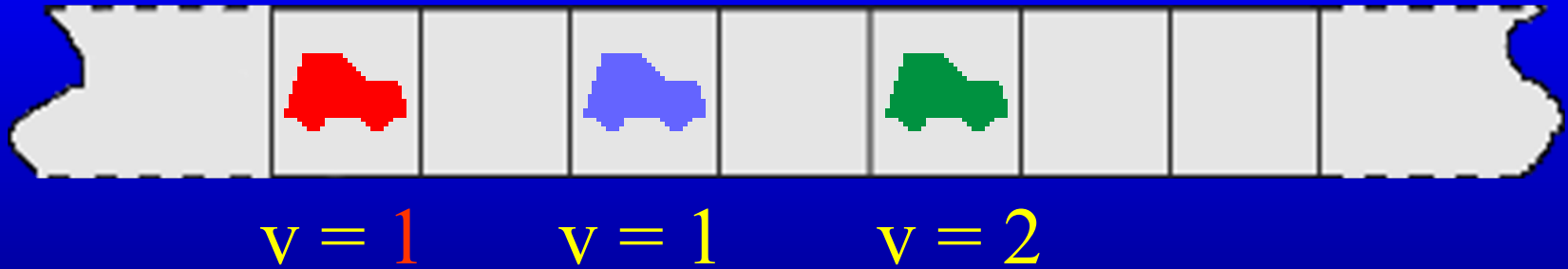


- acceleration:  $v \leftarrow \min(v + 1, v_{\max})$



# Cellular Automaton (II)

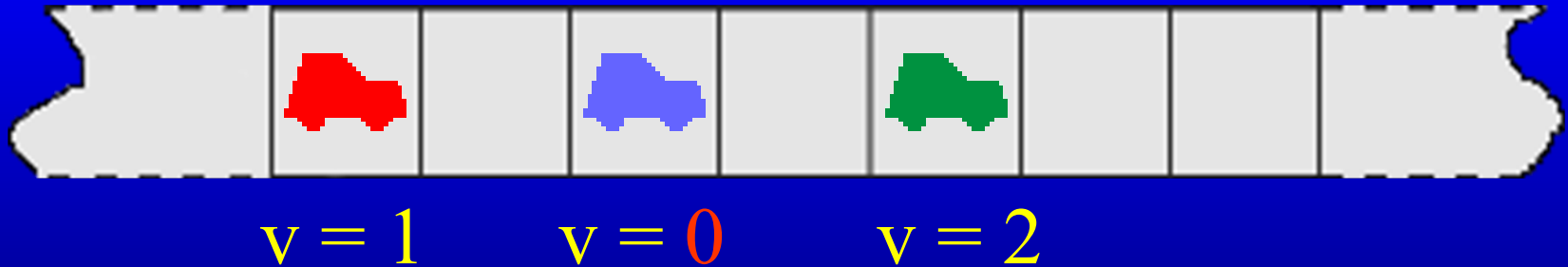
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- acceleration:  $v \leftarrow \min(v + 1, v_{\max})$
- braking:  $v \leftarrow \min(v, \text{gap})$



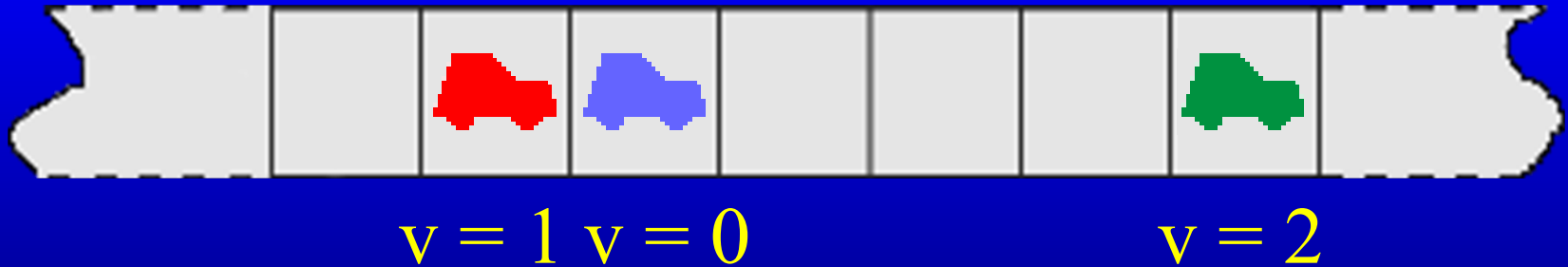
# Cellular Automaton (III)



- acceleration:  $v \leftarrow \min(v + 1, v_{\max})$
- braking:  $v \leftarrow \min(v, \text{gap})$
- randomization with prob  $p_{\text{dec}}$ :  
 $v \leftarrow \max(v - 1, 0)$



# Cellular Automaton (IV)

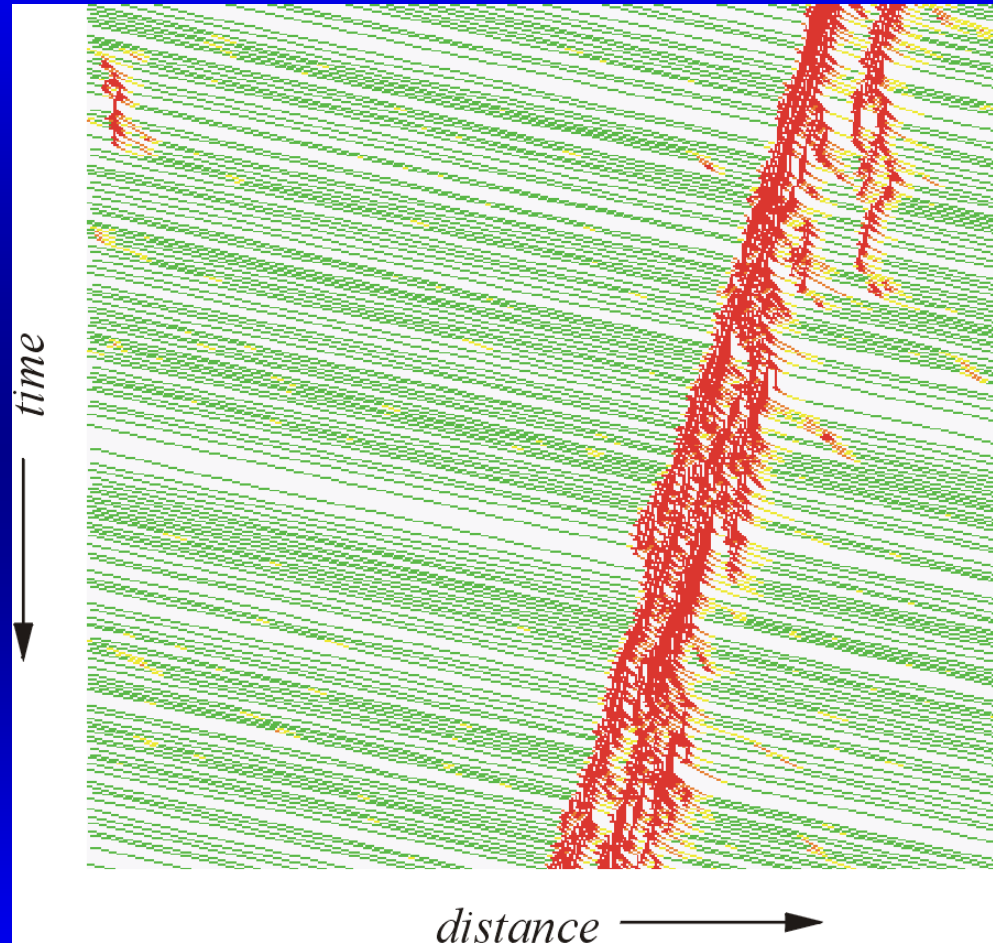


- acceleration:  $v \leftarrow \min(v + 1, v_{\max})$
- braking:  $v \leftarrow \min(v, \text{gap})$
- randomization with prob  $p_{\text{dec}}$ :  
 $v \leftarrow \max(v - 1, 0)$
- driving:  $x \leftarrow x + v$

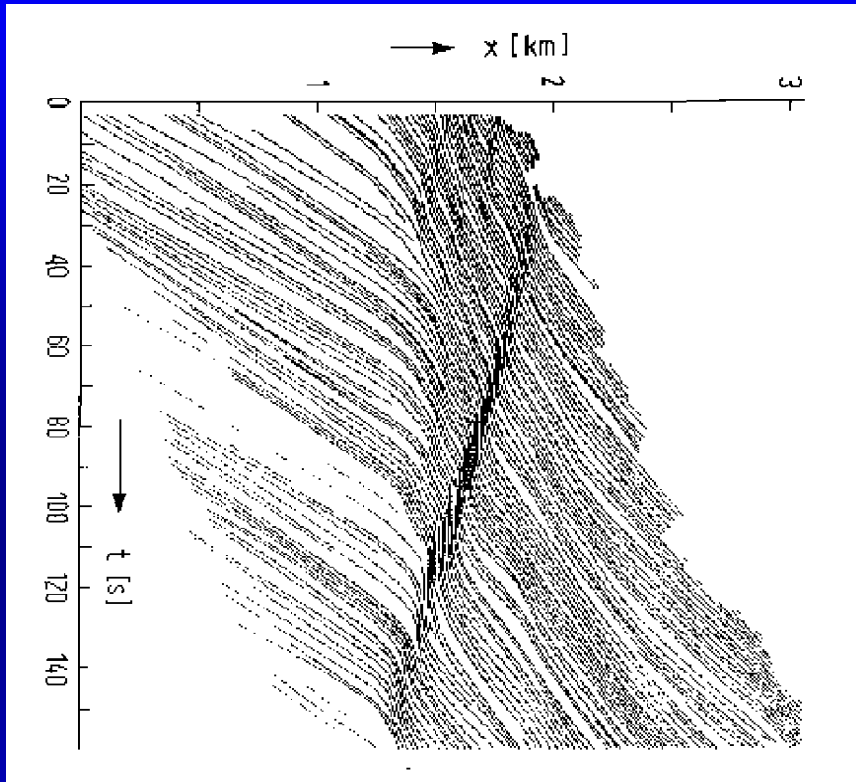


# *Simulated Jams*

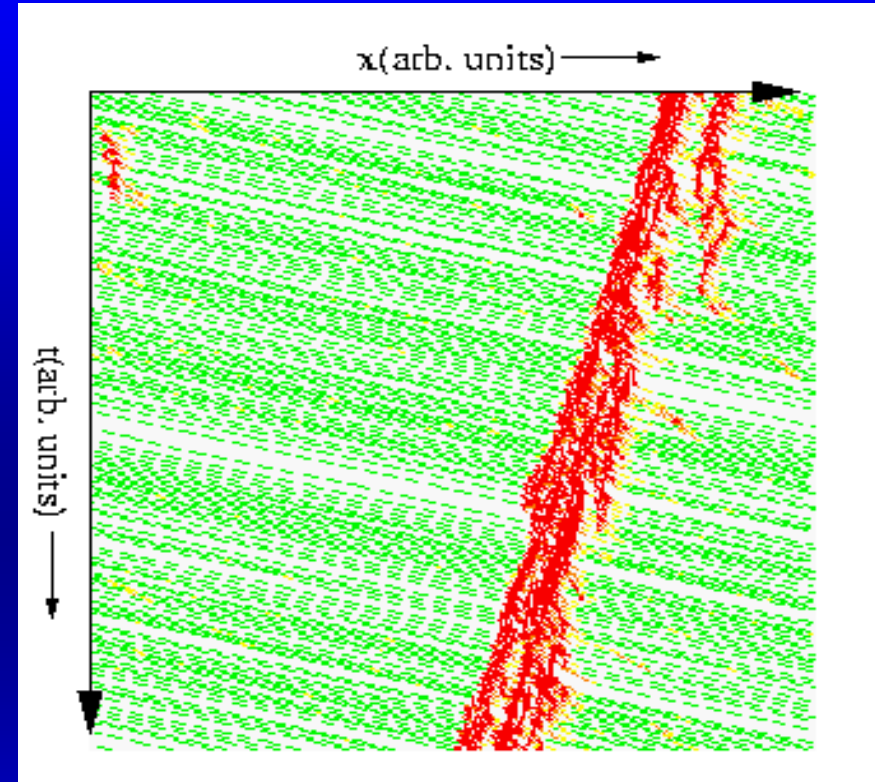
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# Jam Formation



Air video analysis  
(Treiterer 1965)

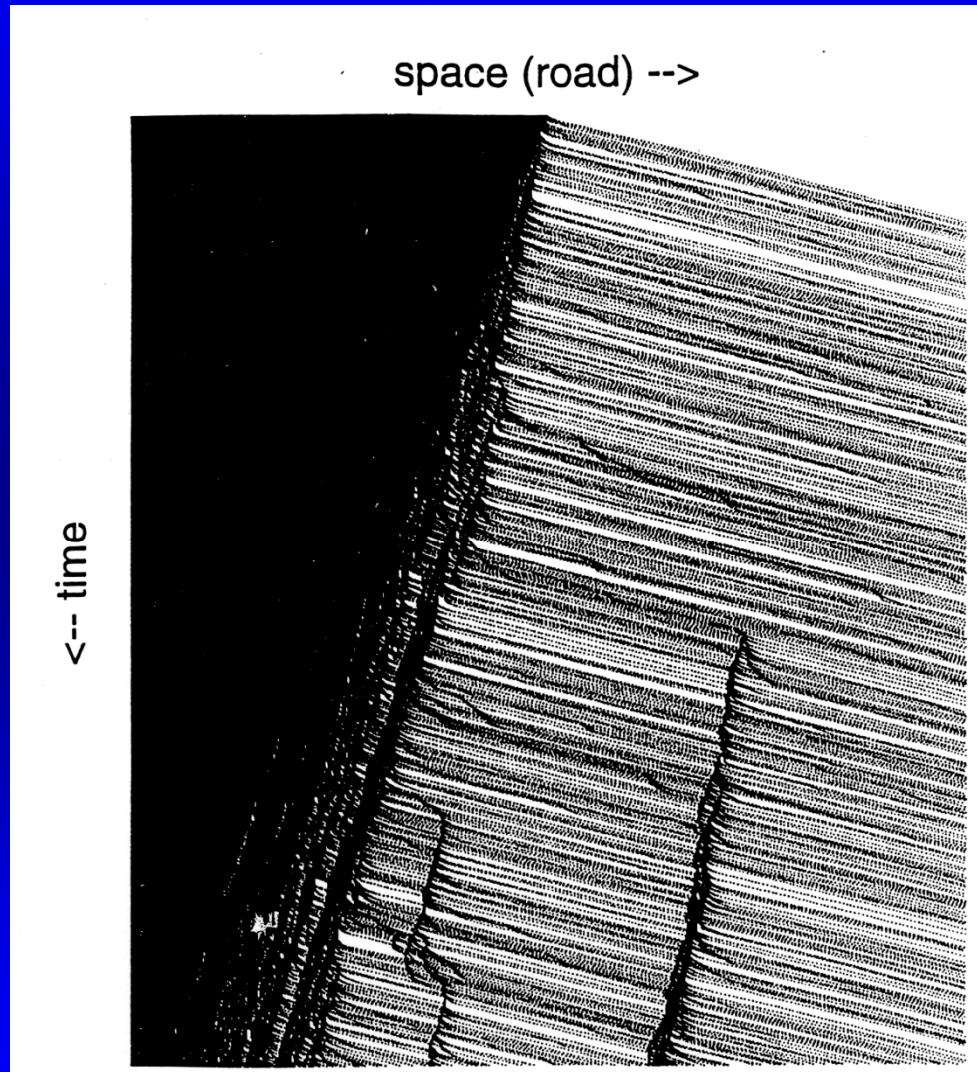


Simulation





# Outflow from a Megajoule SOC

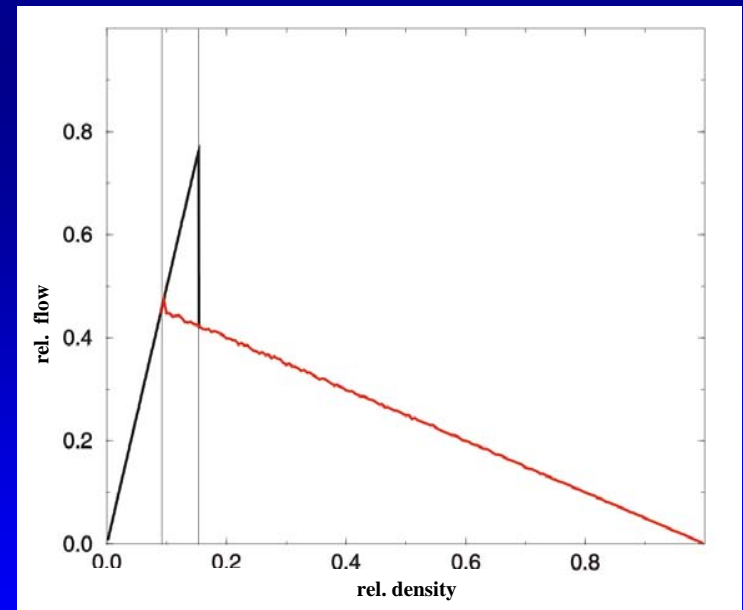
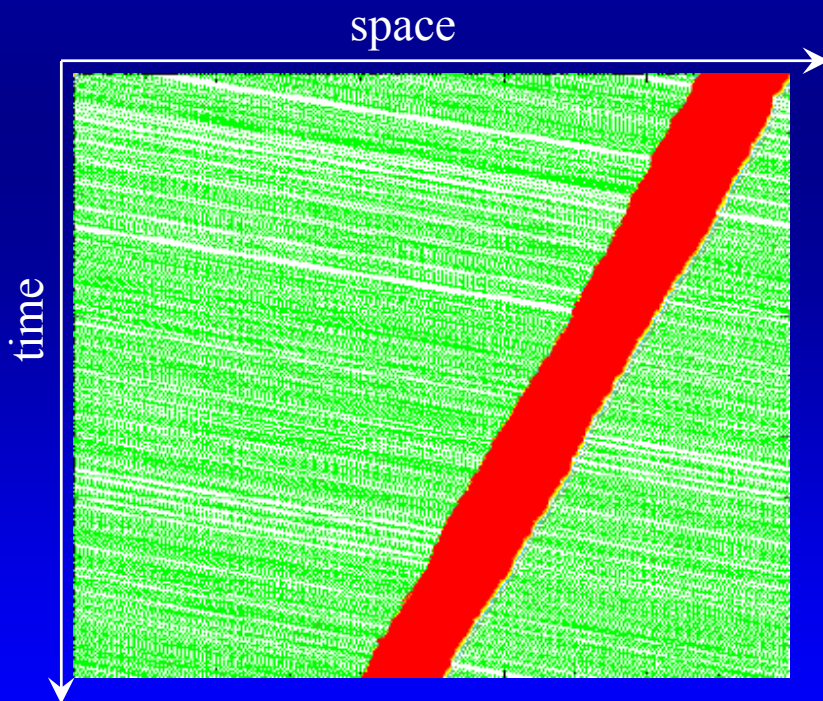


# Velocity Dependent Randomization

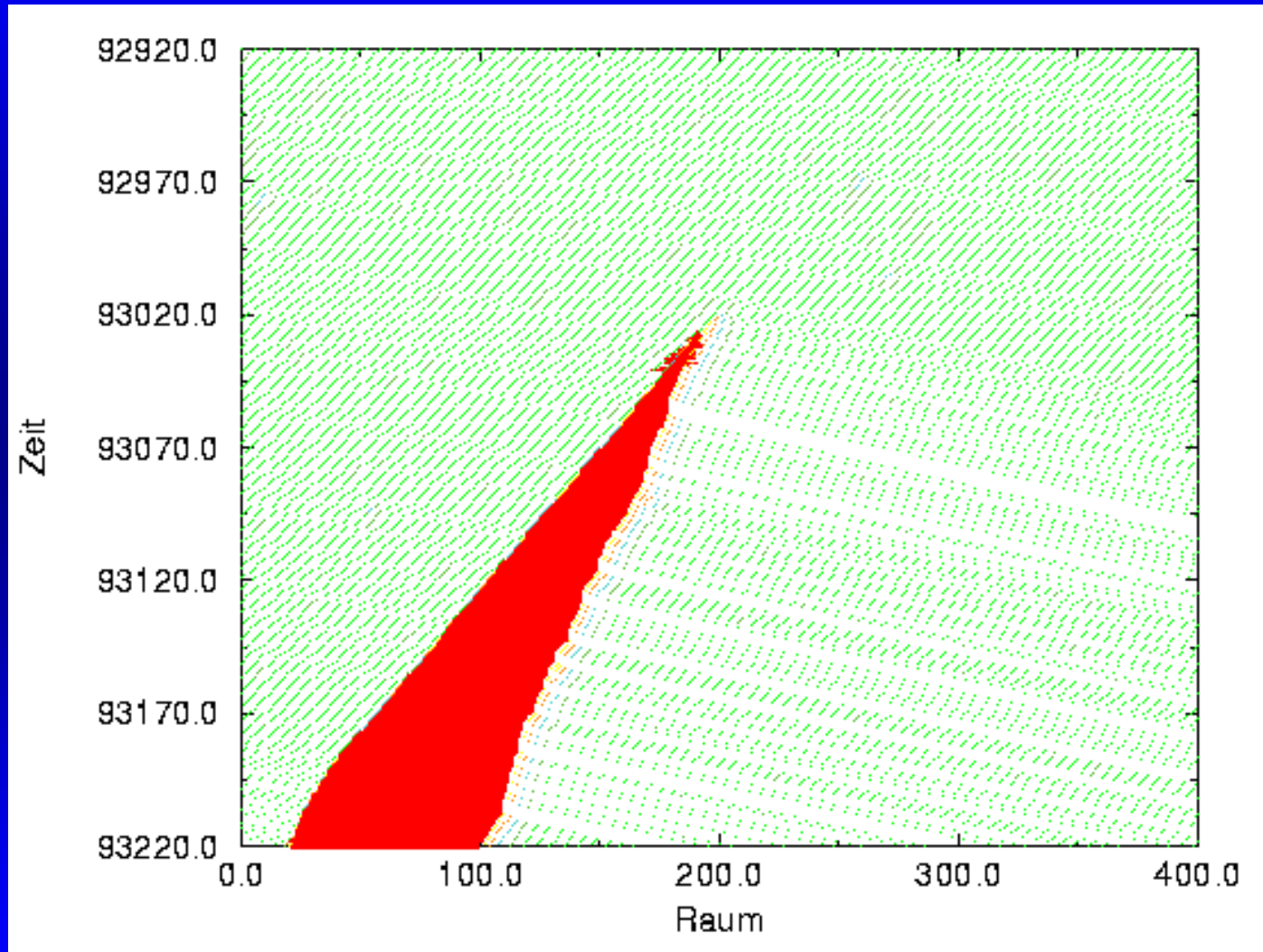
$$p_{\text{dec}} = p_{\text{dec}}(v)$$

$$p_{\text{dec}} = \begin{cases} p_0 & , \text{for } v = 0 \\ p & , \text{else} \end{cases}$$

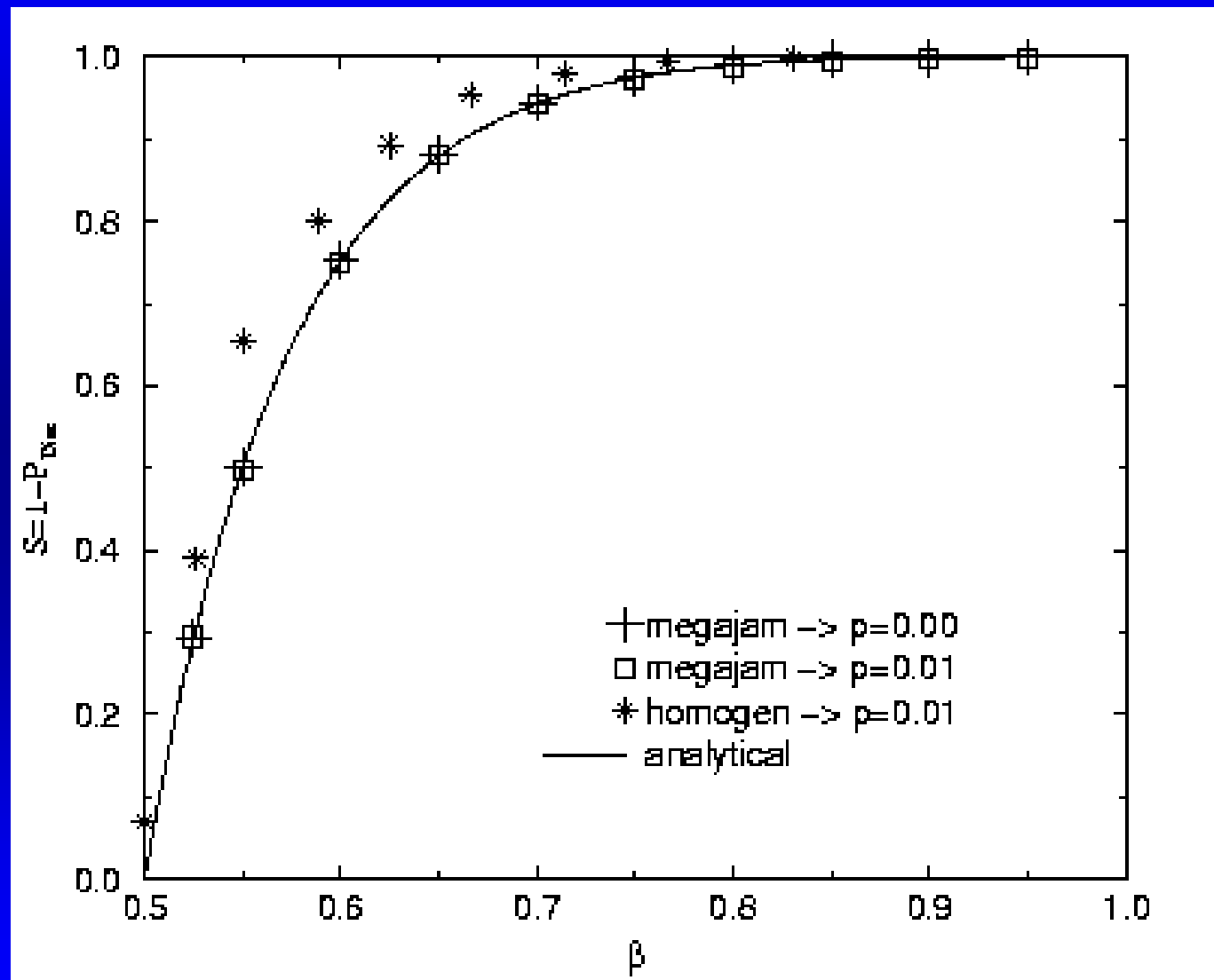
with:  $p_0 > p$



# Metastability



# Jam Probability



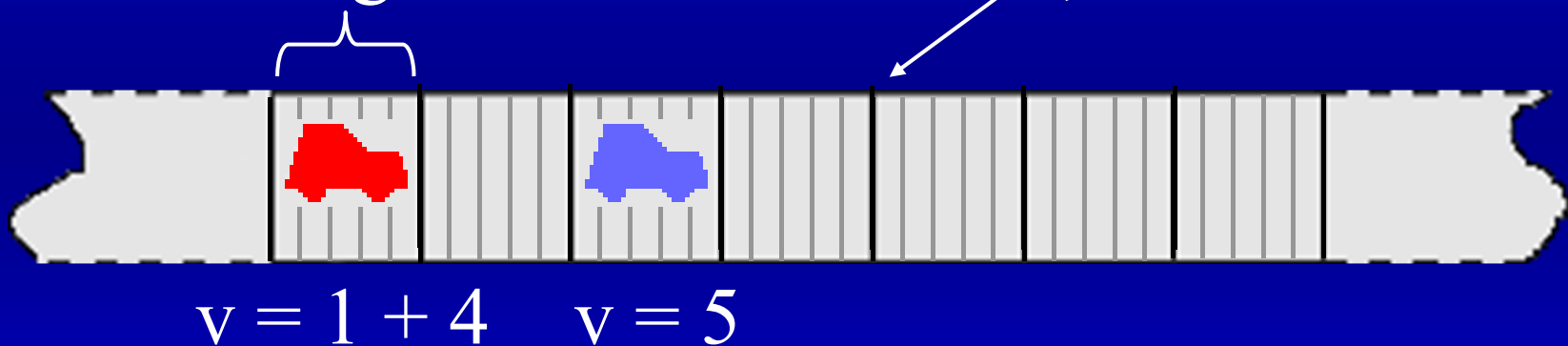
# Anticipation

Anticipation: take into account the speed of the vehicle ahead

Effective distance:  $\text{gap}_{\text{eff}} = \text{gap} + v_{\text{pred}}$

Vehicle length: 5 cells

1,5 m



- small time headways
- ➔
- very high flux
  - realistic lane changes



# *Model Extensions*

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## Requirements:

- Unaffected driving in free traffic
- Reaction on acceleration or braking
- Delayed acceleration out of jams (capacity drop)

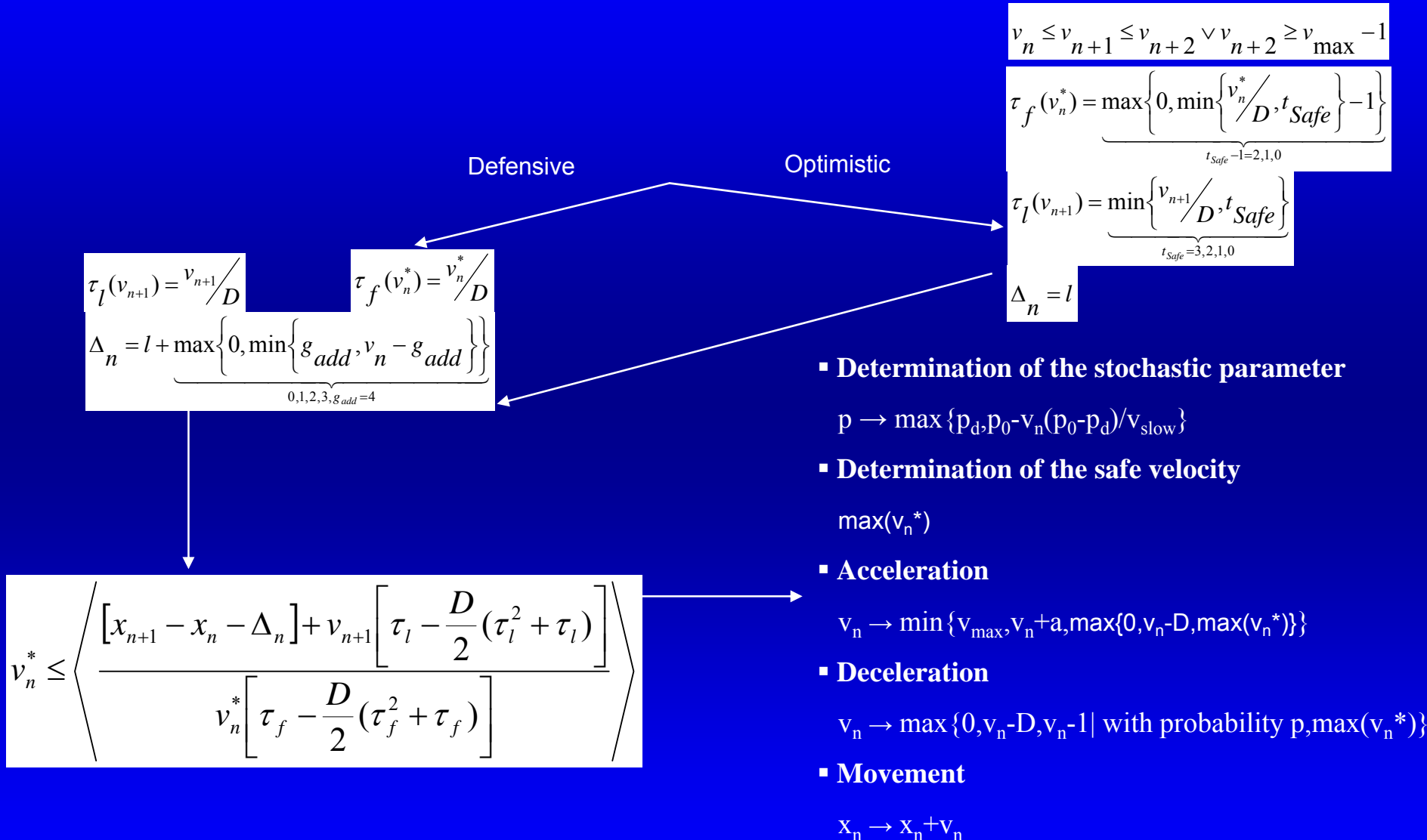
## Ansatz:

- Velocity dependent reaction (VDR)
- Anticipation of driver's behavior
- Adjustment of the cell length



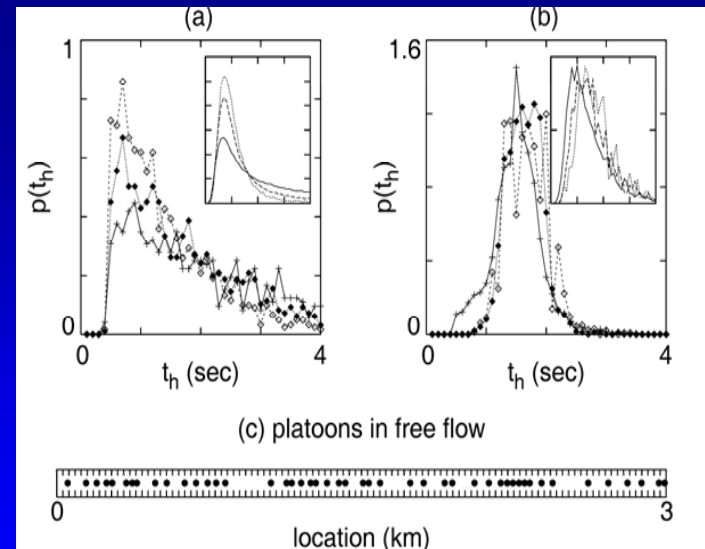
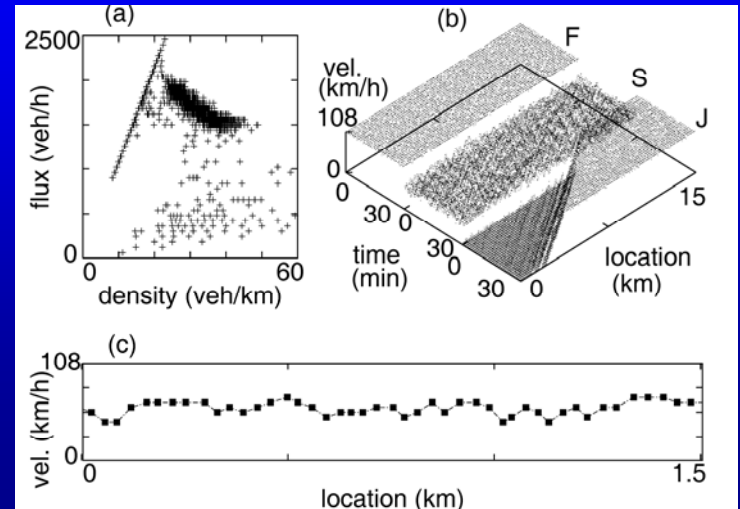
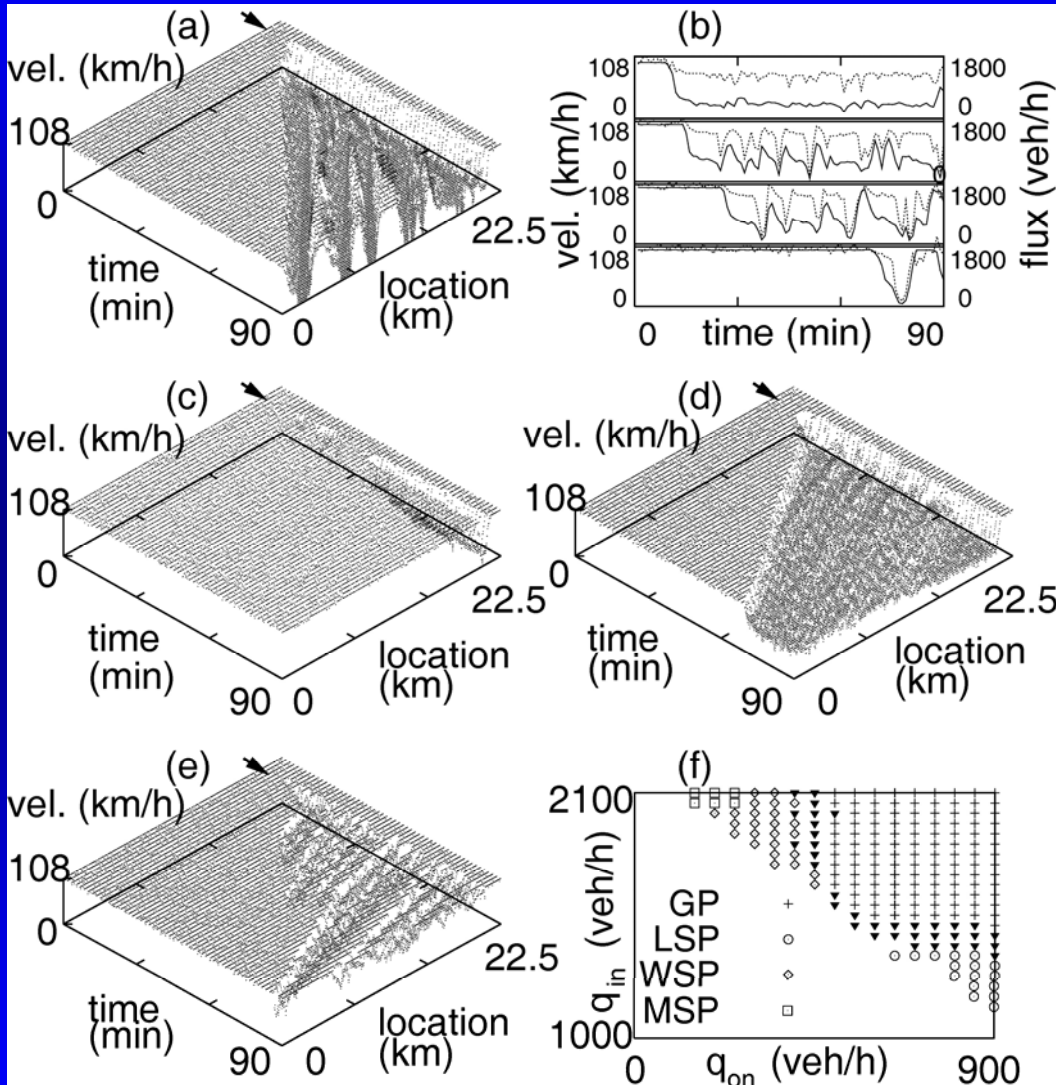


# Driver-Behaviour-Modell (Lee et al)

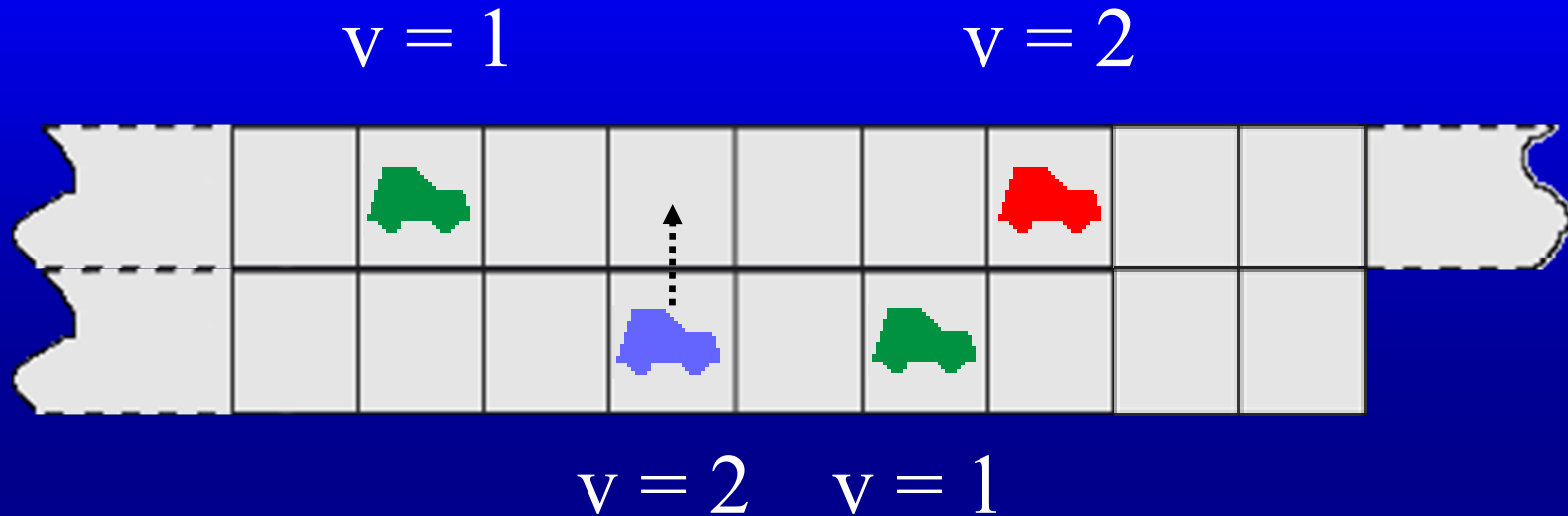




# Traffic Phases



# Lane Changing



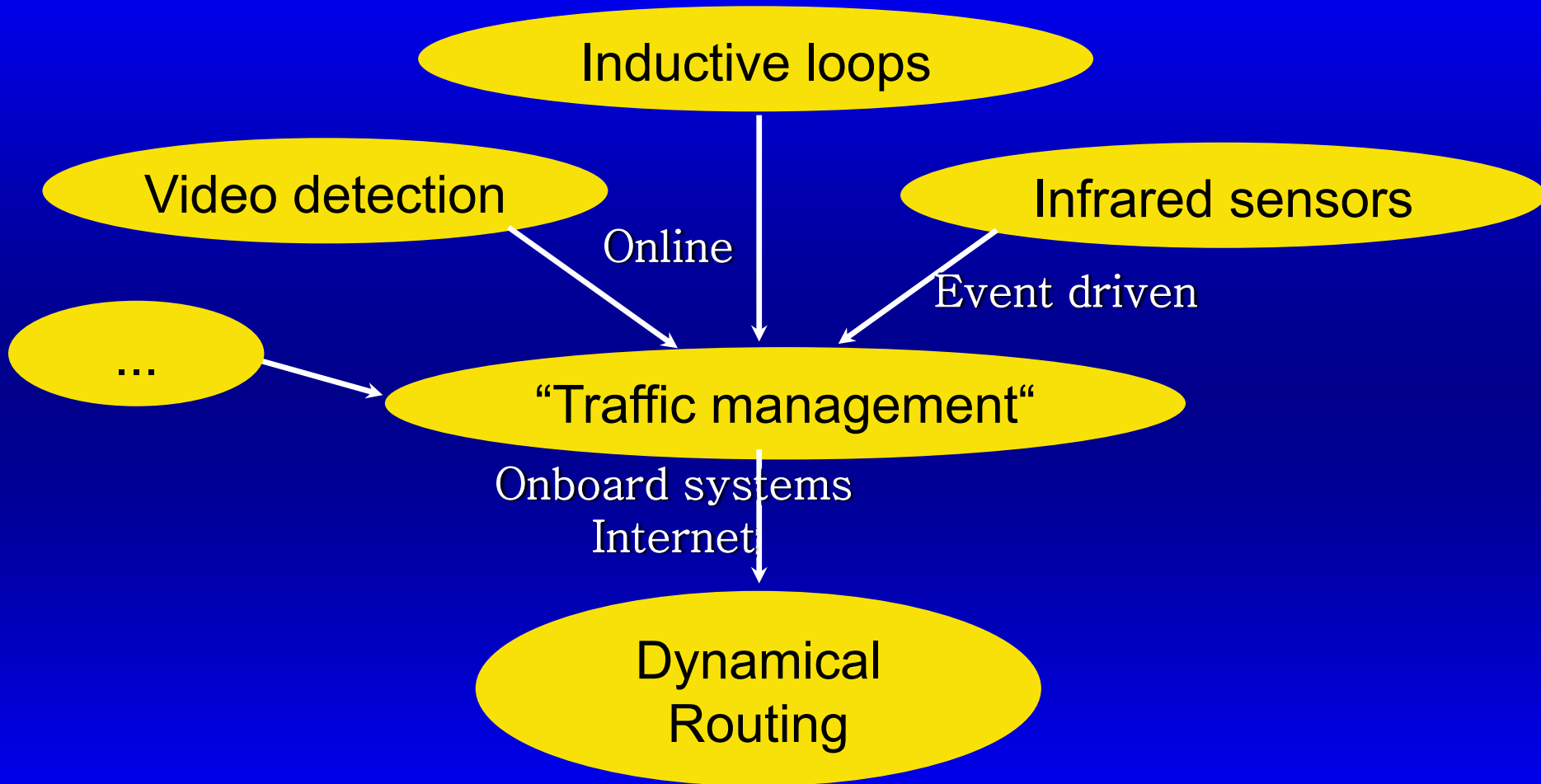
Lane change if

1. the driver wishes it,
2. it is allowed
3. headways remain 'safe' .



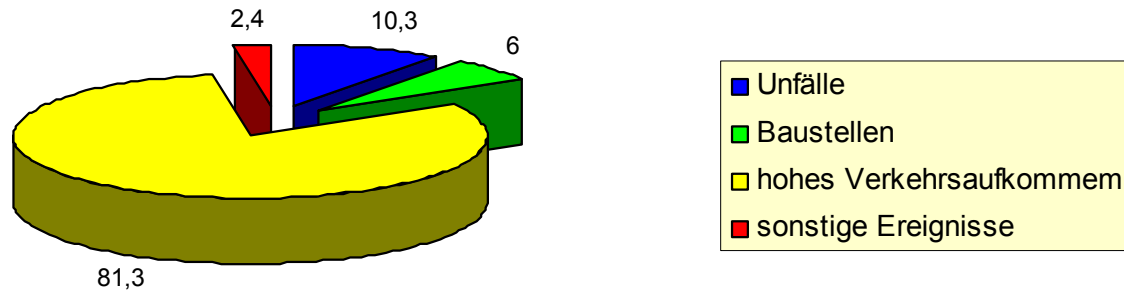
# *Informations in Transport Systems*

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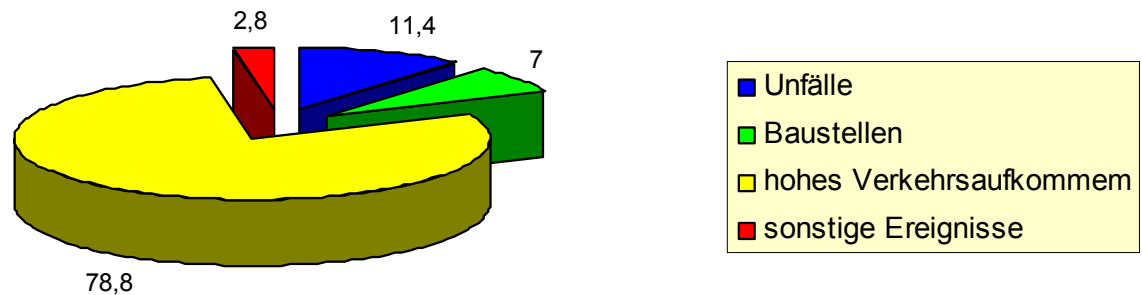


# Jam Statistics

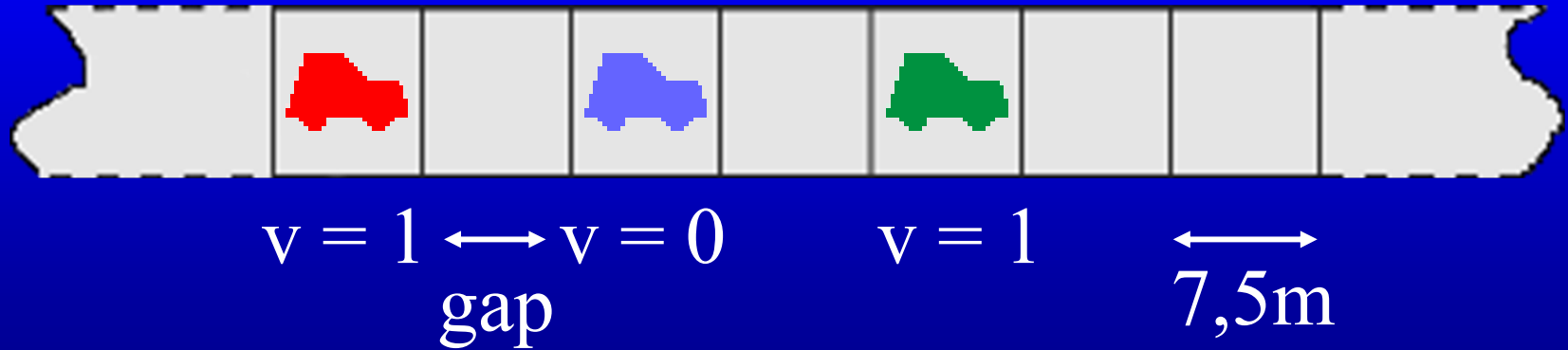
## Störungen 2001



## Störungen 2002



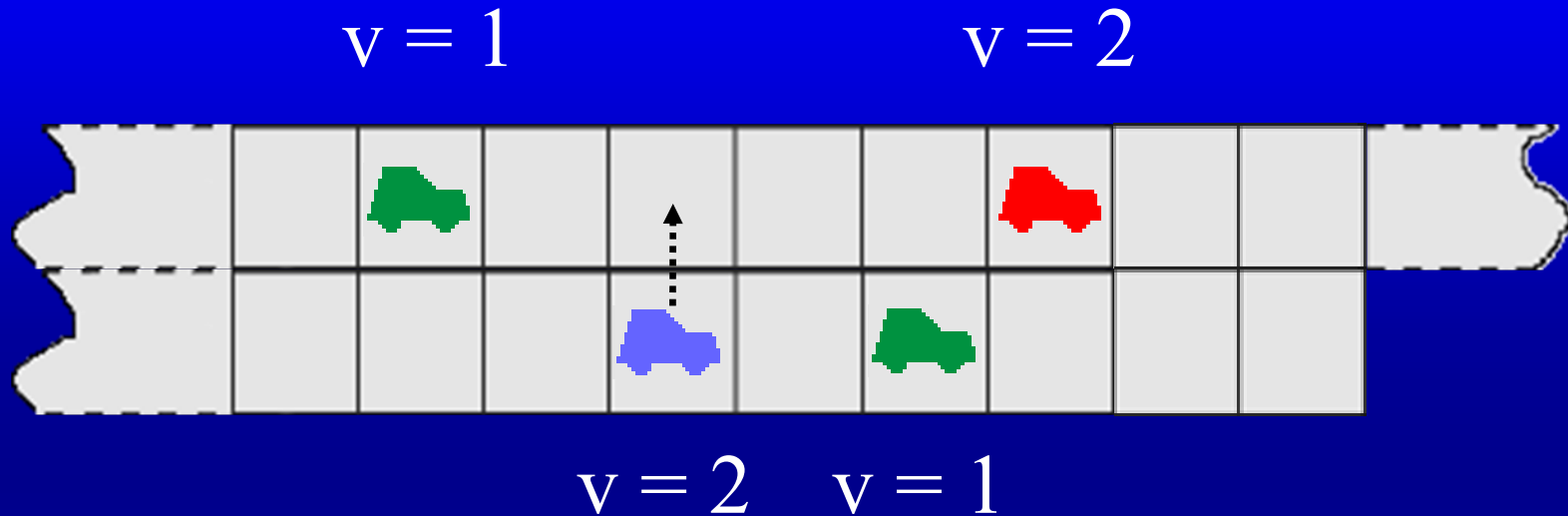
# Efficient discrete Simulation Modell



- Cell length = 7,5 m
- $v =$  speed
- gap = number of empty cells between the cars



# Lane Changing



Lane changing if

1. it is desired,
2. it is legal and
3. Safety distance is obeyed.



# Lane-Changing Rules

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$$t_h = \text{gap}/v$$

$$t_s = \min(v, 6)$$

$$\text{gap}_{\text{eff}} = \text{gap} + \max(v_{\text{anti}} - 7, 0)$$

$$v_{\text{anti}} = \min(\text{gap}_{\text{pred}}, v_{\text{pred}})$$

1.  $b_n = 0$  und  $b_{n+1} = 1$  und  $t_h < t_s$
2.  $\text{gap}_{\text{eff}} \geq v$
3.  $\text{gap}_{\text{back}} \geq v_{\text{back}}$





# *Traffic Informations / Navigation*

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- ❑ Static navigation / maps
- ❑ Dynamic navigation (RDS-TMC/Private)
- ❑ Pre-trip: Internet / TV
- ❑ On-trip: radio / mobile phone / Internet / digital TV / information panels
- ❑ Post-trip: Internet



## Verkehrslage in NRW

Hochrechnung für Bundesautobahnen

Verkehrsinfo.NRW



- ▶ Erläuterungen
- ▶ Technische FAQ
- ▶ Impressum
- ▶ english version

## Verkehrsinformationssystem autobahn.NRW

Mit den folgenden Links können Sie direkt auf die entsprechende Karte gelangen:



aktuelle Verkehrslage



Prognose 30 min



Prognose 60 min

NRW Übersicht  
Aachen  
Köln  
Ruhrgebiet  
Ruhrgebiet West  
Ruhrgebiet Ost  
Ostwestfalen  
Münsterland  
Sauerland  
Bonn  
Niederrhein

NRW Übersicht  
Aachen  
Köln  
Ruhrgebiet  
Ruhrgebiet West  
Ruhrgebiet Ost  
Ostwestfalen  
Münsterland  
Sauerland  
Bonn  
Niederrhein

NRW Übersicht  
Aachen  
Köln  
Ruhrgebiet  
Ruhrgebiet West  
Ruhrgebiet Ost  
Ostwestfalen  
Münsterland  
Sauerland  
Bonn  
Niederrhein



Ministerium für  
Verkehr,  
Energie und  
Landesplanung  
des Landes  
Nordrhein-Westfalen

**Straßen.NRW.**  
Landesbetrieb Straßenbau NRW



Physik  
von Transport  
und Verkehr



Dieses Projekt wurde von  
der europäischen Union  
finanziell unterstützt



autobahn.NRW

Expansion for motorway network

Friday, 09.07.2004, 15:49 h



Current Traffic State Forecast 30 min Forecast 60 min

- colour-blind mode
- ⊙ Info on Roadworks

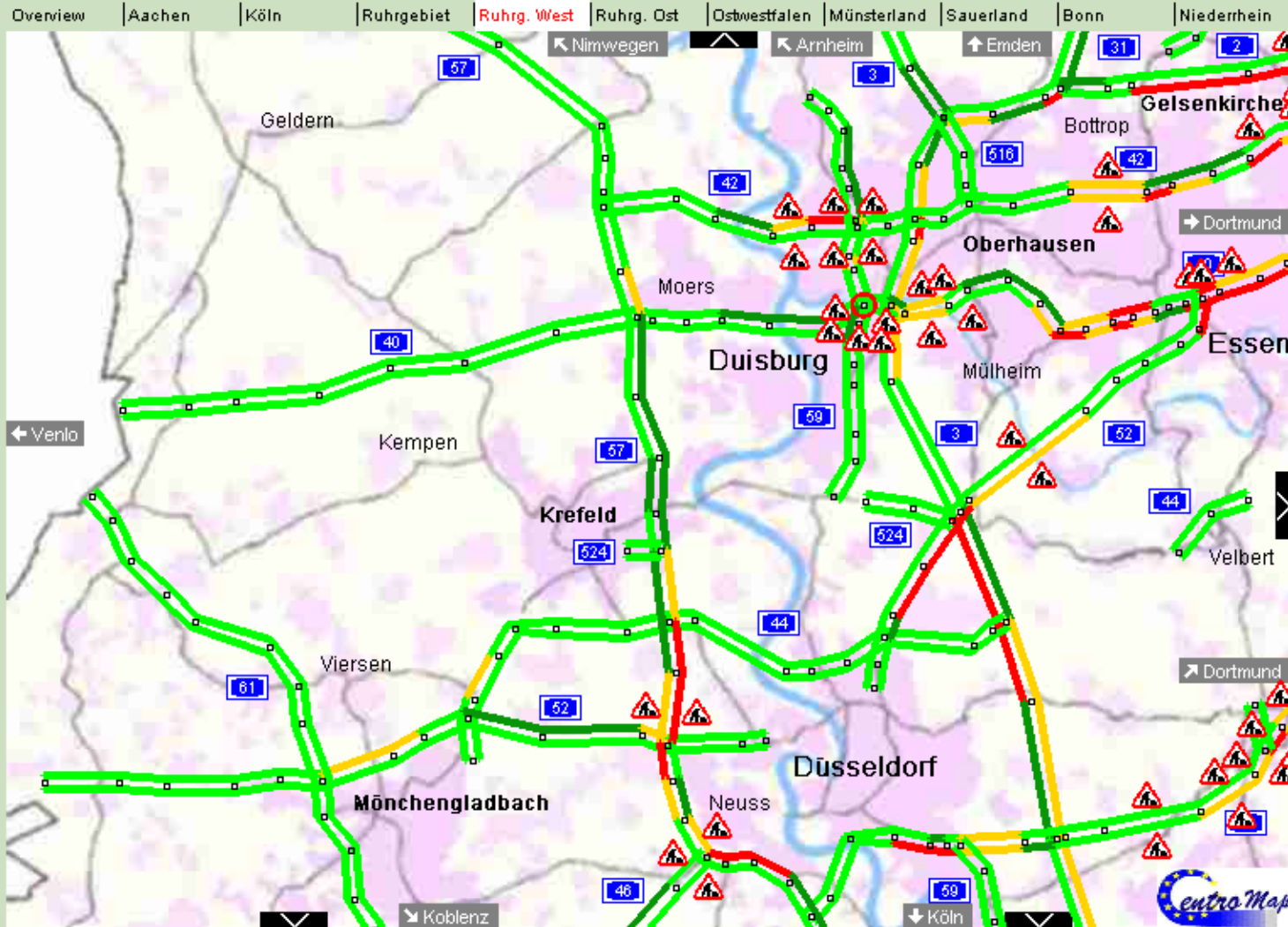
Traffic State

- free
- dense
- viscous
- congested

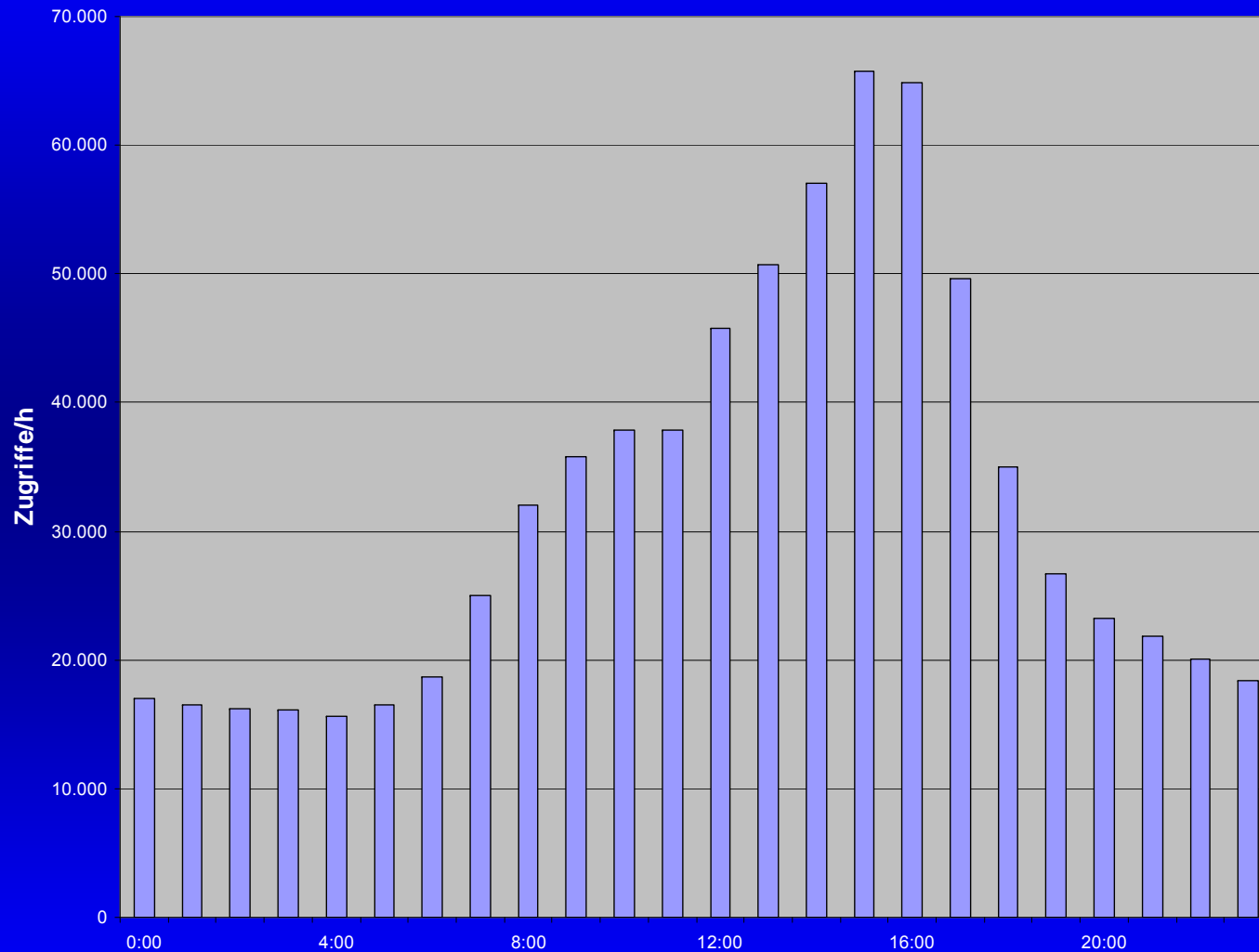
- roadworks with low jam risk
- roadworks with high jam risk
- junction
- closure
- (part-) closure of the junction

- Explanation
- Imprint
- deutsche Version

Version 2.5

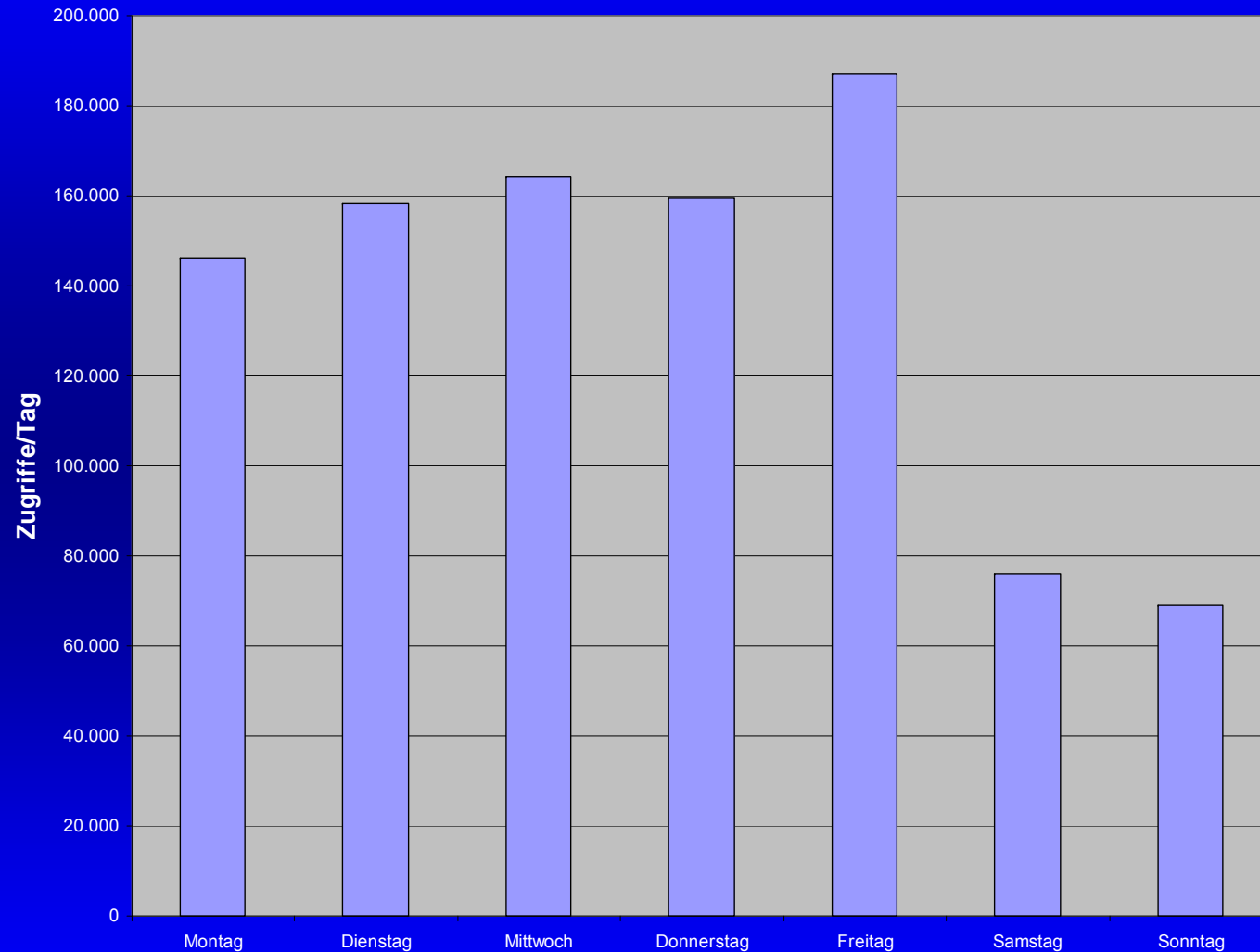


# *Users per Hour*

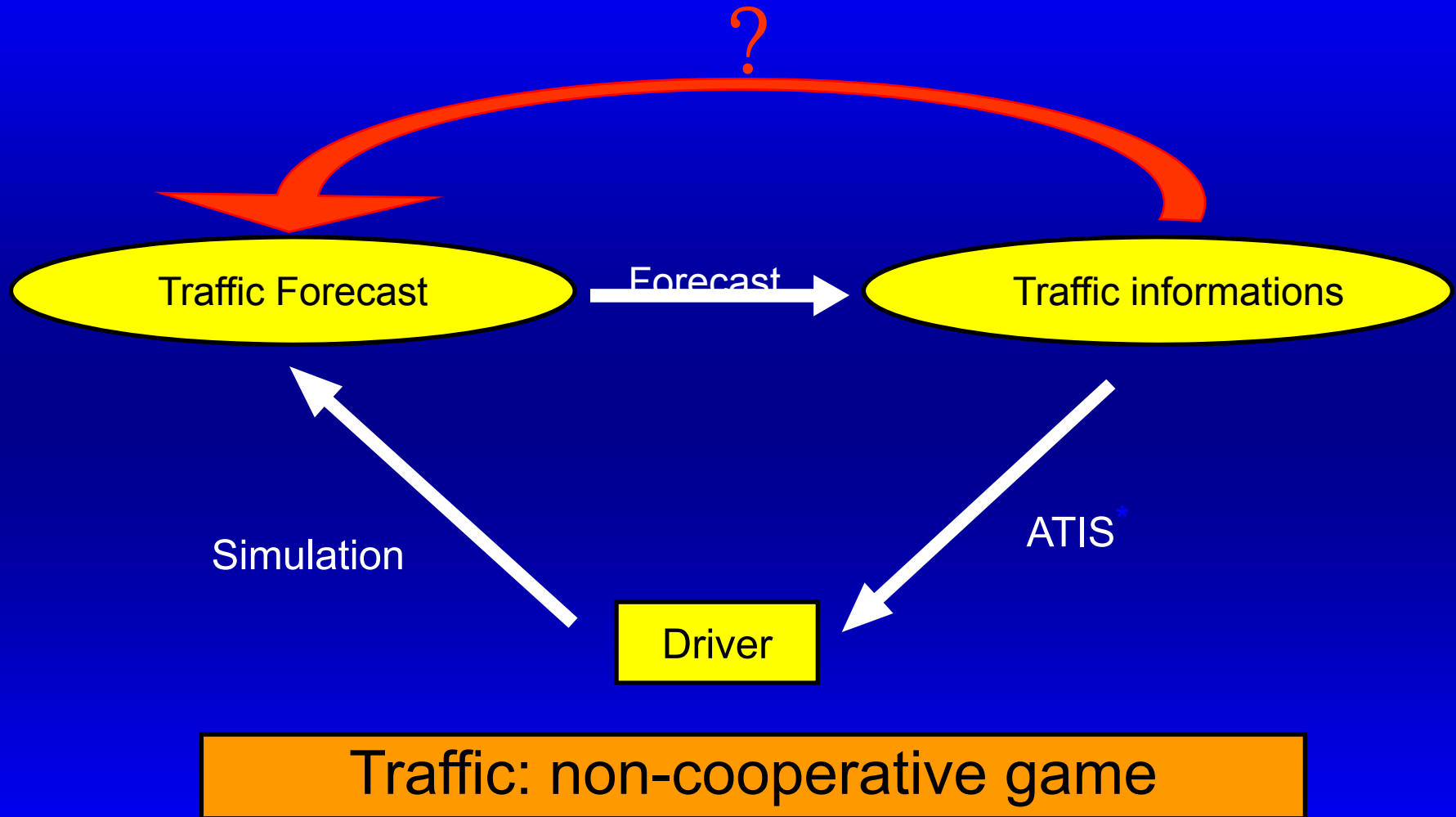


# *Users per Week-Day*

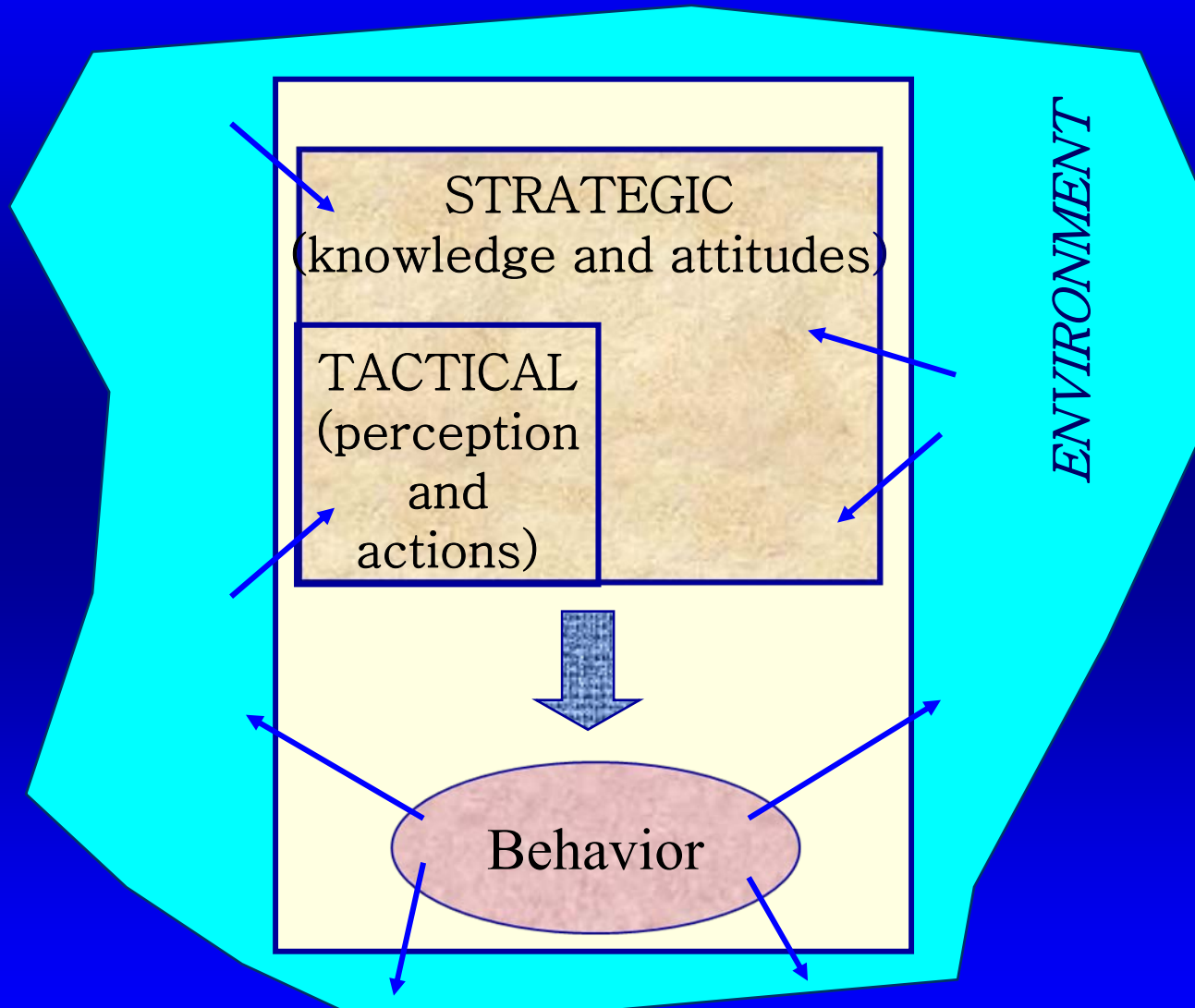
---



# *Anticipatory Traffic Forecast*

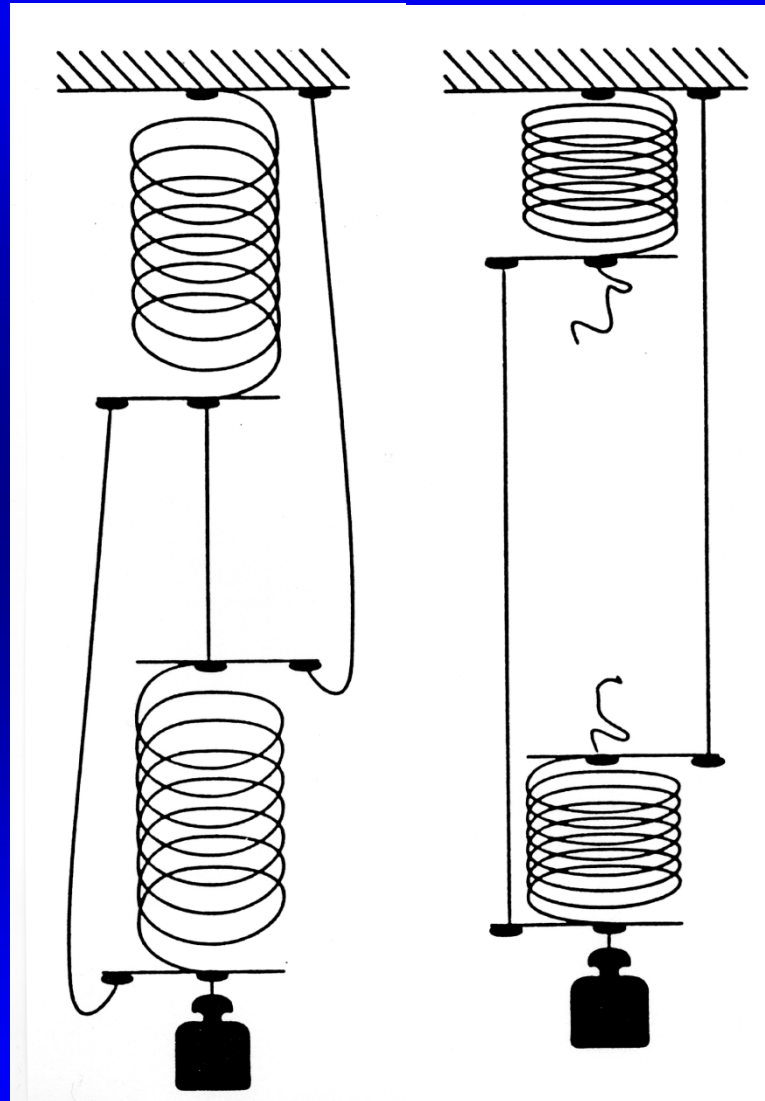


# Multi-Agent Model

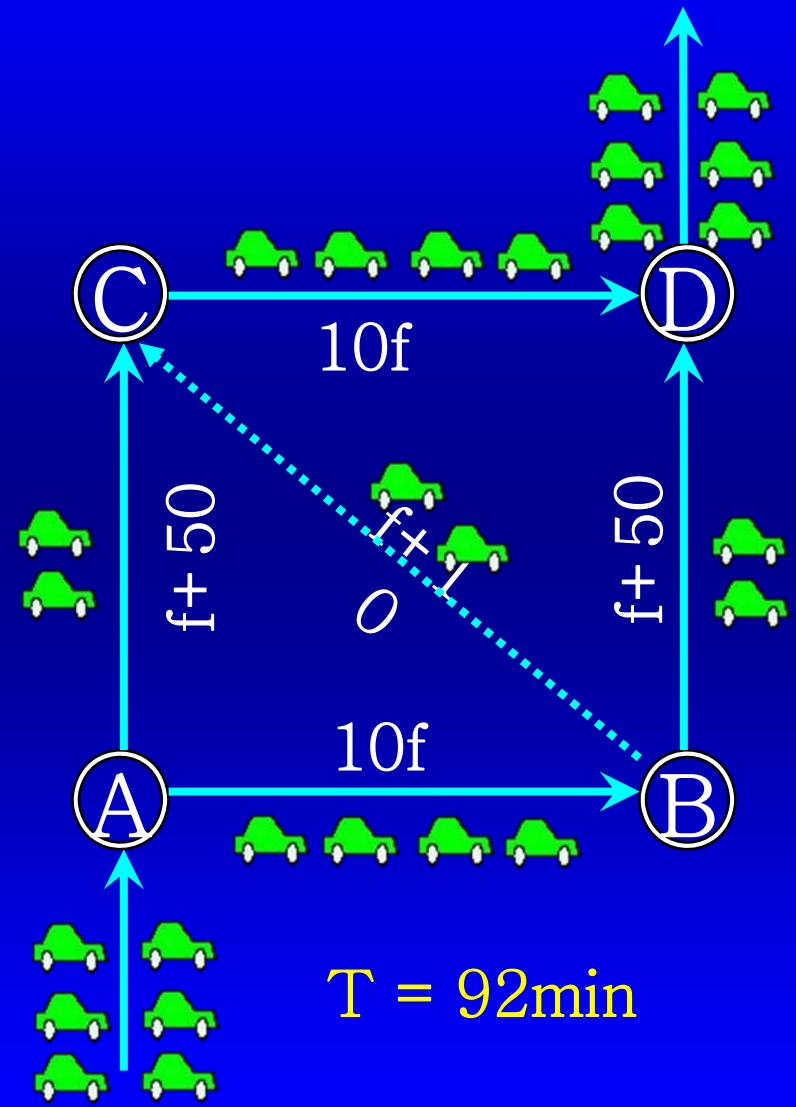
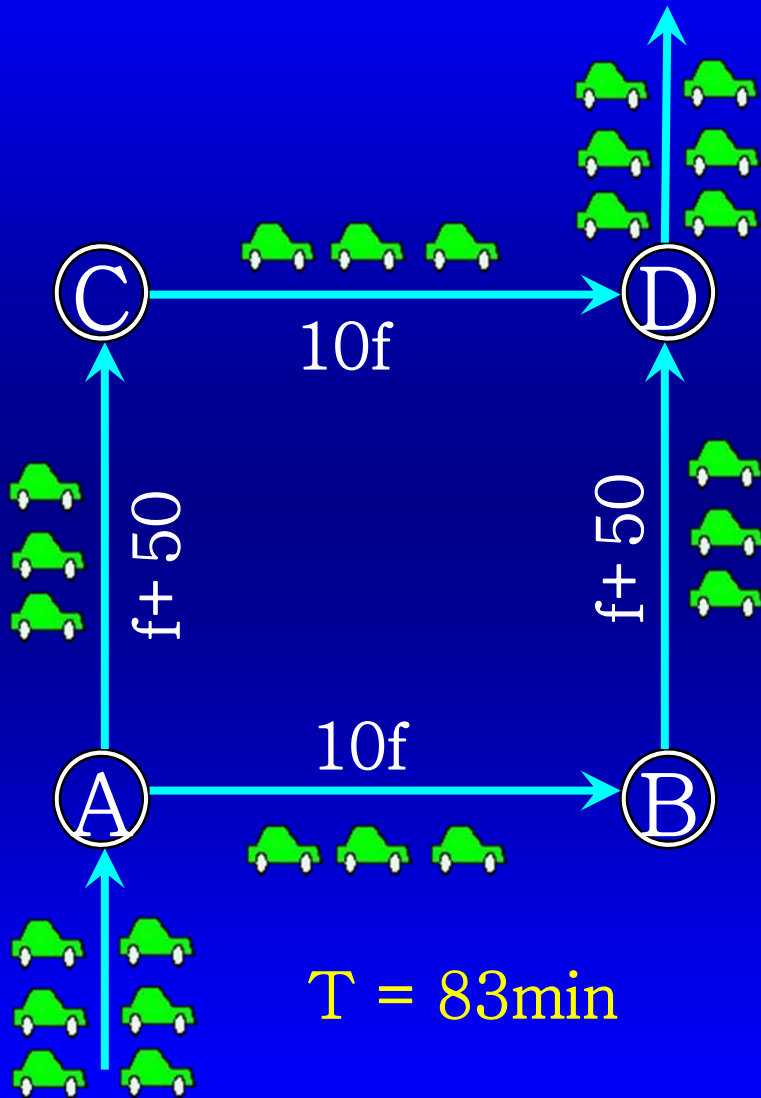




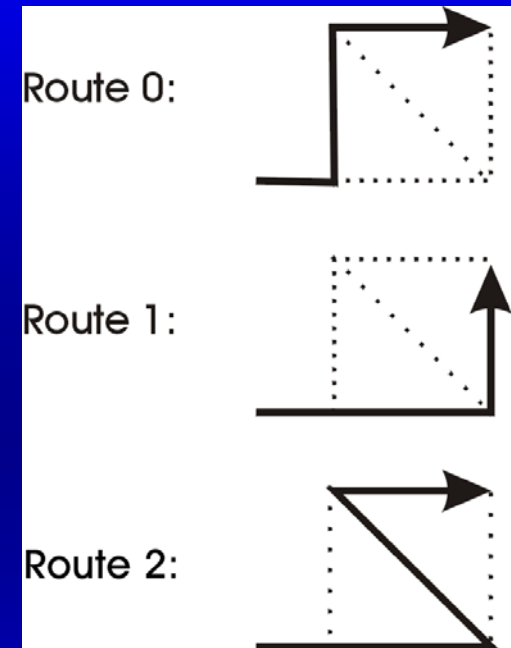
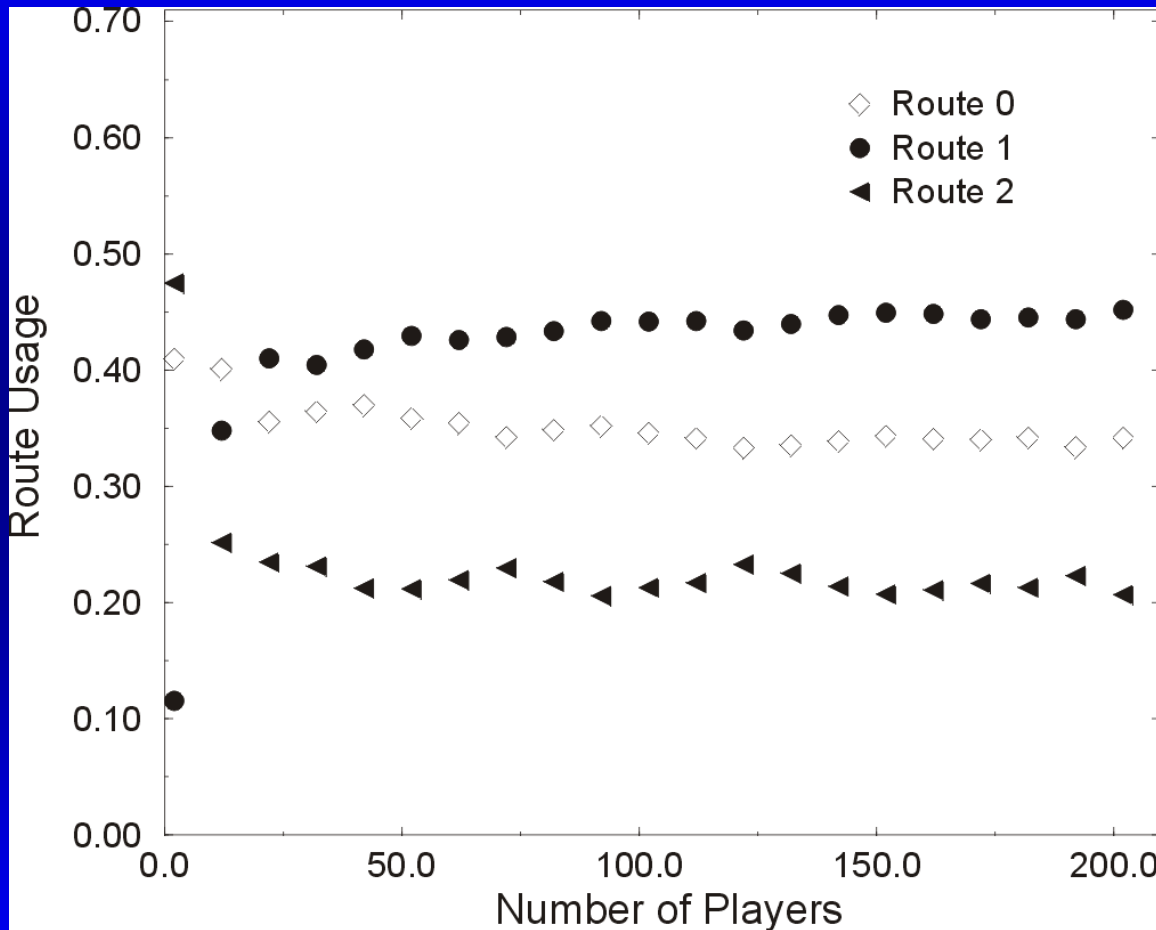
# *The Braess Paradox*



# The Braess Paradox



# Route Choice

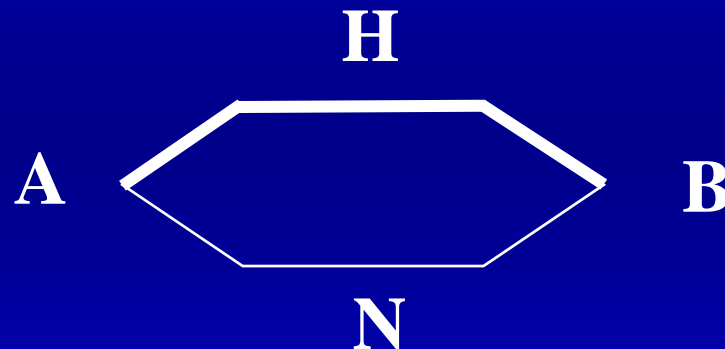


# *Day-to-Day Route Choice-Behaviour*

## *Experimental design*

Trip from **A** to **B**

Two routs **H** and **N** (**H** main, **N** side route)



Each of the 18 participants chooses in every round the main route **H** or the side route **N**.

Play it for 200 rounds.



# Day-to-Day Route Choice-Behaviour

$n_H$ : number of participants choosing H

$n_N$ : number of participants choosing N

## Travel times

For H

$$T_H = 6 + 2n_H$$

For N

$$T_N = 12 + 3n_N$$

## Payment per round: $P = 40 - T$

$$T = T_H$$

For driver on H

$$T = T_N$$

For driver on N

**Starting capital: 200**

**Payment** = starting capital + sum of round payments

Change to real money



# *Day-to-Day Route Choice-Behaviour*

---

## *Informations of the players*

6 rounds each

The diagram consists of a central oval containing the text '6 rounds each'. Two large, white, L-shaped arrows originate from the right side of this oval. The top arrow points to the top information box, and the bottom arrow points to the bottom information box.

### **Informations: experiment I**

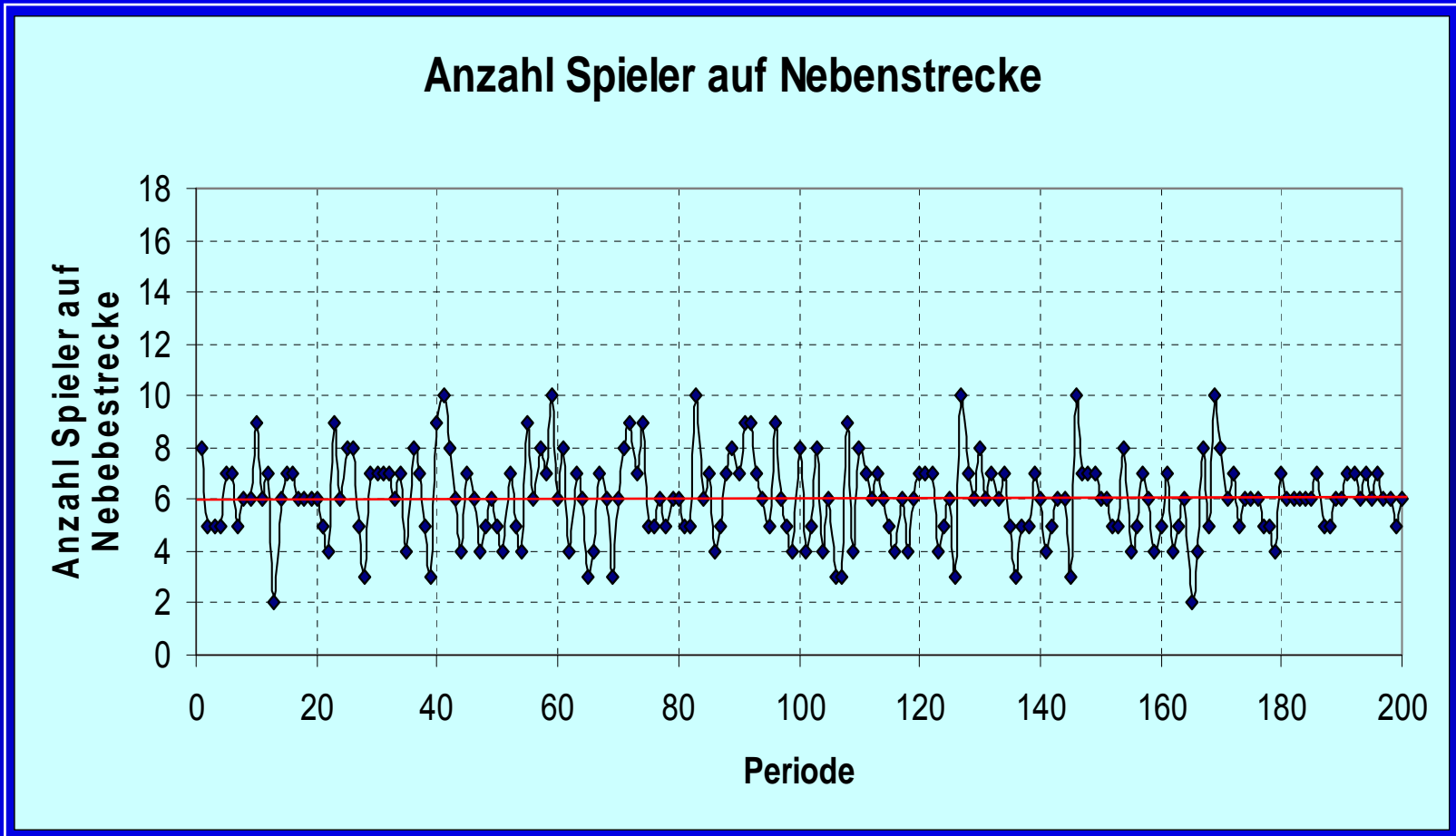
Travel time in the last round for the chosen route.  
Payment for the last round.  
Total payment before the last round.  
Running number of the last round.

### **Informations: experiment II (additional)**

Travel time on the alternative route, which was not chosen in the last round.

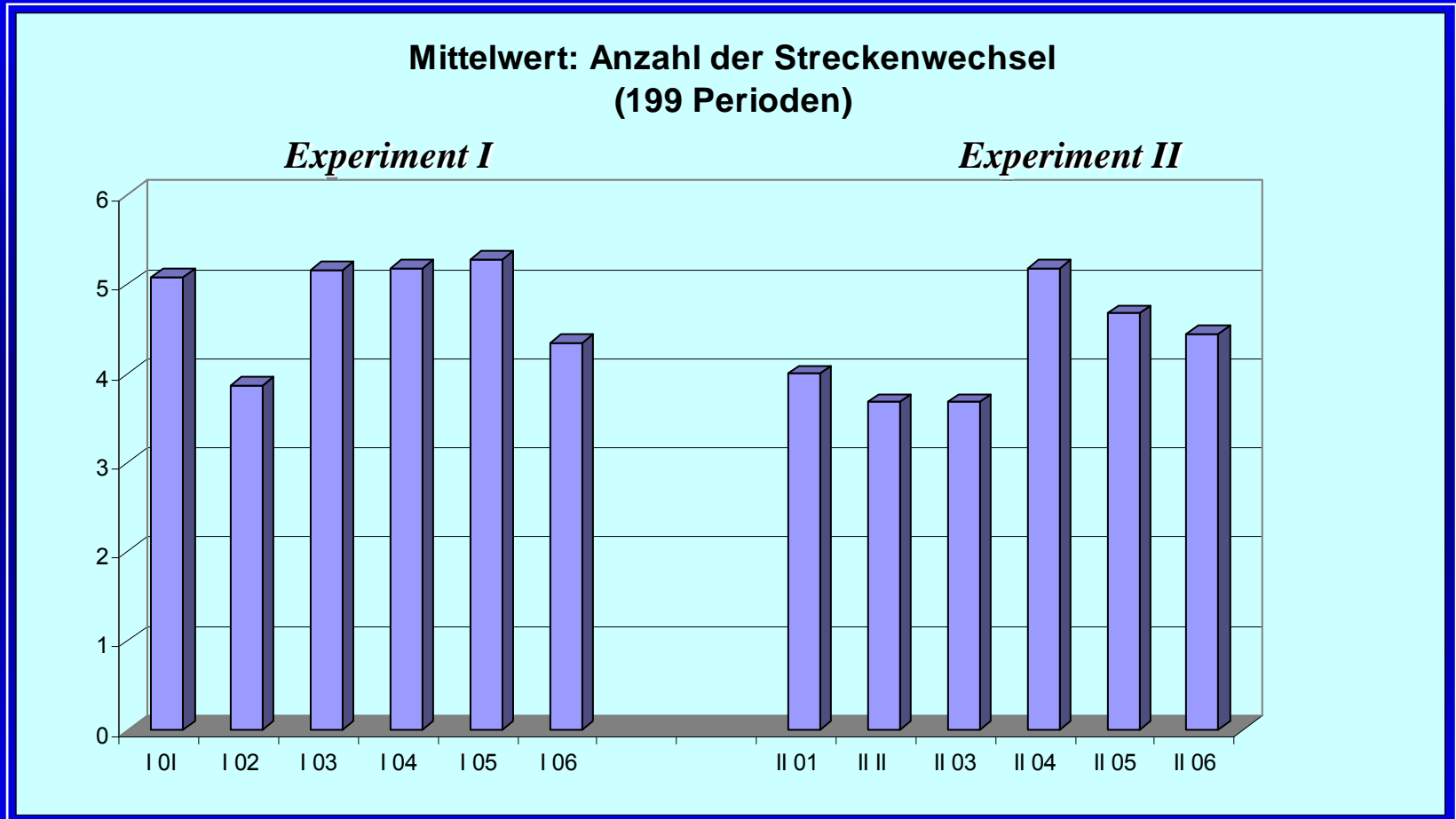


# Day-to-Day Route Choice-Behaviour

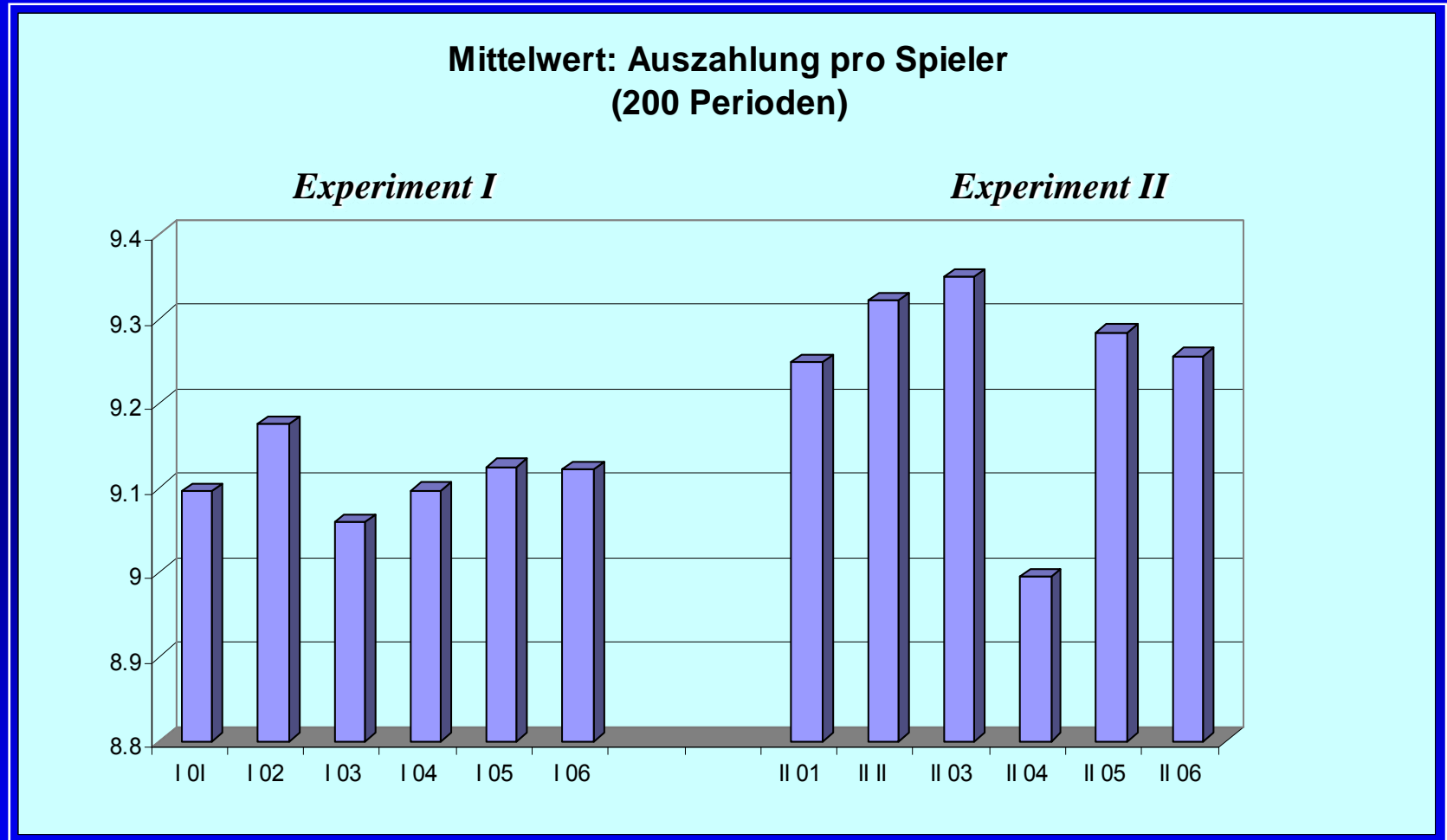




# Day-to-Day Route Choice-Behaviour



# Day-to-Day Route Choice-Behaviour



# *Payoff Sum Model*

---

Bush & Mosteller (1955), Harley (1981), Roth & Erev (1995)

## Idea („Law of effect“):

Play with  $n$  participants and  $k$  pure strategies each.

Tendency at time  $t$ :  $q_{nk}(t)$

If player  $n$  chooses strategy  $k$  at time  $t$ , he wins  $x_{nk}(t)$  (units)

New tendency:  $q_{nk}(t+1) = q_{nk}(t) + x_{nk}(t)$

Probability to choose strategy  $k$  in the next round:

$$p_{nk}(t+1) = q_{nk}(t+1) / \sum_l [q_{nl}(t+1)]$$

$q_{nk}$  is monotonously increasing with  $t$  and not bounded.

> as time goes on the learning effect becomes smaller (**“flatter learning curves“**)



# Day-to-Day Route Choice-Behaviour

## Extended payoff sum model

### Strategy vector

1	main road
2	side road
3	direct
4	contrarian

### Simulations

Initial values ( $x_1, x_2, x_3, x_4$ )

$$x_1 = 1, \dots, 10$$

$$x_2 = 1, \dots, 10$$

$$x_3 = 0, \dots, 10$$

$$x_4 = 0, \dots, 10$$

1000 runs of 200 periods for each vector of initial values

[4,3,3,2] is the only vector of initial values with the property that the simulated means of the variables listed below are in the experimentally observed range.

	min Ex I & II	Simulations	max Ex I & II
mean(#(players[S]))	5.85	5.88	6.17
std_dev(#(players[S]))	1.53	1.65	1.94
mean(#(road_ch))	3.67	5.17	5.28
mean(#(last_road_ch))	154.78	183.73	190.39
mean(yule)	0.12	0.14	0.37
std_dev(yule)	0.52	0.60	0.74



# Day-to-Day Route Choice-Behaviour

## Extended payoff sum model

### Variables

$A_i$	payoff sum for strategy $i$ in period $t$
$A = A_1 + \dots + A_n$	total payoff sum
$a$	payoff for period $t$
$A_i^+$	next period's payoff sum for strategy $i$
$p_i$	probability of choosing $i$

### Adjustment of payoff sum

$x_i > 0$  initial value for  $A_i$  in period 0

For  $a \geq 0$  : 
$$A_i^+ = \begin{cases} A_i + a & \text{if } i \text{ was chosen} \\ A_i & \text{else} \end{cases}$$

For  $a < 0$  : 
$$A_i^+ = \begin{cases} A_i & \text{if } i \text{ was chosen} \\ A_i + |a| & \text{else} \end{cases}$$

### Probability of Choosing $i$

$$p_i = \frac{A_i}{A} \quad i = 1, \dots, n$$

### Logistic version

$$p_i = \frac{e^{\lambda A_i}}{\sum_{j=1}^n e^{\lambda A_j}} \quad \lambda > 0$$



# *Day-to-Day Route Choice-Behaviour*

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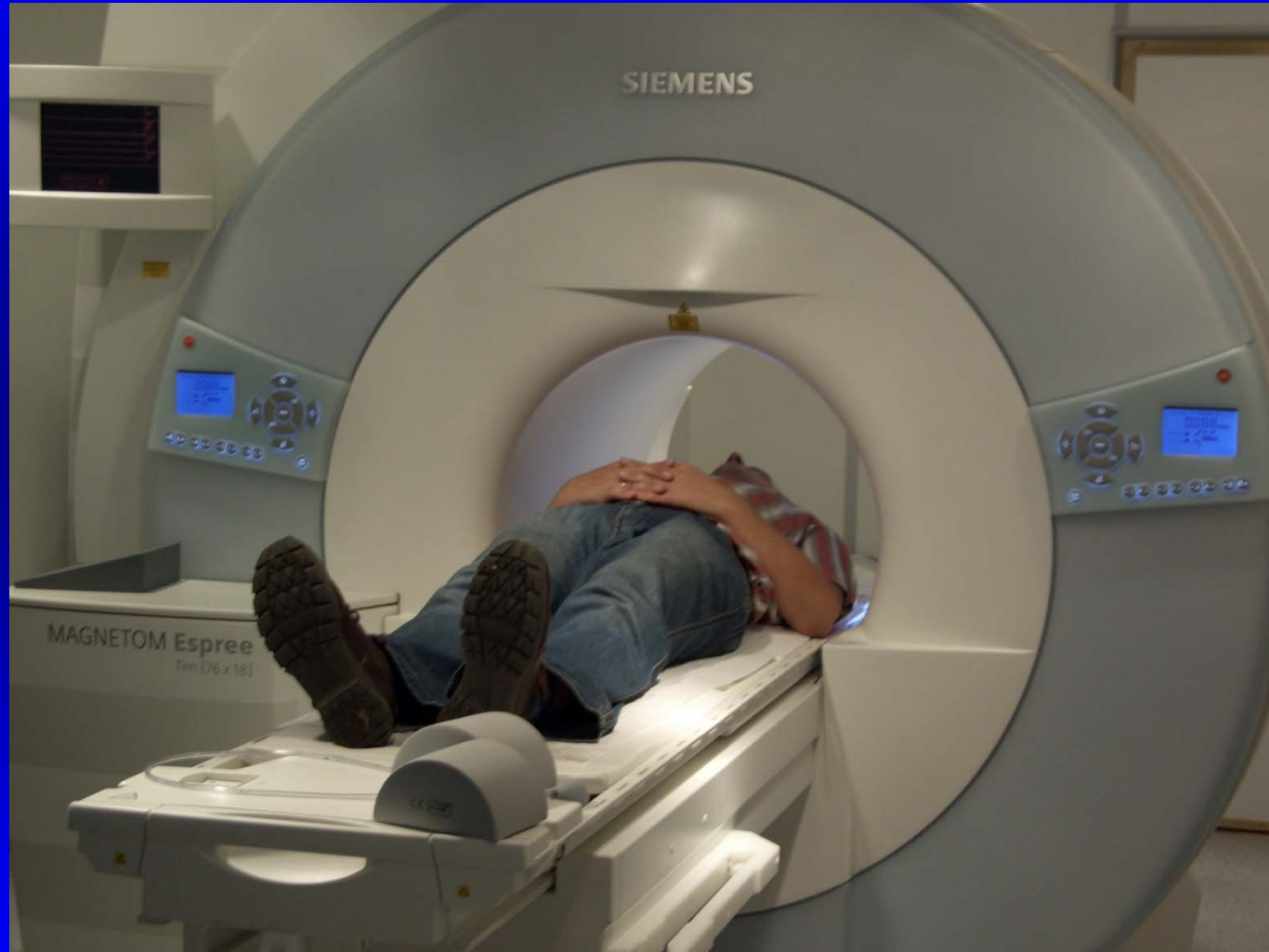
## *Results*

- 1. Mean number of players on main and side route is near to the equilibrium.*
- 2. Fluctuations remain in both experiments up to the end.*
- 3. Fluktuations are significantly lower in experiment II .*
- 4. The total number of route changes ist significantly larger in experiment I.*
- 5. Three typs can be classified: direct ("sensible", 44%), contrarian ("tactical", 14%) und conservative ("not sensible", 40,5% und "stoical", 1,5%).*
- 6. The number of route changes and the payments are in all in all experiments negatively correleted.*



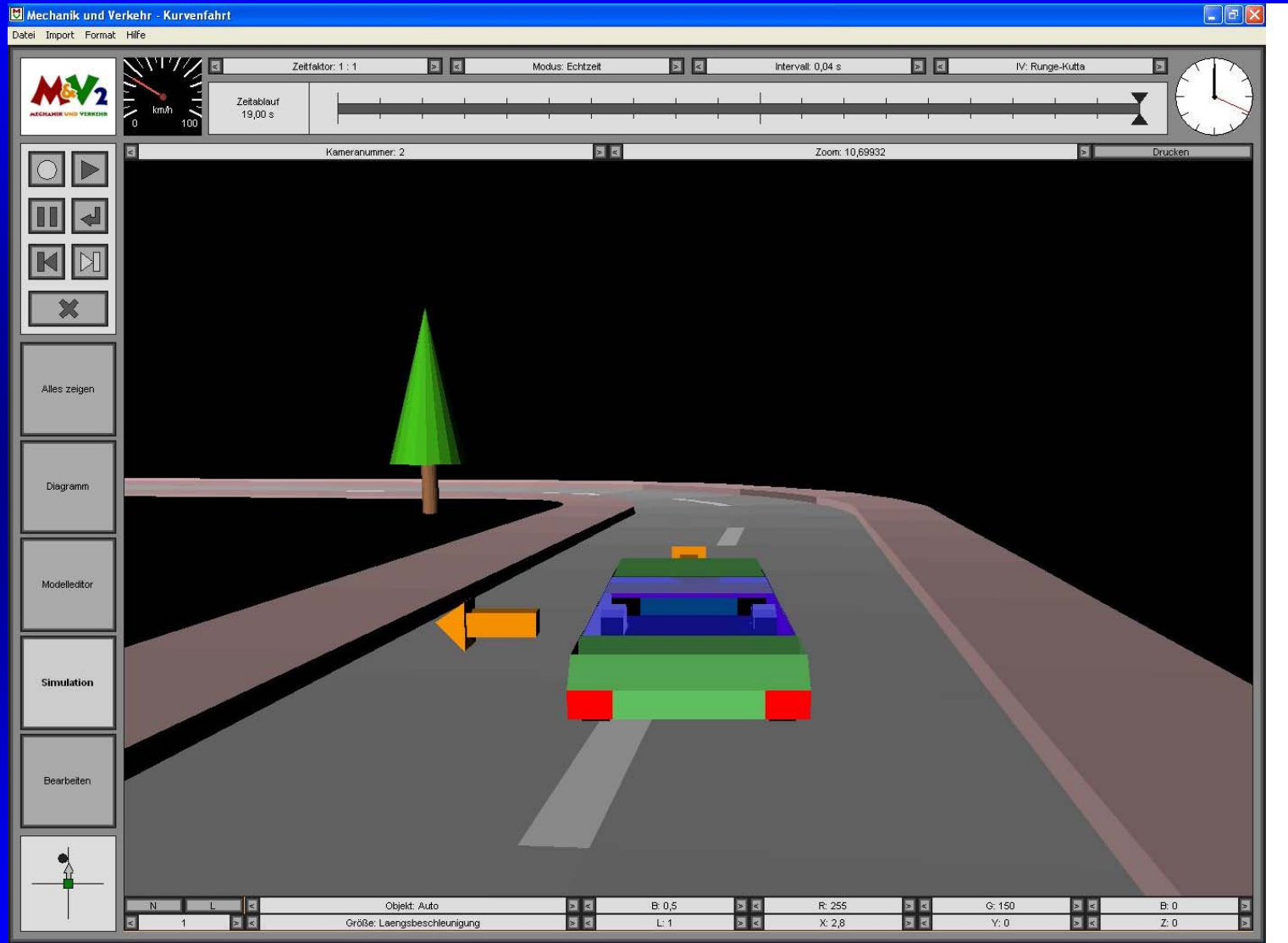
# *fMRI*

---

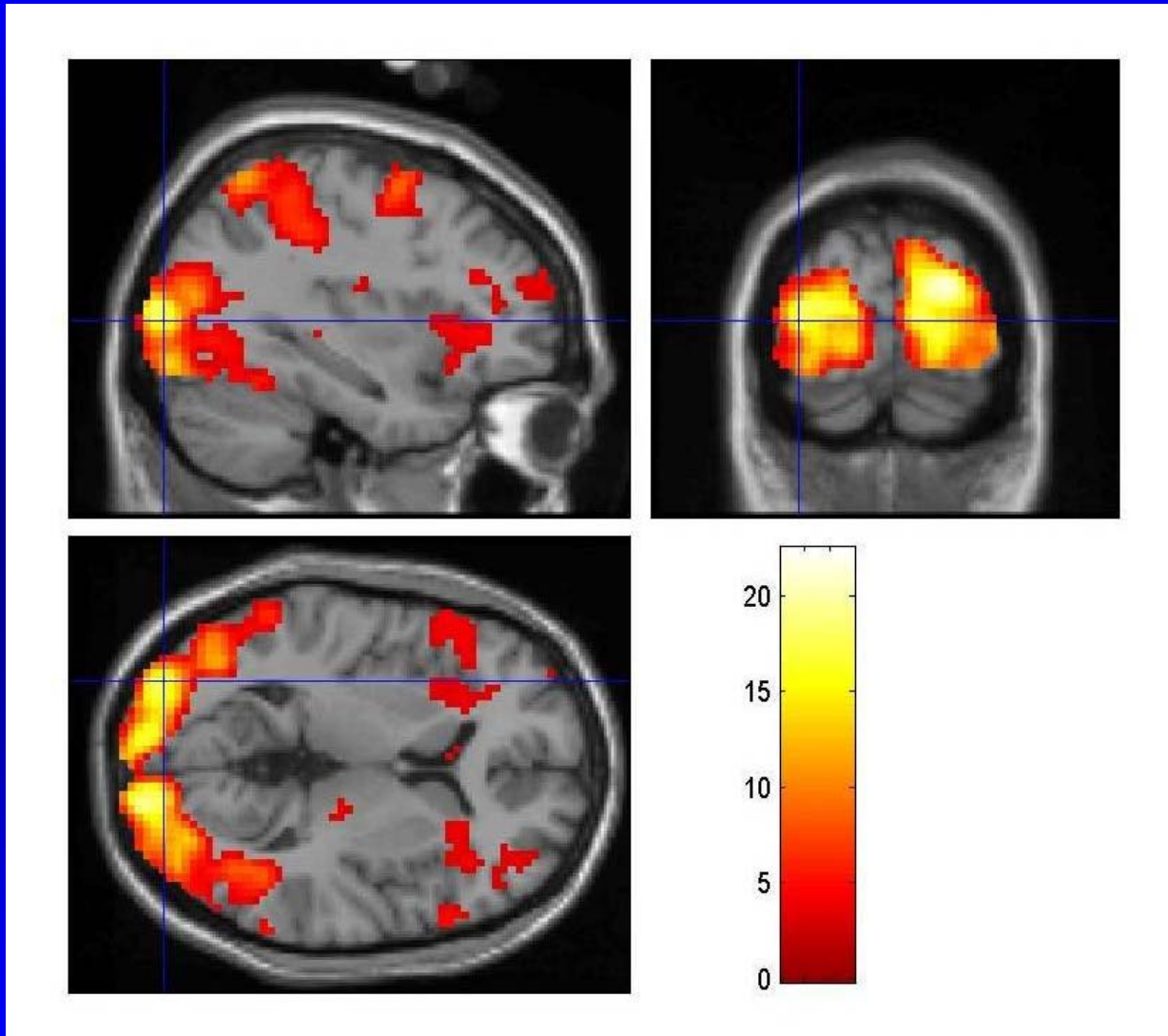




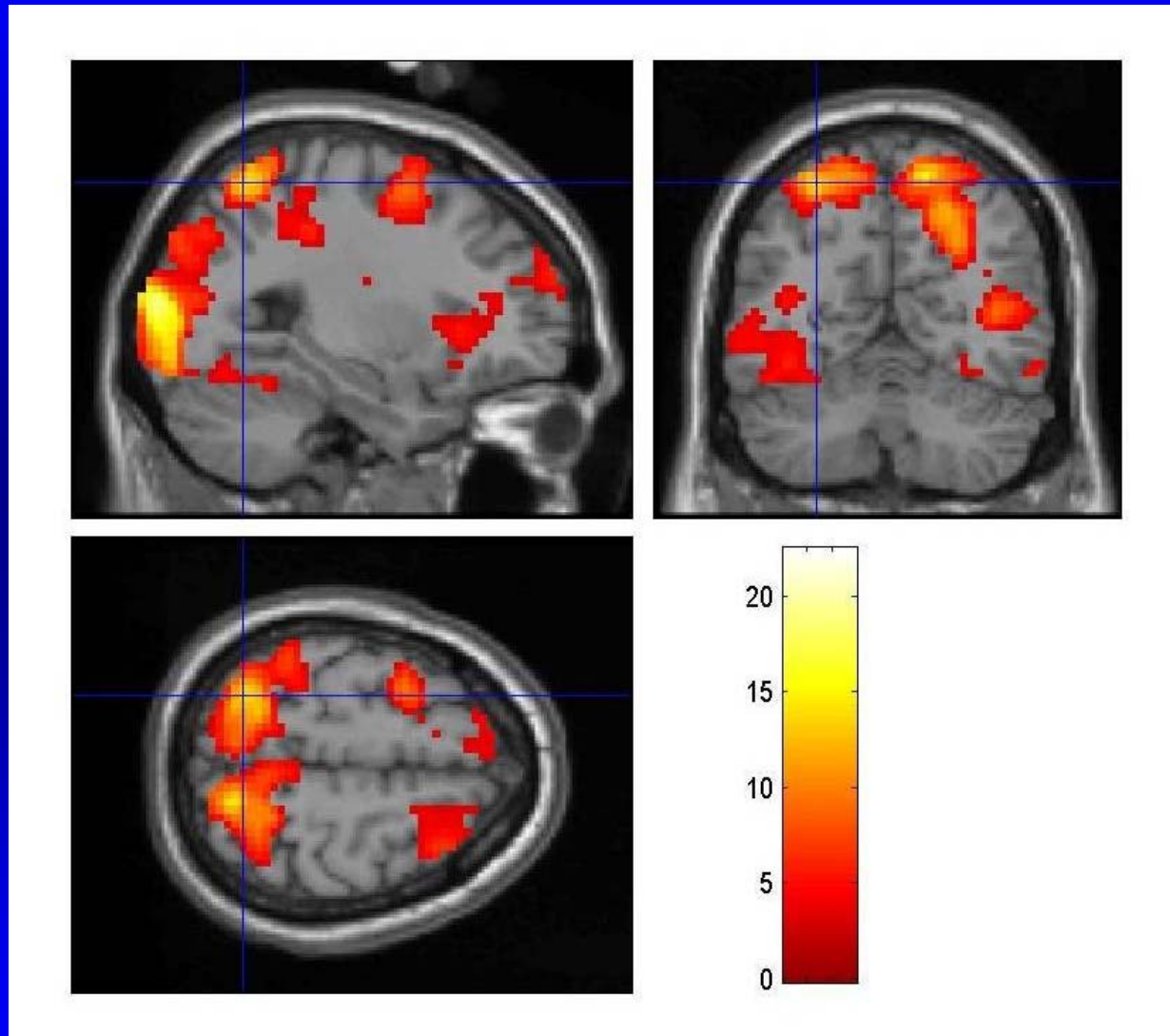
# Simulation



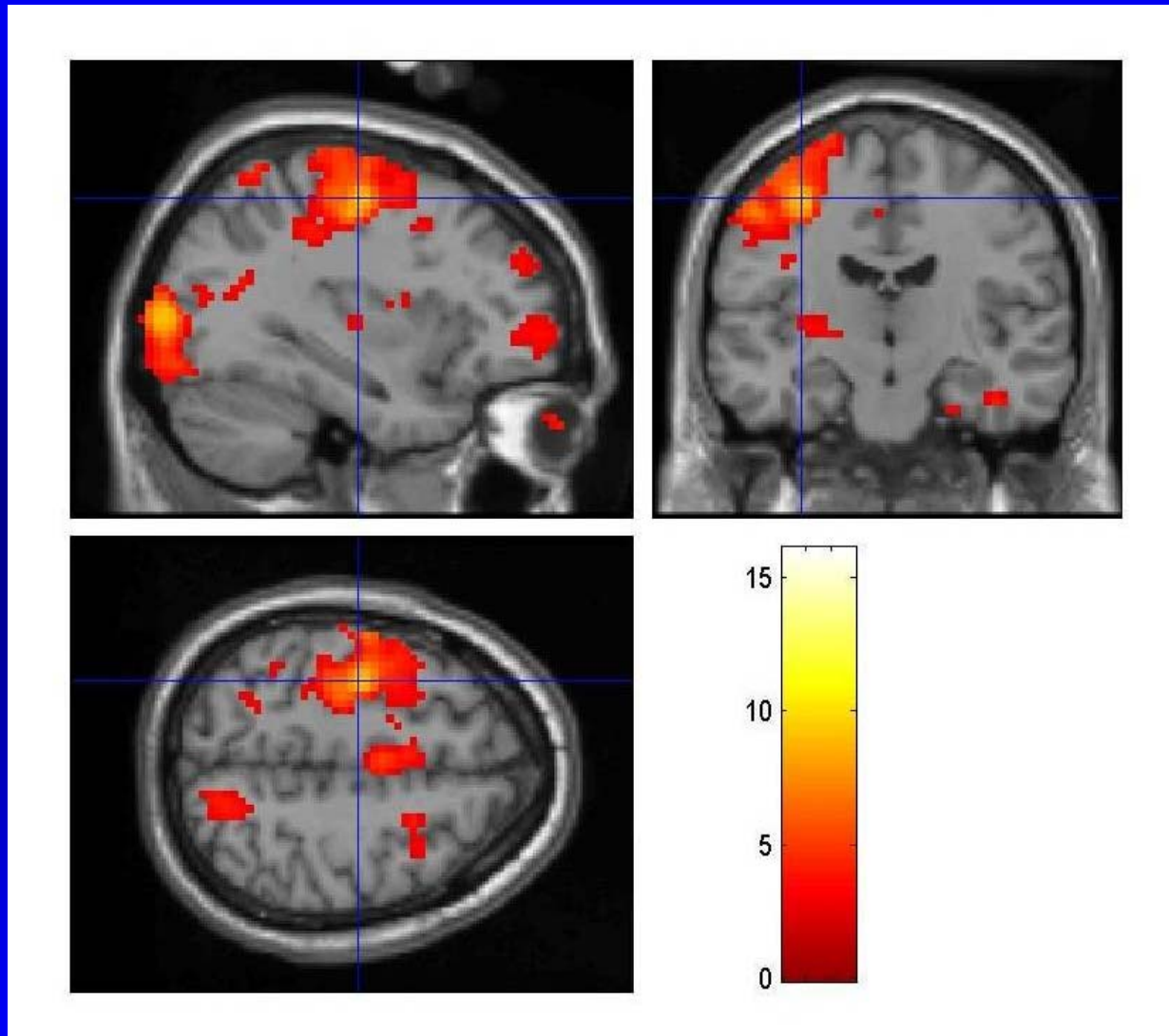
# Looking



# Looking

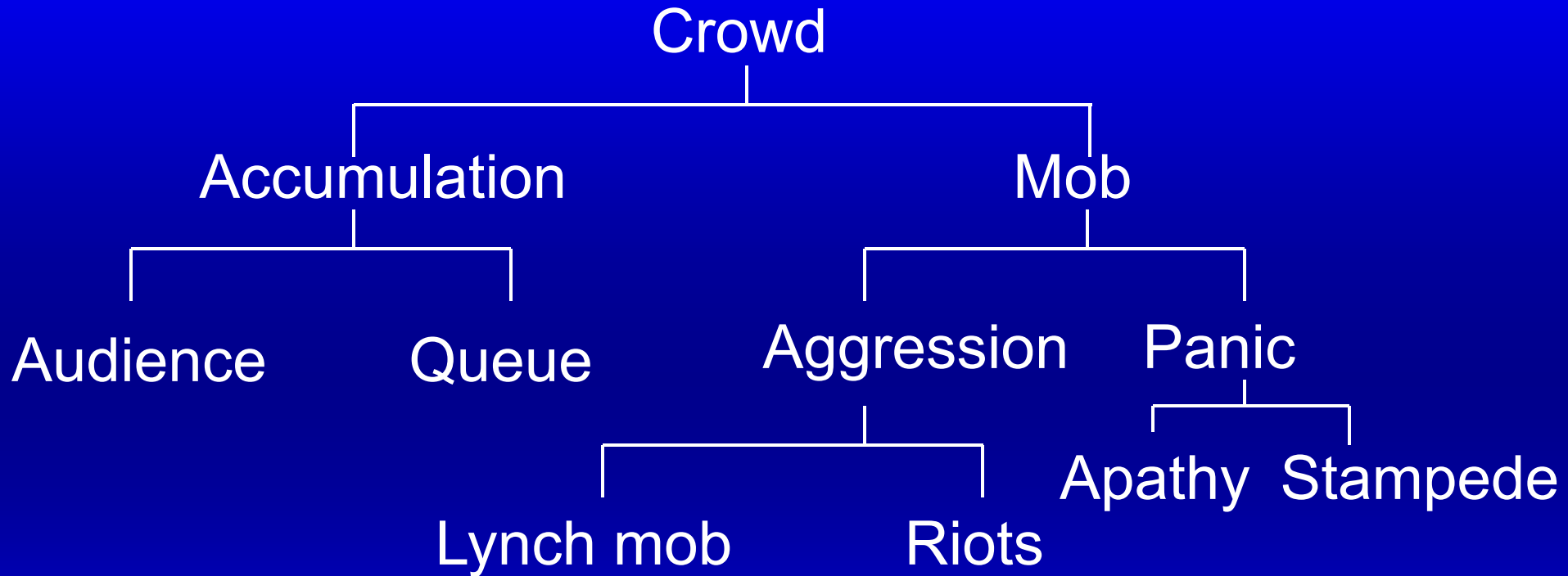


# Driving



# *Terms*

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# *Crowd Phenomena*

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Lane Formation

Jams and crowd





# *Lane Formation*

---





# *Simulation?*

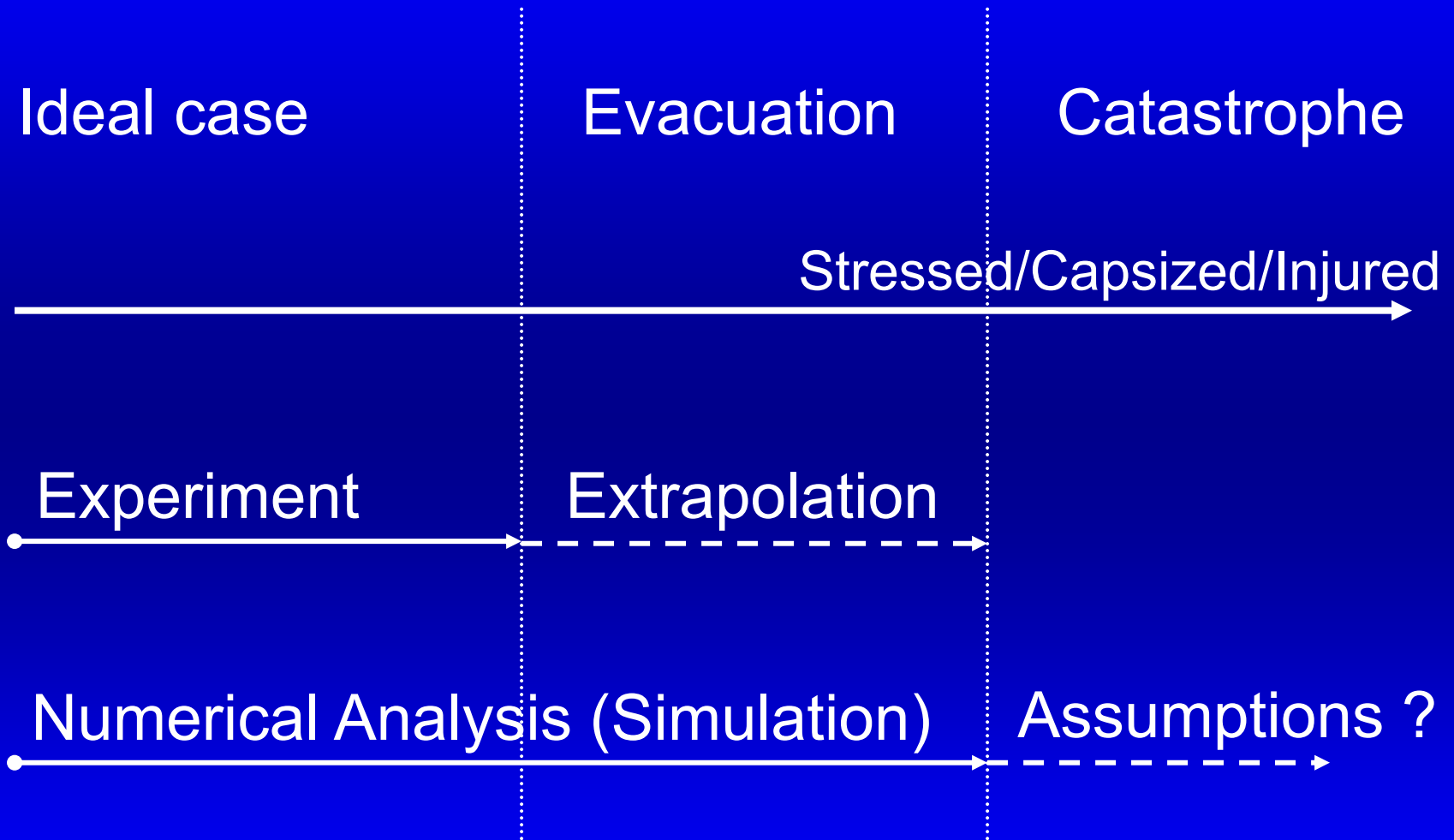
---



(Waterpark Tokyo)



# *What is possible?*





# *Pan I*

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# *Pan II*

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# *Consequences of Panic*

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- Limited perception: tunnel look
- Herd instinct: attraction at larger distances
- Wet hands / feet > ...
- Blood flows from head / stomach into the motion musculature > desire to move
- Blood becomes thicker > faster formation of a scab
- Impatience > turning back
- Abolition of social connections (except own children)
- But also: passive panic > apathy



# *Evacuation of a Cinema*

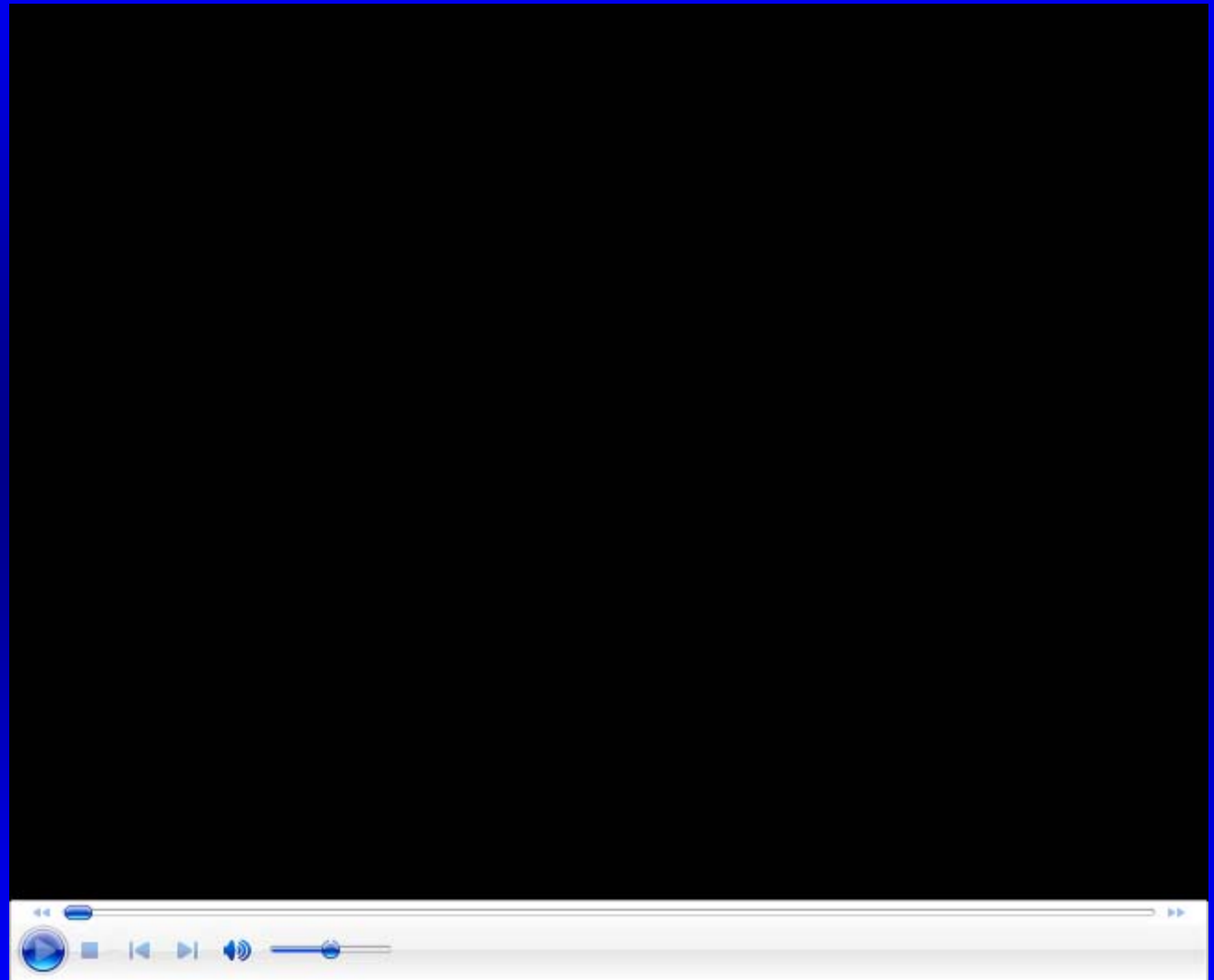
---

Simulation:

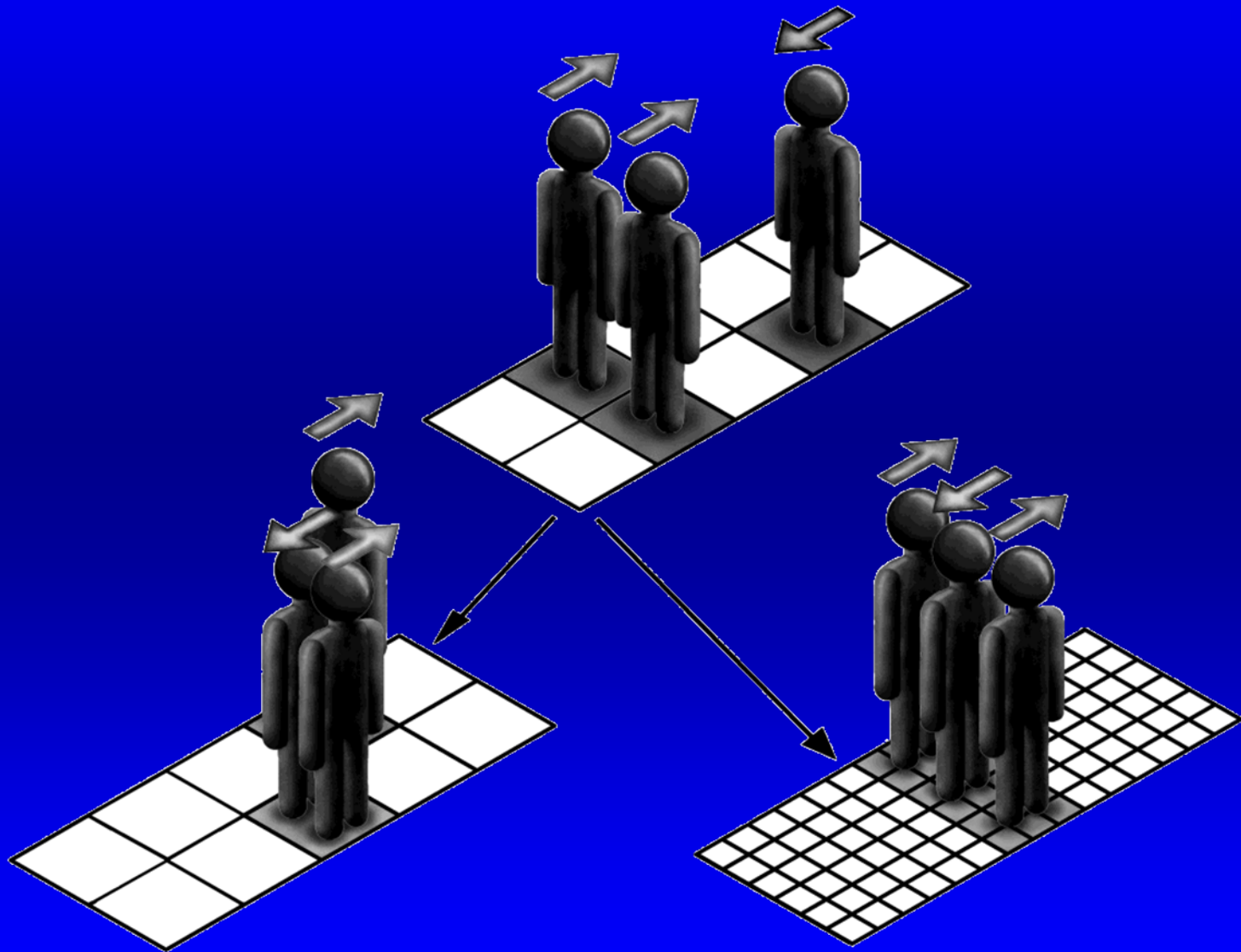
68 s

Reality:

66 s

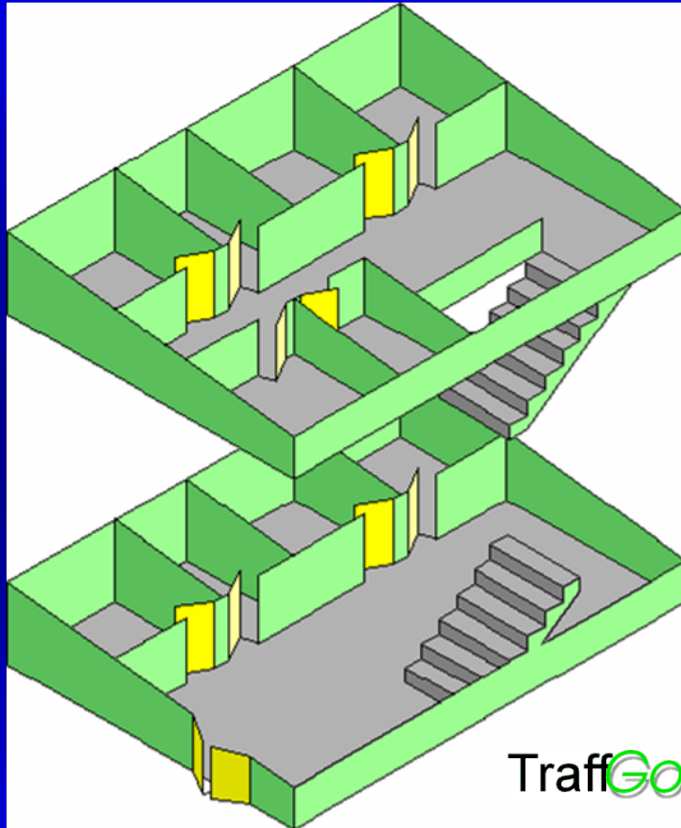


# *Pedestrian Dynamics*





# *Simulation, Discretisation*

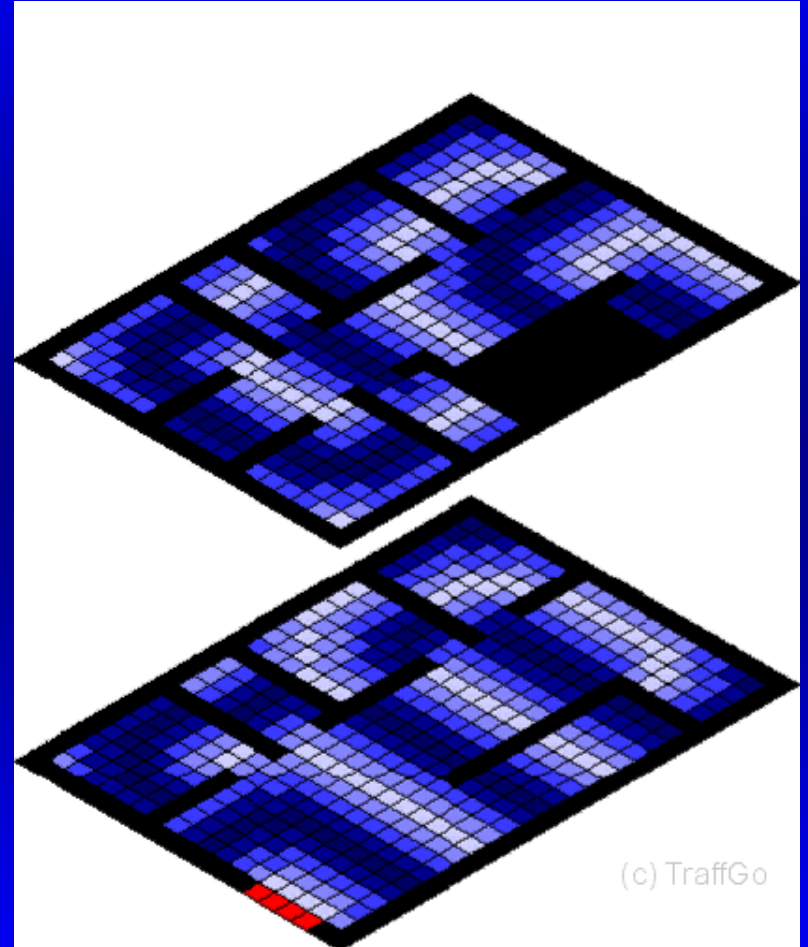
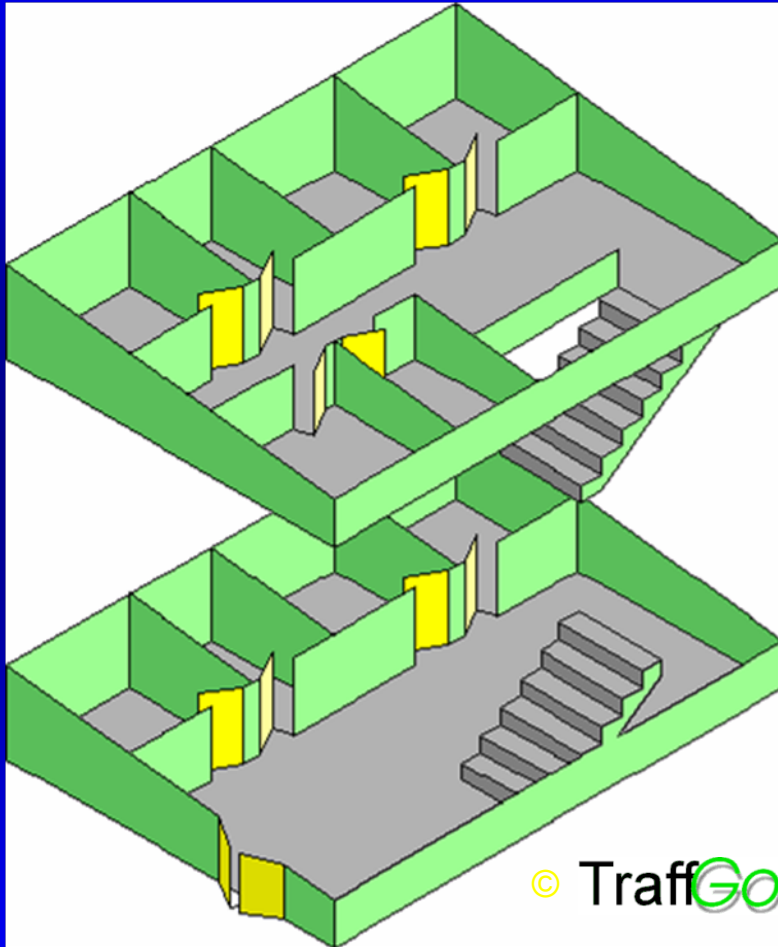


Zell size: 40 cm x 40 cm

- Available cells
- Blocked Cells
- Staircases
- Doors

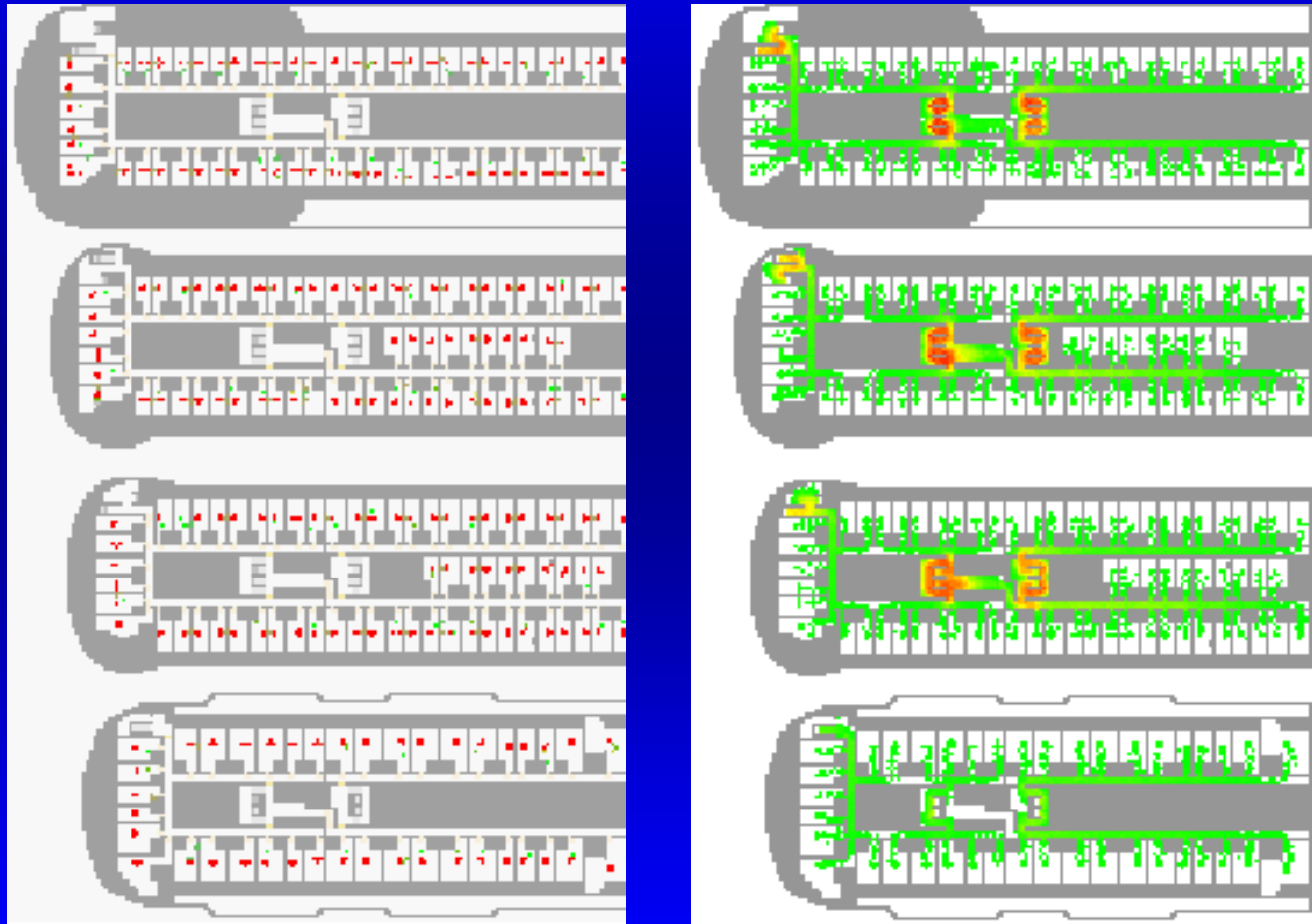


# Simulation, Orientation



# Example

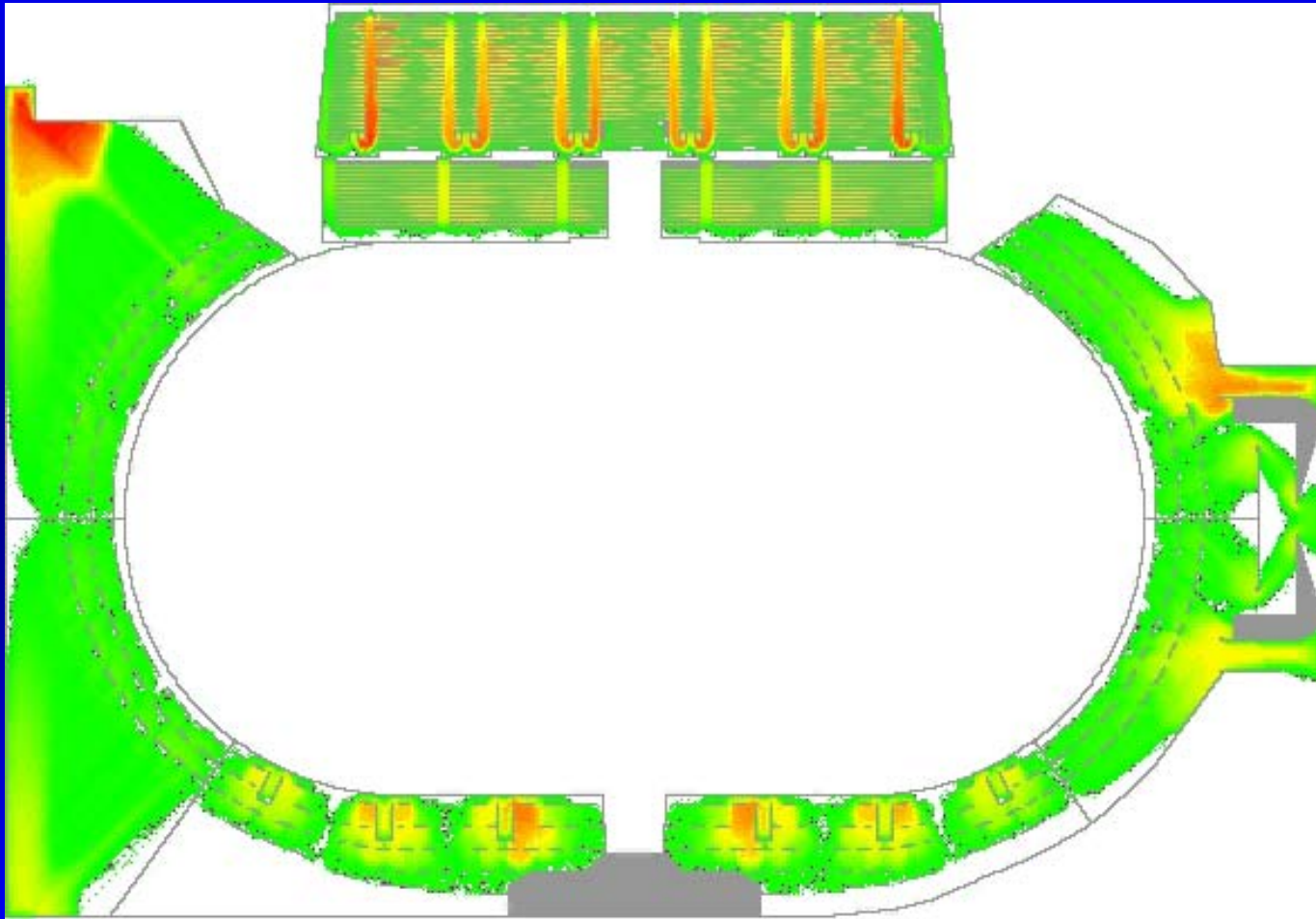
Passenger ship, 4 decks

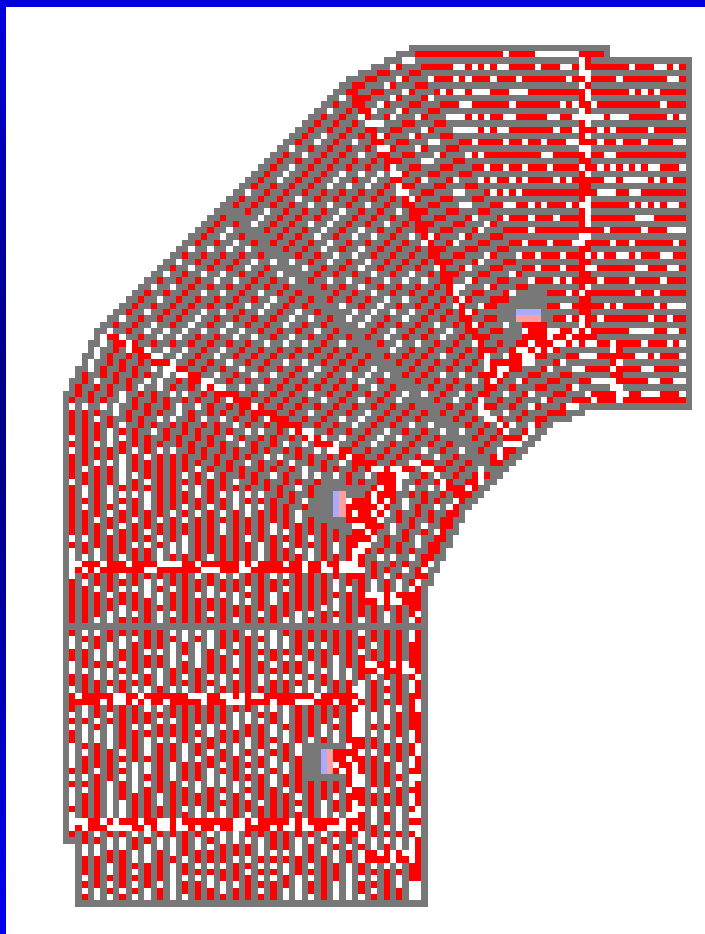


# *Evacuation of a Stadium*

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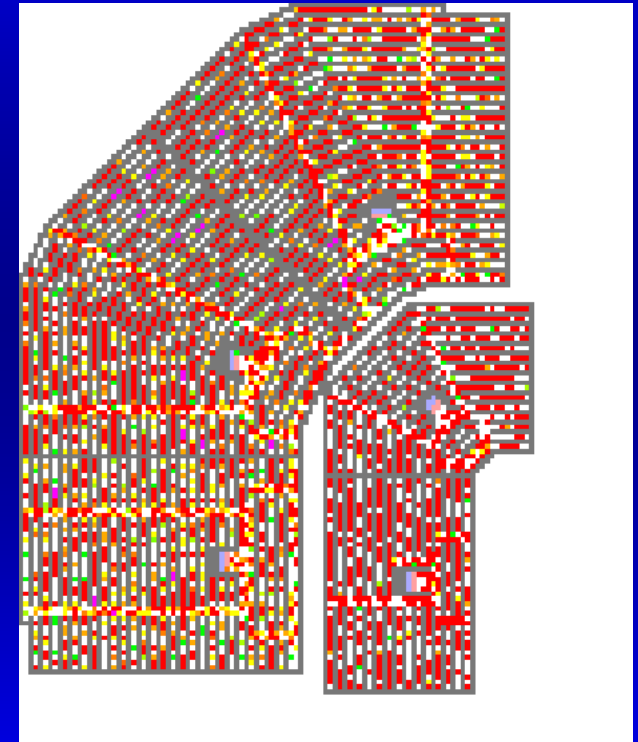




# Comparison I



T = 2 Minuten



T = 20 Sekunden

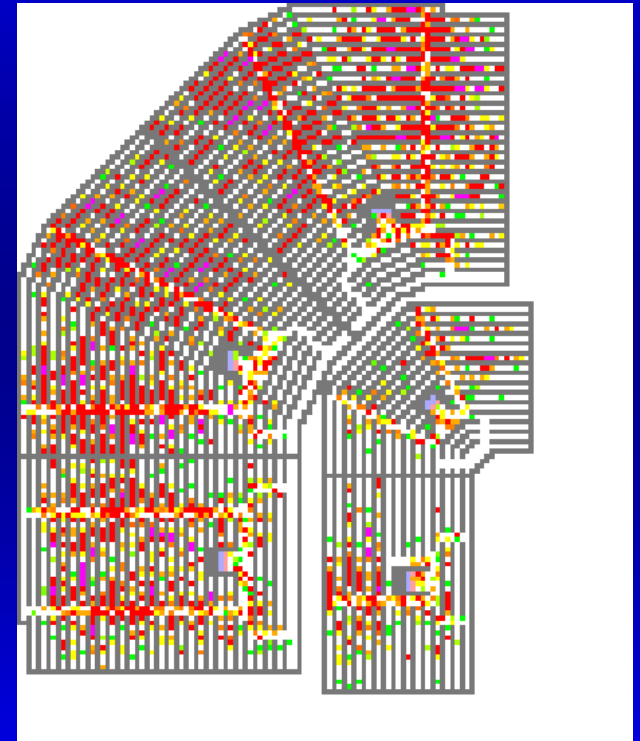




# Comparison II



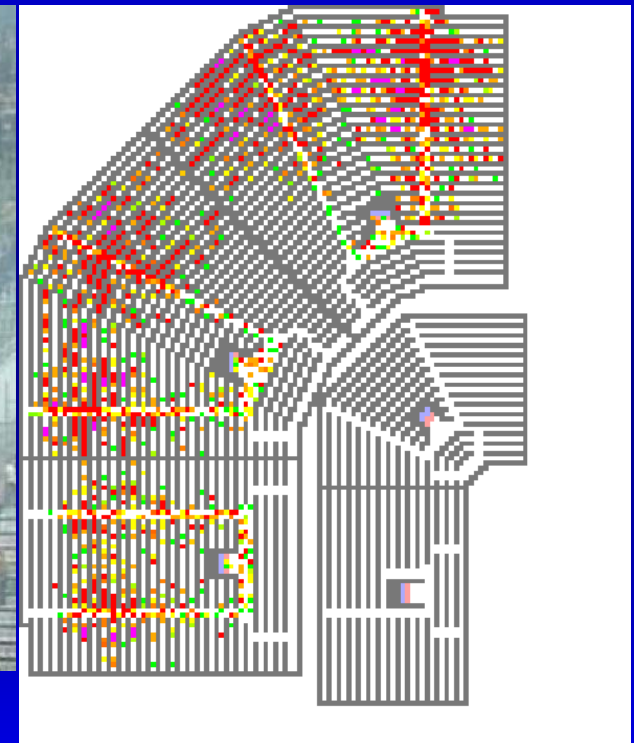
T = 5 Minuten



T = 3 Minuten



# Comparison III

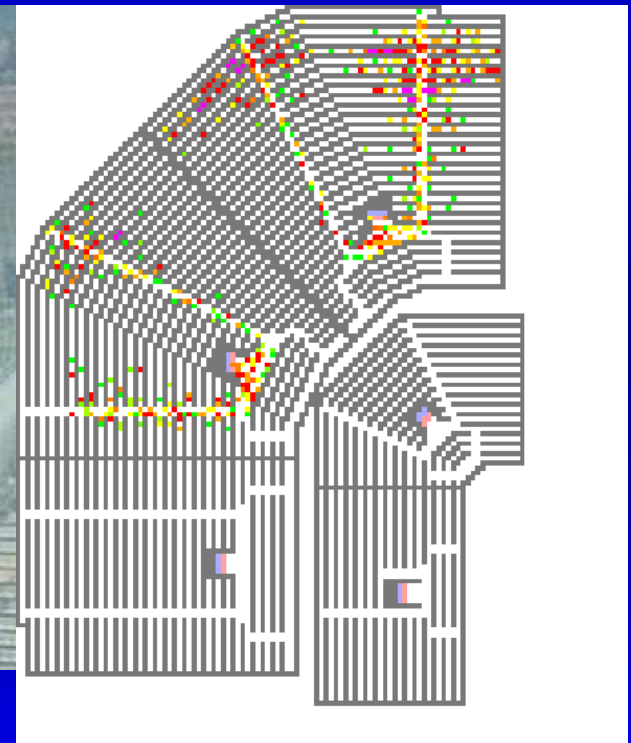


T = 7 Minuten

T = 6 Minuten



# Comparison IV



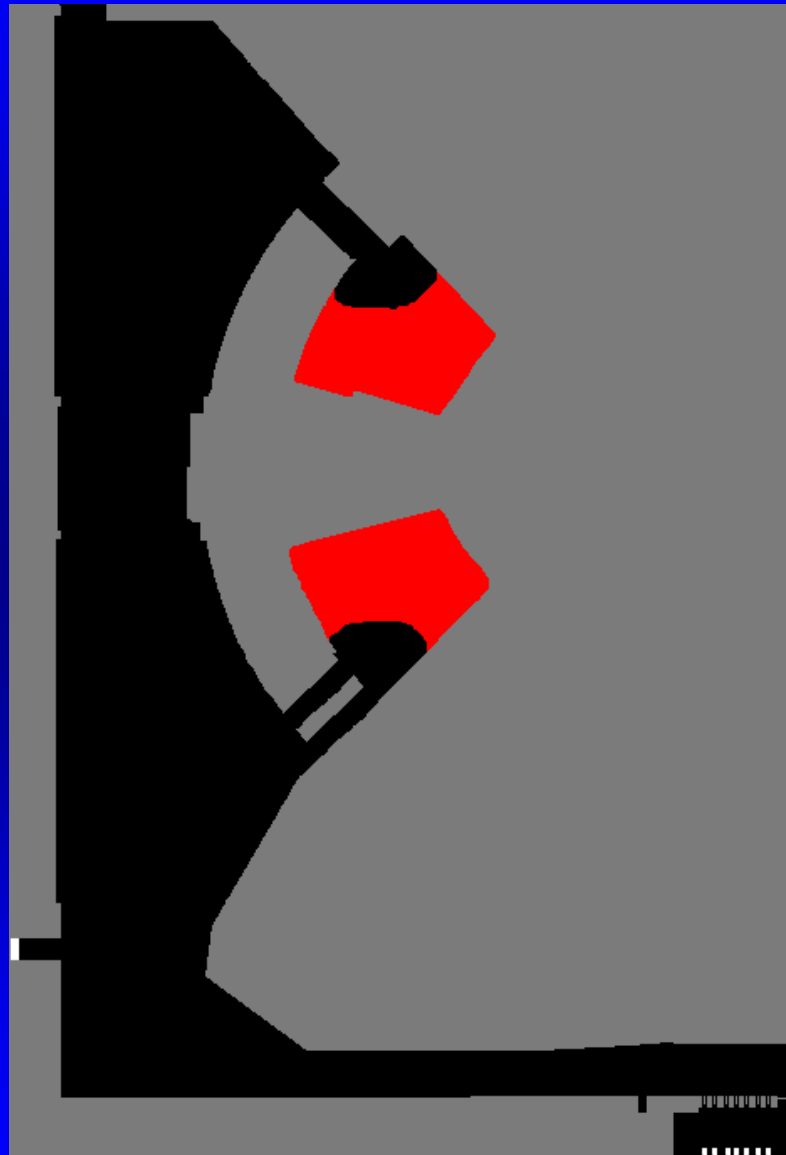
T = 10 Minuten

T = 10 Minuten



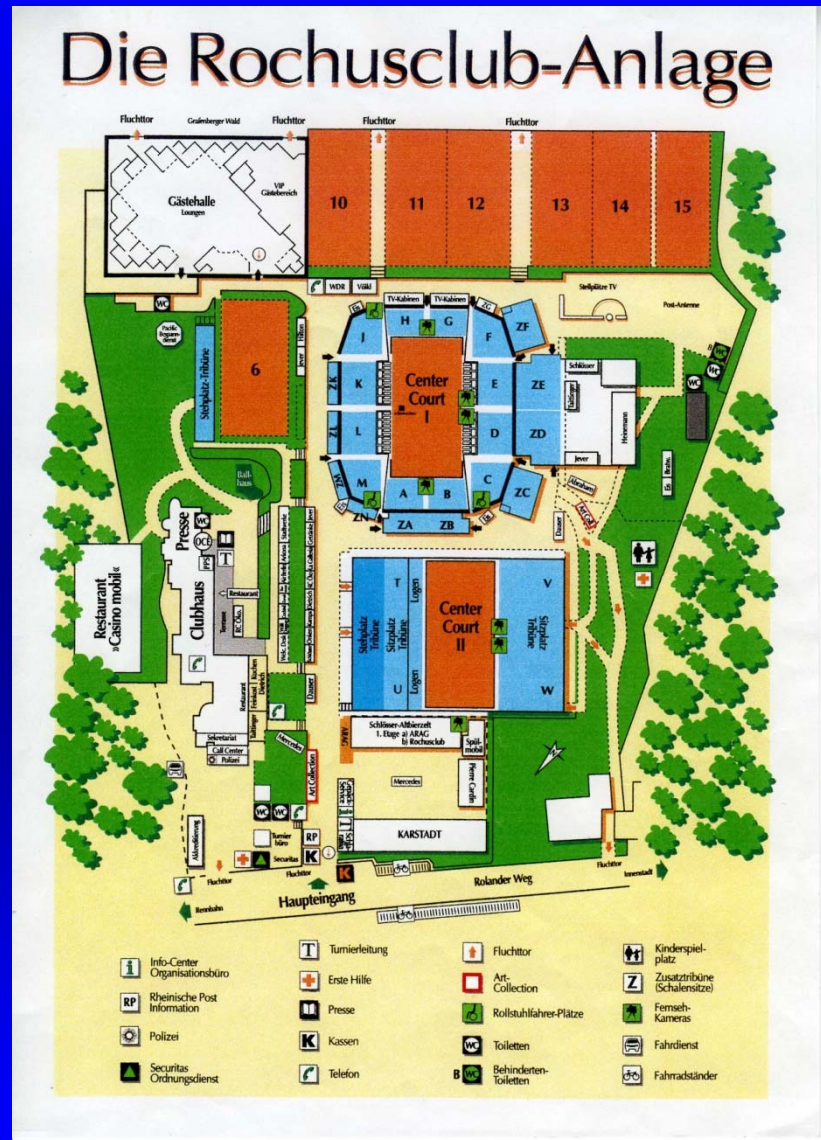
# *Berlin Stadium*

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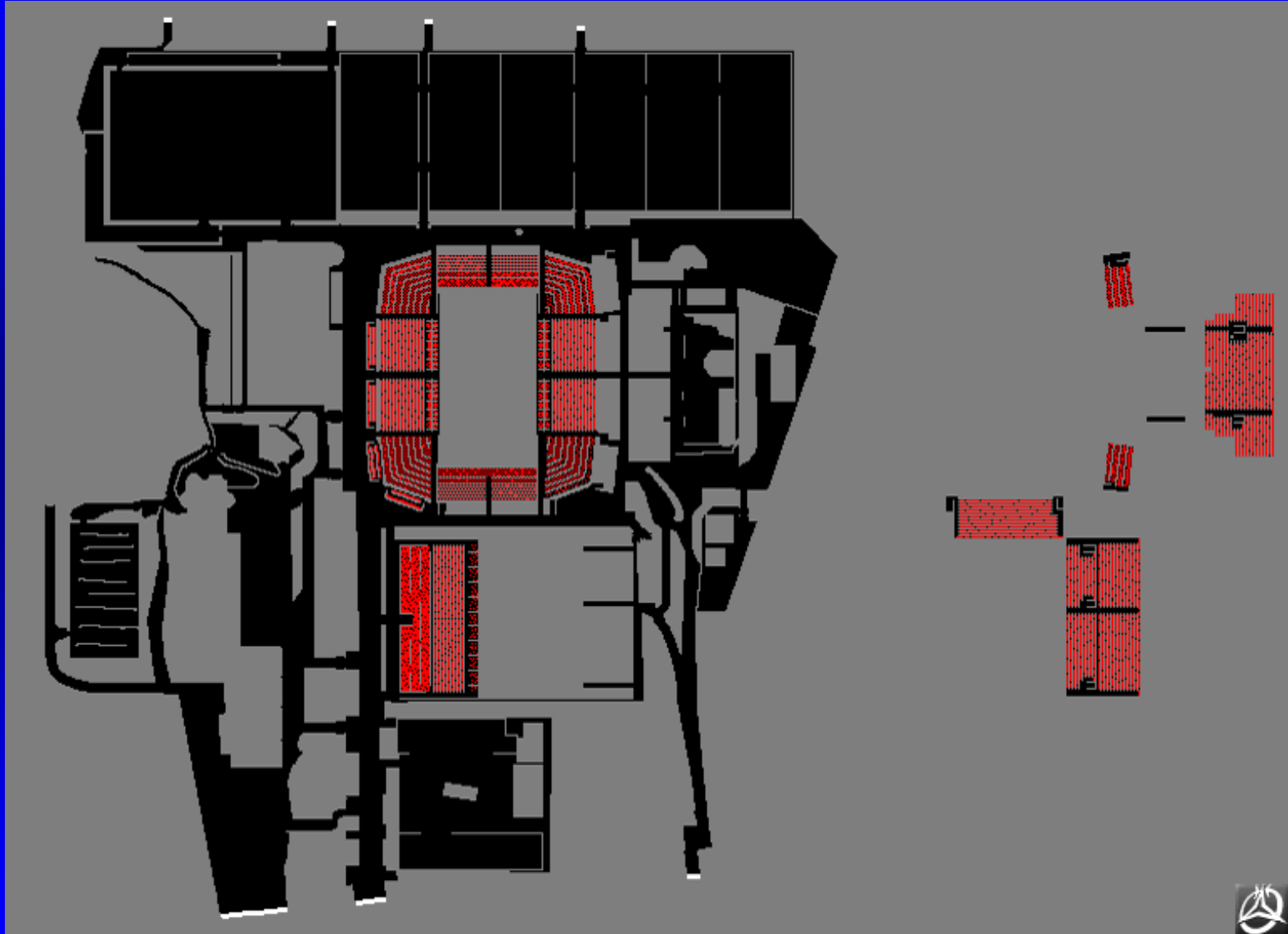




# Rochusclub Düsseldorf

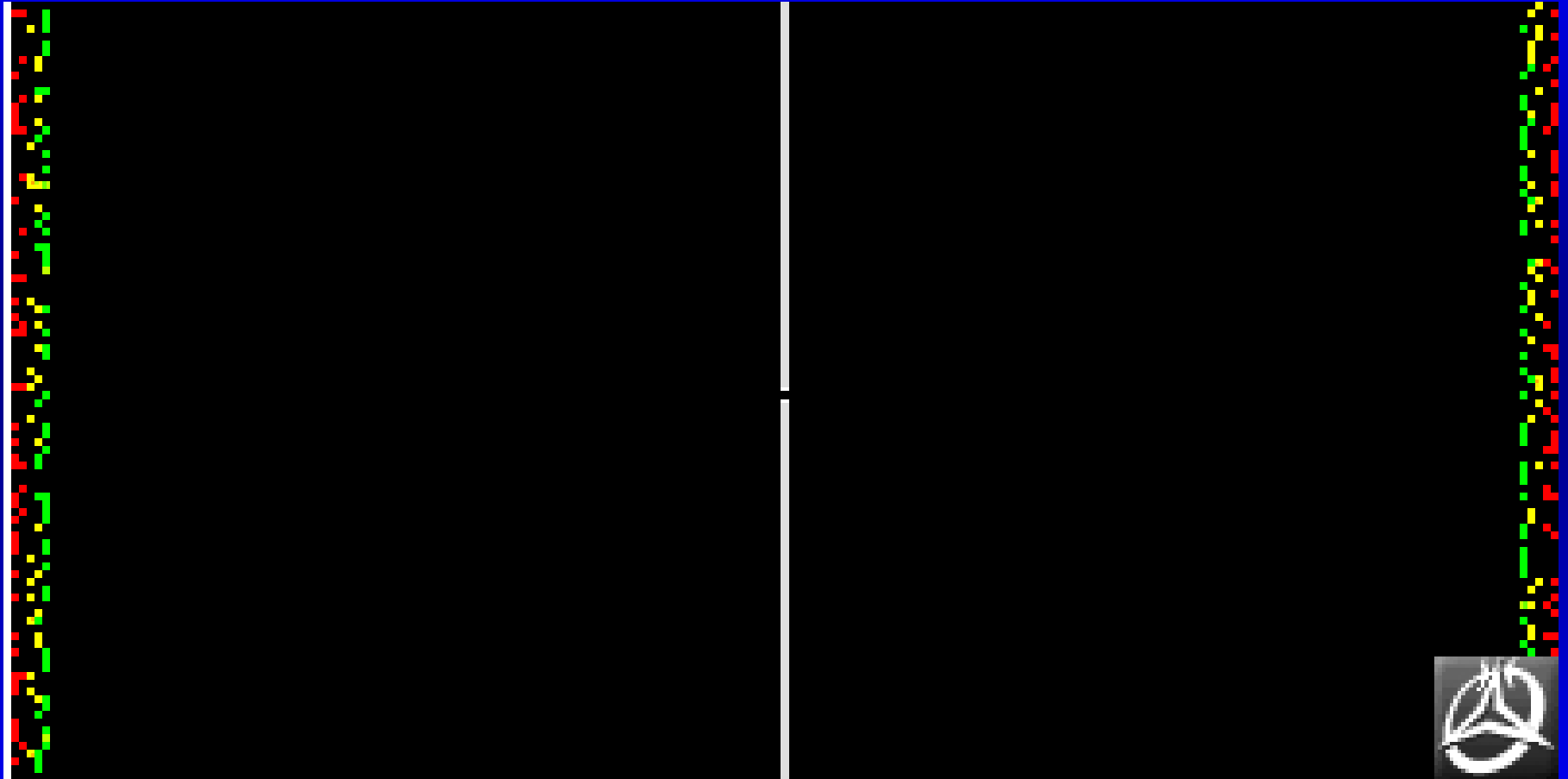


# Tennis Arena



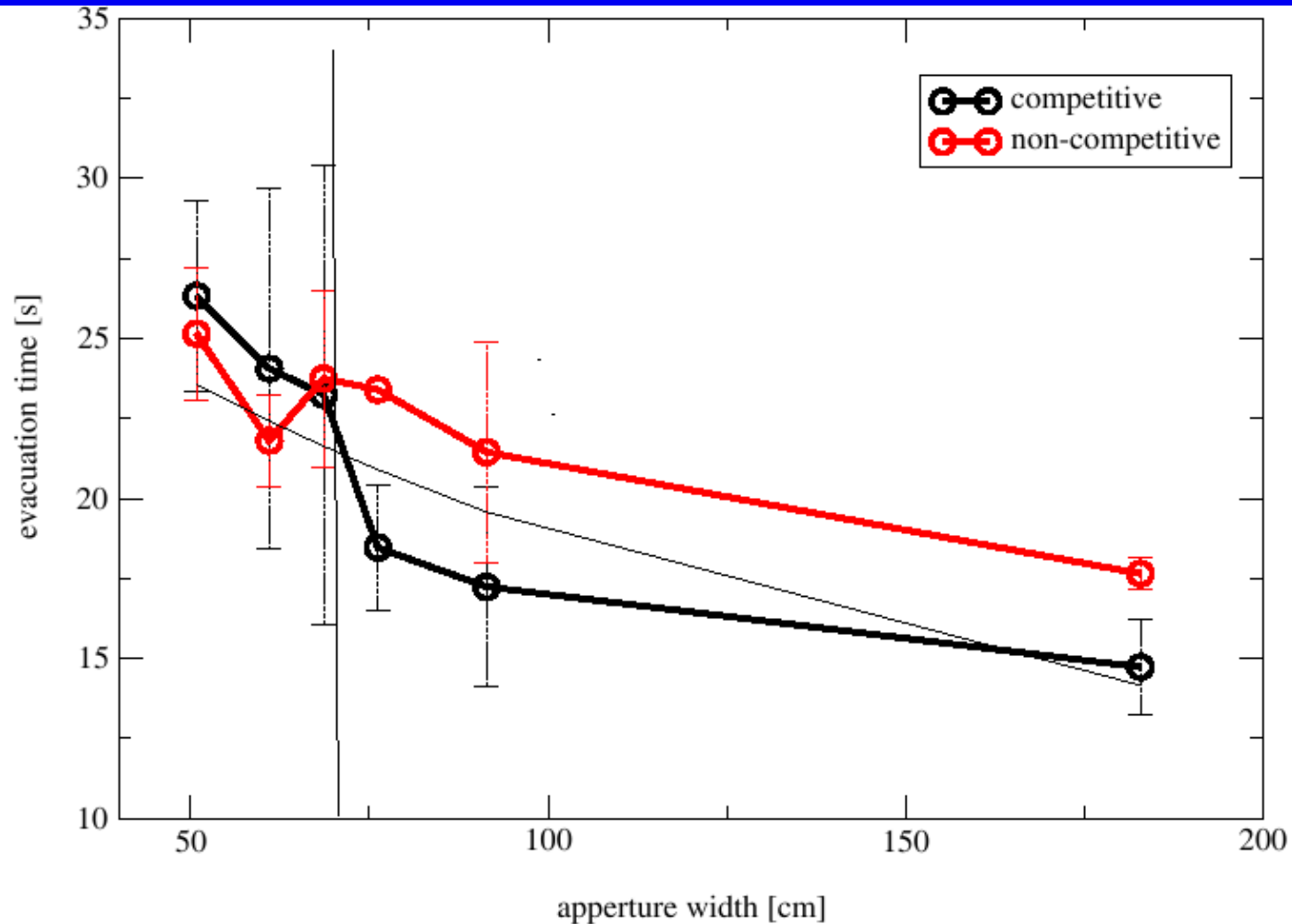
# *Bottleneck Counterflow*

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# Competition



# Hajj

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# Hajj

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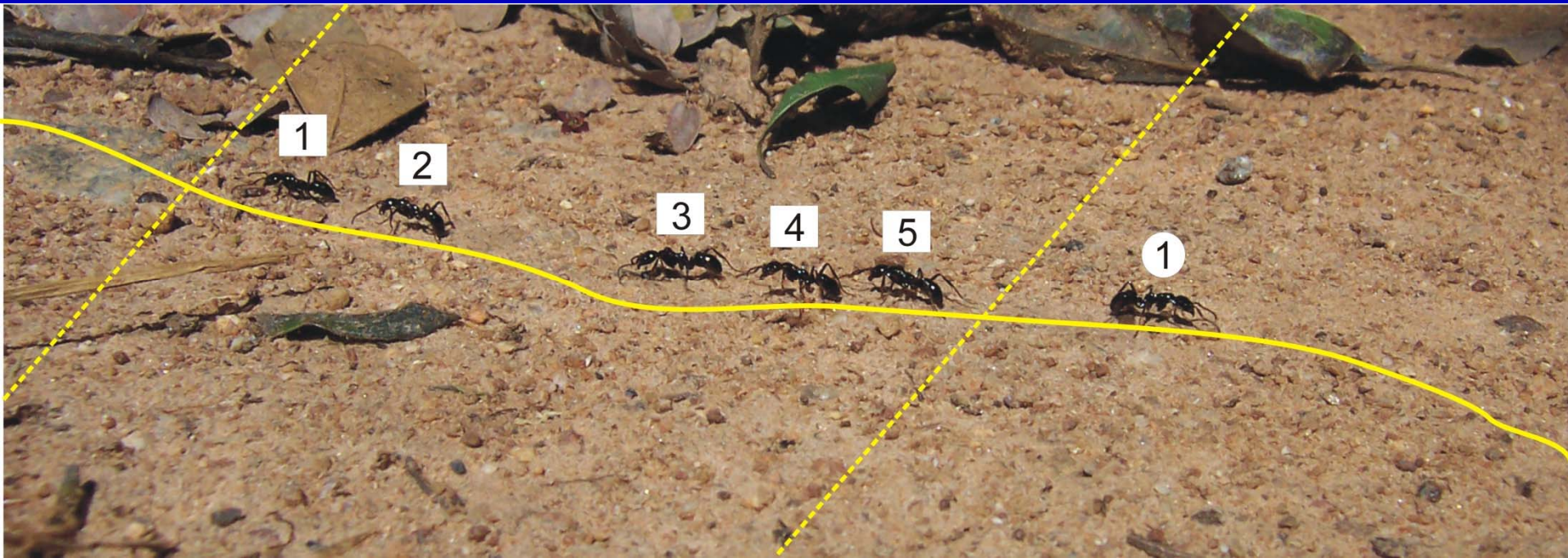
# *Ant Traffic*

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# Ant Traffic



# *Ant Traffic*

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# *Ant Accident*

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# *Ant Trails*

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<http://www.ptt.uni-due.de>

Conferences:

TGF '09: 22 – 24 June 2009, Shanghai

PED '10: 08 – 10 March 2010, Washington

